LECTURE NOTES

ON

MATHEMATICS-II

ACADEMIC YEAR 2021-22

I B.TECH -II SEMISTER(R20)

D.SANDHYA RANI ,Assitant Professor



DEPARTMENT OF HUMANITIES AND BASIC SCIENCES

VSM COLLEGE OF ENGINEERING

RAMACHANDRAPURAM

E.G DISTRICT-533255



JAWAHARLAL NEHRU TECHNOLOGICAL UNIVERSITY: KAKINADA KAKINADA – 533 003, Andhra Pradesh, India DEPARTMENT OF ELECTRONICS AND COMMUNICATION ENGINEERING

I Year - II Semester		L	T	P	C	
1 Tear - 11 Semester		3	0	0	3	
NETWORK ANALYSIS						

UNIT - I

Introduction to Electrical Circuits: Network elements classification, Electric charge and current, Electric energy and potential, Resistance parameter – series and parallel combination, Inductance parameter – series and parallel combination, Capacitance parameter – series and parallel combination. Energy sources: Ideal, Non-ideal, Independent and dependent sources, Source transformation, Kirchoff's laws, Mesh analysis and Nodal analysis problem solving with resistances only including dependent sources also. (Text Books: 1,2,3, Reference Books: 3)

Fundamentals and Network Topology: Definitions of terms associated with periodic functions: Time period, Angular velocity and frequency, RMS value, Average value, Form factor and peak factor- problem solving, Phase angle, Phasor representation, Addition and subtraction of phasors, mathematical representation of sinusoidal quantities, explanation with relevant theory, problem solving. Principal of Duality withexamples.

Network Topology: Definitions of branch, node, tree, planar, non-planar graph, incidence matrix, basic tie set schedule, basic cut set schedule. (Text Books: 2,3, Reference Books: 3)

UNIT - II

Transients: First order differential equations, Definition of time constants, R-L circuit, R-C circuit with DC excitation, Evaluating initial conditions procedure, second order differential equations, homogeneous, non-homogeneous, problem solving using R-L-C elements with DC excitation and AC excitation, Response as related to s-plane rotation of roots. Solutions using Laplace transform method. (Text Books: 1,2,3, Reference Books: 1,3)

UNIT – III

Steady State Analysis of A.C Circuits: Impedance concept, phase angle, series R-L, R-C, R-L- C circuits problem solving. Complex impedance and phasor notation for R-L, R-C, R-L-C problem solving using mesh and nodal analysis, Star-Delta conversion, problem solving. (Text Books: 1,2, Reference Books: 3)

Coupled Circuits: Coupled Circuits: Self inductance, Mutual inductance, Coefficient of coupling, analysis of coupled circuits, Natural current, Dot rule of coupled circuits, Conductively coupled equivalent circuits- problem solving.

UNIT - IV

Resonance: Introduction, Definition of Q, Series resonance, Bandwidth of series resonance, Parallel resonance, Condition for maximum impedance, current in anti resonance, Bandwidth ofparallel resonance, general case-resistance present in both branches, anti resonance at all frequencies. (Text Books:2,3, Reference Books: 3)

Network Theorems: Thevinin's, Norton's, Milliman's, Reciprocity, Compensation, Substitution, Superposition, Max Power Transfer, Tellegens- problem solving using dependent sources also. (Text Books: 1,2,3, ReferenceBooks:2)



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UNIT - V

Two-port Networks: Relationship of two port networks, Z-parameters, Y-parameters, Transmission line parameters, h-parameters, Inverse h-parameters, Inverse Transmission line parameters, Relationship between parameter sets, Parallel connection of two port networks, Cascading of two port networks, series connection of two port networks, problem solving including dependent sources also. (Text Books: 1,2, Reference Books: 1,3)

TEXT BOOKS:

- 1. Network Analysis ME Van Valkenburg, Prentice Hall of India, 3rdEdition, 2000.
- 2. Network Analysis by K.Satya Prasad and S Sivanagaraju, Cengage Learning
- 3. Electric Circuit Analysis by Hayt and Kimmarle, TMH

REFERENCES:

- 1. Network lines and Fields by John. D. Ryder 2ndedition, Asiapublishinghouse.
- 2. Basic Circuit Analysis by DR Cunninghan, Jaico Publishers.
- 3. Network Analysis and Filter Design by Chadha, Umesh Publications.

COURSE OBJECTIVES:

- To understand the basic concepts on RLC circuits.
- To know the behavior of the steady states and transients states inRLCcircuits.
- To know the basic Laplace transforms techniques inperiods'waveforms.
- To understand the two portnetworkparameters.
- To understand the properties of LC networksandfilters.

COURSE OUTCOME:

- gain the knowledge on basic networkelements.
- will analyze the RLC circuits behaviorindetailed.
- analyze the performance of periodicwaveforms.
- gain the knowledge in characteristics of two port network parameters (Z,Y,ABCD,h&g).
- analyze the filter design concepts in realworldapplications.

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Course Title	Year-Sem	Branch	Contact Periods/Week	Sections
NETWORK ANALYSIS	1-2	Electronics& Communication Engineering	6	-

COURSE OUTCOMES: Students are able to

- 1. Understand The Knowledge On Basic Networkelements. (K3)
- 2. Analyze The RLC Circuits Behavior Indetailed. (K4)
- 3. Analyze The Performance Of Periodicwaveforms. (K4)
- 4 Understand The Knowledge In Characteristics Of Two Port Network Parameters (Z,Y,ABCD,H &G). (K3)
- 5 Analyze The Filter Design Concepts In Real Worldapplications (K4)

Unit/ item No.	Outcomes		Торіс	Number of periods	Total perio ds	Book Refere nce	Delivery Method
	CO1: .Understand		Introduction to Electrical Circuits	•			
	the knowledge on	1 1	Introduction to Electrical Circuits	3			Chalk &
1	basic network		Network elements classification,		17		Talk,
	elements.		Electric charge and current, Electric				PPT,
			energy and potential			T1,T	Activ
						5, R3	e
						J, KJ	Learni
							ng
		1.2	Resistance parameter – series and	1			&
			parallel combination, problems,				C Tutorial
			1				Tatoriar
		1.3	Inductance parameter – series and	2			
			parallel combination Capacitance				
			parameter – series and parallel				
			combination				
				2			
			energy sources: Ideal, Non-ideal,	2			
			Independent and dependent sources,				
			Source transformation, Kirchoff's				
			laws, Mesh analysis				
			Nodal analysis problem solving with	2	1		
			resistances only including dependent				
			sources, Numerical problems				

			,				
			finitions of terms -Time period,	2			
			Angular velocity and frequency, RMS				
			value, Average value, Form factor and				
			peak factor, Phasor representation,				
			Addition and subtraction of phasors,				
			En mathematical representation of	2			
			sinusoidal quantities Principal of				
			Duality with examples. Principal of				
			Duality with examples.				
			Definitions of branch, node, tree,	3	1		
			planar, non-planar graph, incidence				
			matrix,problems, basic cut set				
			schedule. basic tie set schedule, E-				
			Class Room				
			TRANSIENTS			T2,R2	Chalk &
		2.1	Transients-introduction	3	1	, 	Talk,
	CO2 :		First order differential equations,				Active
	Analyze The RLC		Definition of time constants R-L				Learnin
2	Circuits Behavior		circuit with DC excitation				g &
	In detailed.	2.2	R-C circuit with DC excitation,	3	1		Tutorial
			problem solving, Solving second		10		
			order differential equations		10		
			L-C elements with DC excitation				
		2.3	R-L-C elements with AC	4	-		
			excitation Response as related to				
			s-plane rotation of roots Solutions				
			using Laplace transform method.,				
			problem solving				
			Steady State Analysis of A.C Ci	ironite			
		3.1	Response to sinusoidal excitation	5	1		
	CO3:	5.1	for pure resistance Response to				
	Analyze The Performance Of		sinusoidal excitation for pure				
3	Periodic waveforms		inductance Response to sinusoidal			TO TA	Chalk &
			_		12	T2,T4, R1	Talk,
			excitation for pure capacitance				Active
			impedance concept, phase angle				
							·

			series R-L circuit response series R-C circuit response series R-L-C circuit response Complex impedance and phasor notation for R-L CIRCUIT R-C, R-L-C problem solving using mesh and nodal analysis, Condition for maximum impedance, current in anti resonance Bandwidth of parallel resonance general case resistance present in both branches, anti resonance at all frequencies.	4			Learning & Tutorial
4	CO4: Understand The Knowledge In Characteristics Of Two Port Network Parameters (Z,Y,ABCD,H &G)	4.2	Network Theorems Thevinin's Theorem, problem solving Norton's Theorem, problem solving Milliman's Theorem Reciprocity Theorem Compensation Theorem Substitution Theorem Superposition Theorem Max Power Transfer Theorem Tellegens- Theorem, problem solving using dependent sources E-Class		8	T2,T3, R2	
	XO5: Analyze The Filter Design Concepts In Real World applications	5.3	introduction Z-parameters, Y-parameters, problems Transmission line parameters,Inverse Transmission line parameters problems h-parameters, Inverse h-		9	T1,T3, R3	
			parameters, inverse in- parameters, problem solving Relationship between parameter sets,	3			

5.4 C	Parallel connection of two port networks, series connection of two port networks Cascading of two port networks, problems problem solving including dependent sources, problem solving E-Class Syllabus (topics covered beyond the syllabus)	3		
	TOTAL	56		

LIST OF TEXT BOOKS AND AUTHORS

Text Books: T1.Electric Circuits by A.Chakrabarthy

- T2. Network Theory by A.Sudhakar & Shyam mohan S Palli
- T3.Network Analysis ME Van Valkenburg, Prentice Hall of India, 3rd Edition, 2000.
- T4. Network Analysis by K.Satya Prasad and S Siva naga raju, Cengage Learning
- T5. Electric Circuit Analysis by Hayt and Kimmarle, TMH

Reference Books:

- R1. Network lines and Fields by John. D. Ryder 2nd edition, Asia publishing house.
- R 2. Basic Circuit Analysis by DR Cunninghan, Jaico Publishers.
- R3. Network Analysis and Filter Design by Chadha, Umesh Publication

NETWORKS NOTES

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 - 2. Theorems 100 2 phillsubnos ali 02

 - 3. L.T.

 4 Transients \(\frac{dc}{ac} \)

 5. Ac Analysis Thefor (And sentence) or joil expressed than
 - 1. Network Analysis Van valkenburg
 - 12. Engg. circuit analysis Hayte kemmerly
- 3. Previous papers: Gk pub.
 - (i). GATE (1990-2007) (ii). RES EE

 - (iii). BAS Prelims EE / Ray kand lent look

this bottos or brings (32 contino Roll and)

us la phool Basics! The of the phool of the > The mechanism of energy stom through the conductor and ohm's law: is a man and and and

of 23 sait to sphibilothe conjuctor is subject bally axial electric ⊕ > Ag+ ion, immobile, larger in size ie 10° timeq than ē. · -> free e or story the story of

- → The mobility of free e's in a Ag, is several times to that of other conductors so its conductivity is very high.
- Generally in any conductor, there are (ie per unit cube)

 10¹⁸ to 10²³ atoms per unit volume and hence
 there are 10¹⁸ to 10³ free e s n in a Ag

 conductor. ie every conductor is a very
 rich of free e s.
- → In the presence of external field different free e will under go diff. forces [due to a large no. of free ēs] and hence they will move with diff. velocity. But only one velocity is defined, so called deift velocity. It is an avg. velocity of all the tree ēs within a conductor. and is given by vi = HE m/s.

 $\mu = \text{mobility of free } \bar{e} s \frac{m^2}{v-sec}$ E - Applied external field v/m $\rightarrow \text{The } k.E. \text{ associated with each free } \bar{e} \text{ is}$

 $KE = \frac{1}{2} m_0 u_0^2$ J effective mass $m = 9.11 \times 10^{-31} \text{ kg}$ (mezm)

me is the mass of tree e while it is in a motion.

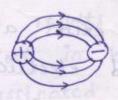
The first Half of the Ohm's experiment when the conductor not carrying electrical prince energy set = 0:- don = 0 . S IN = p

 \rightarrow when $E=0 \Rightarrow V_d=0 \Rightarrow k.E.=0$ ie all the free e are in the rest.

-> since the conductor is operating at room temp. (27°C of 300 K), diff. free Ex will acquire diff thermal energies (due to a large no. of tree e] and hence they will move in deff. directions in a random manner the net flow of e-motion in any direction zero, ie the charge motion is zero and the i is zero and also the current density [] tud jois ogeso. ways as tigu vag topusus soft to

when E=0, then J=0.

Second Half of ohm's experiment, when the conductor is carrying electrical energy



when the conductor is subjected to an axial electric I field, the force will be exerted on every face e.

e = - 1.6 x 10 9 c

Since 'e' is -ve, there exists the direction focce is in amosite to that of E. and hence there exists a net e motion ie the charge motion in the direction

opposite so that of 'E'.

The magnitude of charge is given by q = ne c , n = no of free e's crossing

a reference cs area, a variable quantity,

due a large no of free e.

 $e = -1.6 \times 10^{-19} c$

→ The time eate of flow of electric charges is nothing but the electric i ie

mon deline = 1 de l'Anton certificat es d'alon dell'error

since q is -ve, the conventional current direction is opposite that of the charge motion ie e motion (ie in the dire. of *) The current per unit es area is nothing but the current density resulted within a conductor

ie $J = \frac{i}{s} A Im^2$

since 's' is a scalar, the dire of j' is in the dire of i', ie in the dire of E.

Acc. to. Ohm, there exists a linear relation blw the applied electric field and resulting current density by Jak J- of J- ohm's law in the field theory

or -> conductivity of the conductor.

hence there exists a net & hotion

charge modion

J-E characteristics:
At the origin $E = 0 \Rightarrow J = 0$ and σ is not equal to zero.

Limitation:-

only when proportionality const. o is const. ie the temp. is kept condition.

At the const. E, as temp. increases from room temp. there exists an increase in collisions among the free es and hence the mobility falls, so the conductivity decreases. (Here the collisions blw the free e's and +ve ions are assumed to be const., since E is kept constant.]

At a const. TEMP. as 'E' increases there exists an increase in collisions blw the free es and the tree ions [larger in size], which results the fost in vy and hence the lost in K.E. This losted energy will be dissipated in the form of heat, which results the volt deop across the conductor. I flere the collisions amount, the free es are assumed to be const, since the temp. is kept const.

-> Actually the ornosition for the energy flow is distributions ve through the conductor. But practically this is approximated into rassive lumped R, L, c's for lower treg-s [unto IMH] and hence now theory valid for only lower freques.

At higher freque we can't derive the lumped elements so no lumped electric nlw, so no nlw theory is field theory is applicable miss sadden good

field theory approach of solving the destributive electric n/w's are valid for all frequis starting from zero (DC).

so the currents through all the 3 passive Lumped elements will always flows from tve to -ve terminals.

Resistance
$$R:=$$
 $\Rightarrow \sin ce J = \sigma E$
 $\Rightarrow i = \sigma(\frac{v}{v})$
 $\Rightarrow v = (\frac{1}{\sigma s})i$
 $\Rightarrow v = Ri \rightarrow Ohm's law in ckt$
 $\Rightarrow k = \frac{1}{\sigma s}$
 $\Rightarrow k = \frac{1}{\sigma s}$

Limitation: The Ohm's law is valid when R is kept const ie temp. is kept const.

```
\rightarrow As T \uparrow \Rightarrow l \uparrow, s \uparrow, \frac{l}{s} = almost const.
   -> Rt = Ro (1+xt), x - temp. coe. in 1 c,
         which is +ve for all the conductors.
\rightarrow Since v = Ri \Rightarrow i = \frac{V}{R} = VG \rightarrow 3rd form
         of ohm's law. 1 = (11) b
                G = conductance v
        Since i = \frac{dq}{dt}, v = R \cdot \frac{dq}{dt} \rightarrow 4 + h form ohm's
   \rightarrow R = \frac{L}{\sigma s} \Rightarrow \sigma = \frac{L}{Rs} = \frac{m}{n - m^2} = \frac{v/m (or) s/m}{s}
   \rightarrow Resistivity e = \frac{1}{\sigma} = \frac{RS}{L} = \frac{\Lambda - m^2}{m} = \Lambda - m
   \rightarrow power p = \frac{d\omega}{dt} = \frac{d\omega}{dq} \cdot \frac{dq}{dt}
   \rightarrow P = i^2 R = v^2 /_R (\omega) = v \cdot i (\omega)
      > knergy dw = pdt => w = Spdt (3)
         \omega = \int i\hat{R} dt = \int \frac{v^2}{R} dt
   V-I characteristics:
  I Quadrant I Quadrant with iv
   on one of one
  total energy standards of the details
                      sont Witness (afterna
      observations :-
    1. Resistor is a linear, passive, bilateral
      and time invariant in v-1 plane.
       Inductance L:-
                       when a time varying i is flowing
       through the coil, a time varying v vog magnetic thuse will be produced.
                     The total flux produced gn = 4 (ab)
```

of flux per turn, N-no. of turns.
The total flux is proportional to the i through the coil ie pai rabith it + ve - for it of place conductors. The volt drop across the coil is $v = \frac{d\psi}{dt}$ de v = d (Li) = L. did 2'mdo to i = t 1 v. dt - o o t > o power $p = vi = L \cdot \frac{di}{dt} \cdot i = Li \cdot \frac{di}{dt} \cdot (\omega)$ Energy w= Indt $= \int \text{Li}\left(\frac{\text{di}}{\text{dt}}\right) \cdot \text{dt} \quad (3)$ $P = Li \frac{di}{dt} = \frac{d}{dt} (\% Li^2)$ $\omega = \int \frac{d}{dt} \left(\frac{1}{2} L_{i}^{2} \right) dt$ $\omega = \frac{1}{2} Li^{2}(J)$ The energy stored in the inductor at any instant will depends only on the correct through the inductor, this is total energy stored by inductor from infinite past (-0) to present time 't' → The inductor is a linear,

-passive bilateral line passive, bilateral, time invariant element in ______ invariant element magnetic flux soil be produced.

The total flux produced got 4 (ab)

capacitor
$$c:=\frac{dy}{dt}$$
, $y \propto y$
 $y = cy$
 $y = cy$

- NOTE:- ALW PEY 1. WL = 1/2 Li2 and i = [#. dl
- @ Wc = 1/2 cv2 and v = 1 E. 11 so inductor stores energy in the fam of magnetic field and capacitor -> in the for of electric field. Types of Elements:
- 1. Active and passive
- 2. Linear and Non-linear
- 3. Bilateral and unilateral
- 4. Distributed and lumped
- 5. Time varient and invariant
- -> An element is said to be active if it delivers a net amont of energy to the outside world. Otherwise it is said to be
- -> An element is said to be linear if its char. & for all time 't', is a st. line, through the origin, otherwise -> Non linear
- -> An element is said to be bilateral if "it offers same impedance for either dire. of i flow, -> otherwise -> unilateral.

element, if (i, v) is on the char-s then (-i,-v) must also be on the char.s.

At the thirt was

-> An element is said to be time inva-
rient if its chars doepn't change with
time affective a time varient.
-> The besides char. & also represents &
passive, Linear and bi-
lateral.
NOTE: The resistors, inductors, capacitors are
passive if and only if R70, L70 & C710.
Otherwise they are said to be active ie
RLO, LLO & CLO.
The v-1 chars of an element is shown in fig(b)
then the element -?
1). V Sinear, passive,
Dilateral element.
bilateral element.
(ii) Non-linear, passive, uni-
lateral element
delivery signs drawn with when the
(iii) > Non-linear, passive, Bi-lateral
TO THE PERSON OF
a samos applier dochi no ni oz
(IV). v -> Non-linear, passive
unilateral (Y) z = 3/3
Non linear, active 34 2
NOTE: No passive element will have -ve impedance
in any portion of its chars. so above charg tactive

```
The voltage-current relations in a resistor
i= zv2 then that element -?
Non linear, active, uni-
   Lateral
Quive y linear and property of
 inear, active

\Rightarrow linear, active

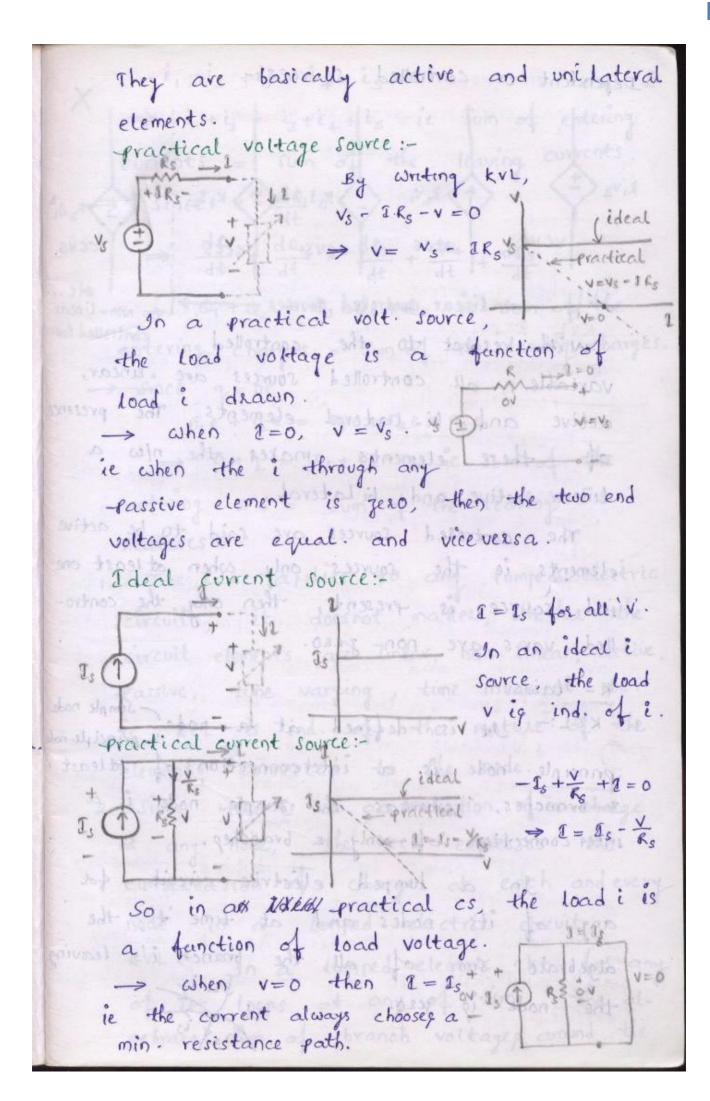
\Rightarrow bi-lateral (i,v) = (-3,5)

\Rightarrow =(3,-5).
  Otherwise they seeks had too best artificities
 Obs: - All the linear elements are always bi-
 lateral and converse need not be true.
  SOURCES:- V < Edeal

practical

dependent (s < Ideal

practical
    vevs vees eeus eees
  and adeal voltage sources:-
        + 11 from any source the energy
         delivery is from the tre terminal.
               Source voltage = Vs
       v=vs for all 2'.
    so in an ideal voltage source,
   the load voltage is indepen-
   dent of load i drawn.
   NOTE: - All the sources are inherently
   non-linear in nature, since the voltage
   and current relation is non-linear.
```



Dependent or controlled sources: fical voltage solves:-VEVE VEES VEEVS Leces with respect to the controlled controlled source variable, all controlled sources are linear, active and bi-lateral elements. The presence of these elements makes the nIW a linear active and bilateral. The controlled sources are said to be active elements ie the sources only when atleast one ind source is present, then only the controlled var s are non- gero. K- laws !-1. KCL:- It is defined at a node principle node principle node is a interconnection of atleast 3 branches, whereas the semple node is a interconnection of only 2 branches. In a lumped electric circuit, for

In a lumped electric circuit, tole any of its nodes and at time 't', the algebraic sum of all the branch i's leaving the node is geno.

$$-i_1 - i_2 + i_3 + i_4 + i_5 = 0$$

 \Rightarrow i, +i₂ = i₃+i₄+i₅ ie Sum of entering currents = sum of the leaving currents.

 \rightarrow Since $i = \frac{de}{1+}$

 $\Rightarrow \frac{dQ_1}{dt} + \frac{dQ_2}{dt} = \frac{dQ_3}{dt} + \frac{dQ_4}{dt} + \frac{dQ_5}{dt}$

⇒ 01+02 = 03+04+05 ie sum of the entering charges = Sum of the leaving charges. $\rightarrow \text{ since } q = ne,$ $n_1e + n_2e = n_3e + n_4e + n_5e$

⇒ n1+2 = n3+n4+n5 ie sum of the entering es = sum of the leaving es. -Features:-

- 1. The KCL applies to any lumped electric circuit, it does not matter, whether the circuit elements are linear, non-linear, active, passive, time varying, time invarient etc. ie KCL is ind. of the nature of the elements connected to the node.
- 2. Since there is no accumulation of a charge at any node, the KCL expresses the conservasion of charge at each and every node in a lumped electric circuit. KVL: In a lumped electric ckt fol any of its loops at any of time, the algebraic sum of branch voltages around the

loop is gero. $V - V_R - V_L - V_c = 0$ $V = V_R + V_L + V_c$ $V = V_R + V_L + V_C$ V

elements, present in a loop.

2. KVL expresses the conservation of energy in a every loop of a lumped electric ckt.

→ kcl + Ohm's law = Nodal Analysis

kvl + Ohm's law = Mesh Analysis

since kcl & kvl are ind. each other, the

nodal & mesh procedures are ind. to each
other.

The above techniques are valid only for the lumped electric circuits, [where kcl, kvl are valid] and that to at a constant temp. [where the ohm's law is valid].

→ The K-laws are ind. of the nature of the elements, where as ohm's is a function of the nature of elements.

the ohm's law is defined across an element that element can be lumped or distributed J= oE, where as the k-laws are applicable to only for the lumped electric circuits.

The ohm's law is not applicable for active elements like sources, since the v-I relation is non- linear and it is applicable to only for the linear passive elements like R, L, C. Nodal Analysis: - step1:-(t) 1) Se, L3 () vet) 2. Assign the node Ras voltages with reference to ground node, whose voltage always =0. 3. By using KCL first & ohm's next write nodal equations. At Node 2; $\begin{cases} v_2 > v_1 \\ v_2 > 0 \end{cases}$ $\begin{cases} c + i_L + i_{K_L} = 0 \end{cases} (B_y \ kcL)$ $c \cdot \frac{dv_2 - v_1}{dt} + \frac{1}{L} \int_{-\infty}^{t} v_2 dt + \frac{v_2 - v(t)}{K_2 + R_3} = 0$ (By ohm's) + + VE = 0 (+) - VE = 0 (+) - VE3 = 0 VES & R3 V2 - iR2 R2 - 18(t) - iR2 R3 = 0 $\Rightarrow vi_{R_{L}} = \frac{v_{L} - v(t)}{t_{L} + k_{L}}$ sandhine ic baro, 200-10, = Oni 2 sandh symi $v_1 = v_c + v_c \Rightarrow v_2 = v_1 + v_c \Rightarrow v_c = v_2 - v_1 ; \quad i_c = c \frac{dv_c}{dt} = c \frac{d}{dt} (v_c - v_1)$ At Node 1:- [1/2 /2] -i(t) + U1 + c. d (4-1/2) =0 Mesh -Analysis:-Steps:-1. Identity the no. of itt () { RI) meshes.

2. Assign mesh i's in clockwise 3. By using KYL first and ohm's law next write the mesh equations. Mesh 3:- (13>i2) - as approve of sides -VL - VRz - V(t) -VR3 = 0 manala $= \int_{-L}^{3\sqrt{i_3}} \int_{-L}^{4\sqrt{i_3}} \frac{1}{4t} (i_3 - i_2) - i_3 R_2 - v(t) - i_3 R_3 = 0$ Mesh 2:- $(i_2 > i_3)$ - L. $\frac{d}{dt}(i_2 - i_3) - R_1(i_2 - i_1) - \frac{t}{c}\int_{-\infty}^{t} dt = 0$ 123 (is into diffi Since the voltage across the ideal " House My any value, it is not possible to write the mesh eq. for mesh 1. KCL^{-1} $-i(+)+i_1=0$ $Equivalent circuits:- <math>i(+)=i_1$ -> when 2 elements are said to be in series only the i through them are same. -for 11el -> voltages are same. The impedances in series and admittances in Hel then we can add them. $Z_L = J\omega L \Lambda$; $Z_c = \frac{1}{J\omega c} \Lambda$ voltage division principle: V = 1 Zeq => 1 = Zeq ____ $V_1 = \frac{V. Z_1}{Z_1 + Z_2} ; V_2 = \frac{V. Z_2}{Z_1 + Z_2}$

when
$$Z = R$$
, when $Z = J\omega L$ when $Z = J\omega L$
 $V_1 = \frac{V R_1}{R_1 + R_2}$ $V_2 = \frac{V L_1}{L_1 + L_2}$ $V_3 = \frac{V C_2}{C_1 + C_2}$
 $V_2 = \frac{V R_2}{R_1 + R_2}$ $V_2 = \frac{V L_2}{L_1 + L_2}$ $V_2 = \frac{V C_1}{C_1 + C_2}$

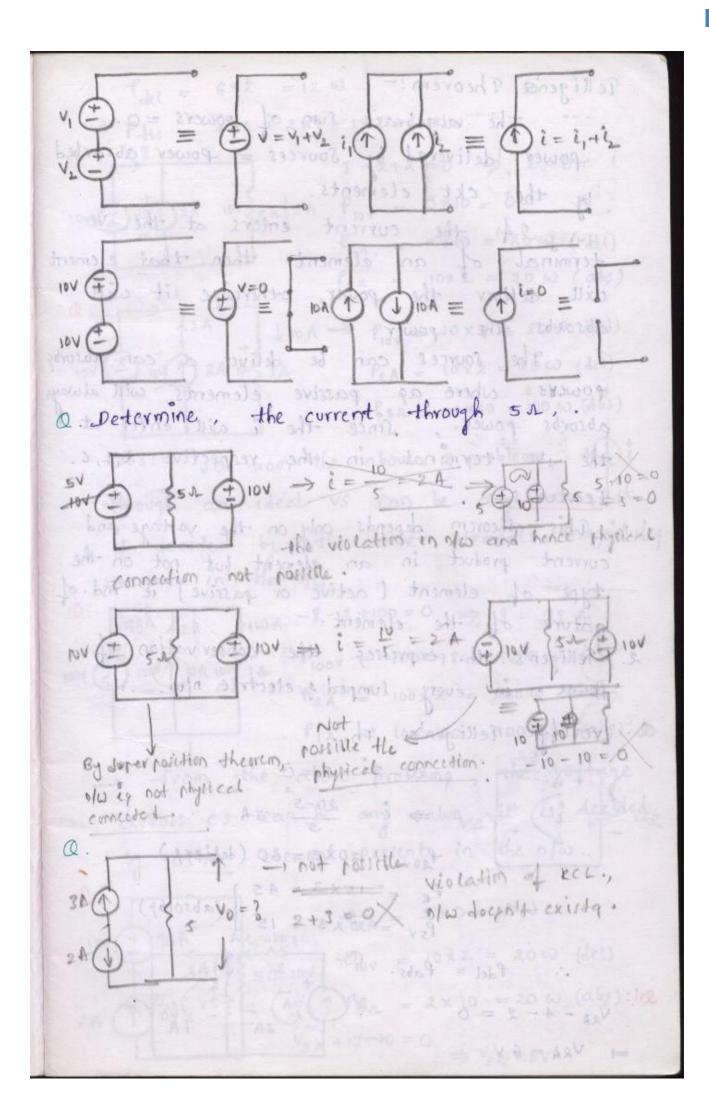
CURRENT Division:

 $V_1 = \frac{V R_1}{R_1 + R_2}$ $V_2 = \frac{V L_2}{L_1 + L_2}$ $V_3 = \frac{Z_1 \cdot Z_2}{Z_1 + Z_2}$

when $Z = R$, when $Z = J\omega L$ when $Z = \frac{Z_1 \cdot Z_2}{Z_1 + Z_2}$
 $V = \frac{R_1 \cdot R_2}{Z_1 + Z_2}$ $I_1 = \frac{R_1 \cdot L_2}{L_1 + L_2}$ $I_2 = \frac{R_1 \cdot C_2}{C_1 + C_2}$
 $I_1 = \frac{R_1 \cdot R_2}{R_1 + R_2}$ $I_2 = \frac{I \cdot L_2}{L_1 + L_2}$ $I_3 = \frac{R_1 \cdot C_2}{C_1 + C_2}$
 $I_4 = \frac{R_1 \cdot R_2}{R_1 + R_2}$ $I_4 = \frac{I \cdot L_2}{L_1 + L_2}$ $I_4 = \frac{R_1 \cdot C_2}{C_1 + C_2}$
 $I_4 = \frac{I \cdot R_1}{R_1 + R_2}$ $I_4 = \frac{I \cdot L_2}{L_1 + L_2}$ $I_4 = \frac{I \cdot C_2}{C_1 + C_2}$
 $I_4 = \frac{I \cdot R_1}{R_1 + R_2}$ $I_4 = \frac{I \cdot R_2}{R_1 + R_2}$ $I_4 = \frac{I \cdot R_2}{R_1 + R_2}$ $I_4 = \frac{I \cdot R_2}{R_1 + R_2}$
 $I_4 = \frac{I \cdot R_1}{R_1 + R_2}$ $I_4 = \frac{I \cdot R_2}{R_1 + R_2}$ $I_4 = \frac{I \cdot R_2}$

Equivalent circuits wiret source point of view: Here Ri +00, Since the violation 1 of KCL. A resistor in series with an ideal cs, is neglected in the analysis ie the load i ind of R. We can't omit this R, in power calculations, Since 22 R, is + 0. Here Ri + 0, Since the) {e, = (1) violation of kvl.

A resistoe in 11el with an ideal vs can be neglected in the analysis ie the load volt is ind. of R. . We can't omit thing R, in power calculations, since V2/R, #0. $-i_2+i_1=0 \Rightarrow i_1=i_2 \quad v_1-v_2=0 \Rightarrow v_1=v_2$ Two ideal as are south the connected in series only when their magnitudes are equal, otherwise the violation of kch, which results the unstability due to oscillations. Similarly 2 ideal vs are in 11th only when their magnitudes are equal, otherwise the violation of kul.



Telligena Theorem:

The algebraic sum of powers = 0.

power delivered by sources = power absorbed

by the ckt elements.

If the current enters at the -ve terminal of an element then that element will deliver the power, otherwise it will absorbs the power.

The sources can be deliver of can absorbs powers where as passive elements will always absorbs power. , since the i will enter at the tre terminal in the respective R, L, C.

features:-

1. This theorem depends only on the voltage and current product in an element but not on the type of element [active or passive] is ind. of nature of the element.

2. Telligen's the expresses the conservation of power in every lumped electric n/w.

a. verify Telligen's Th.

$$20V = \frac{20-5i-5=0}{5}$$

$$\Rightarrow i = \frac{20-5}{5} = 3A$$

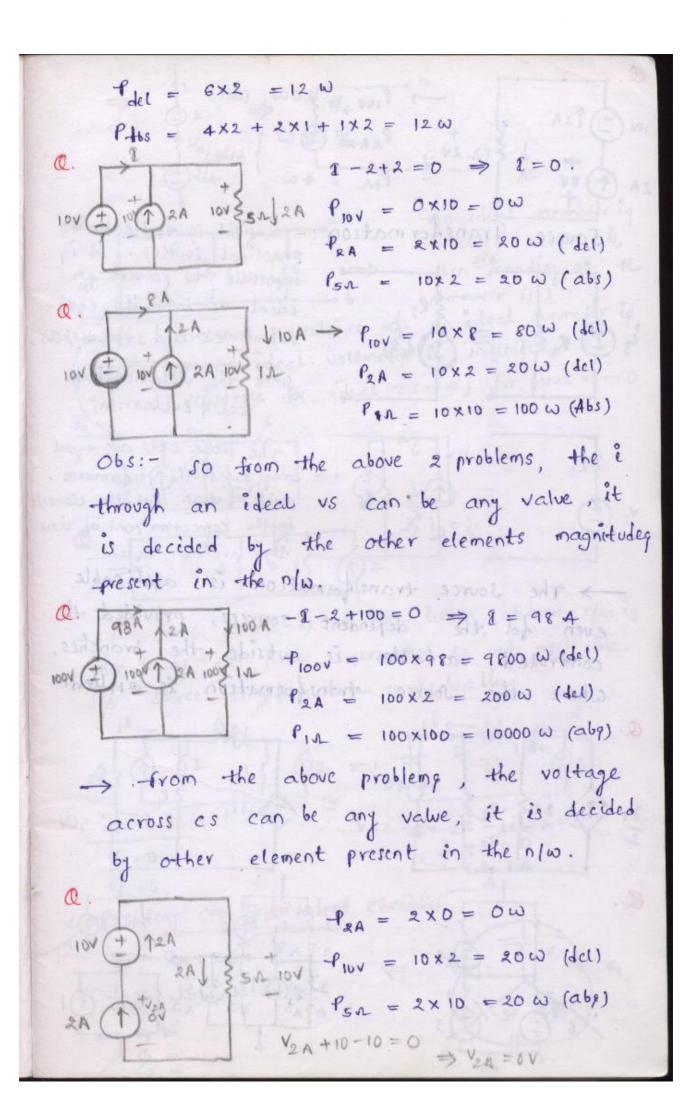
$$P_{20V} = 20\times3 = 60 \text{ (deliev}\text{p})$$

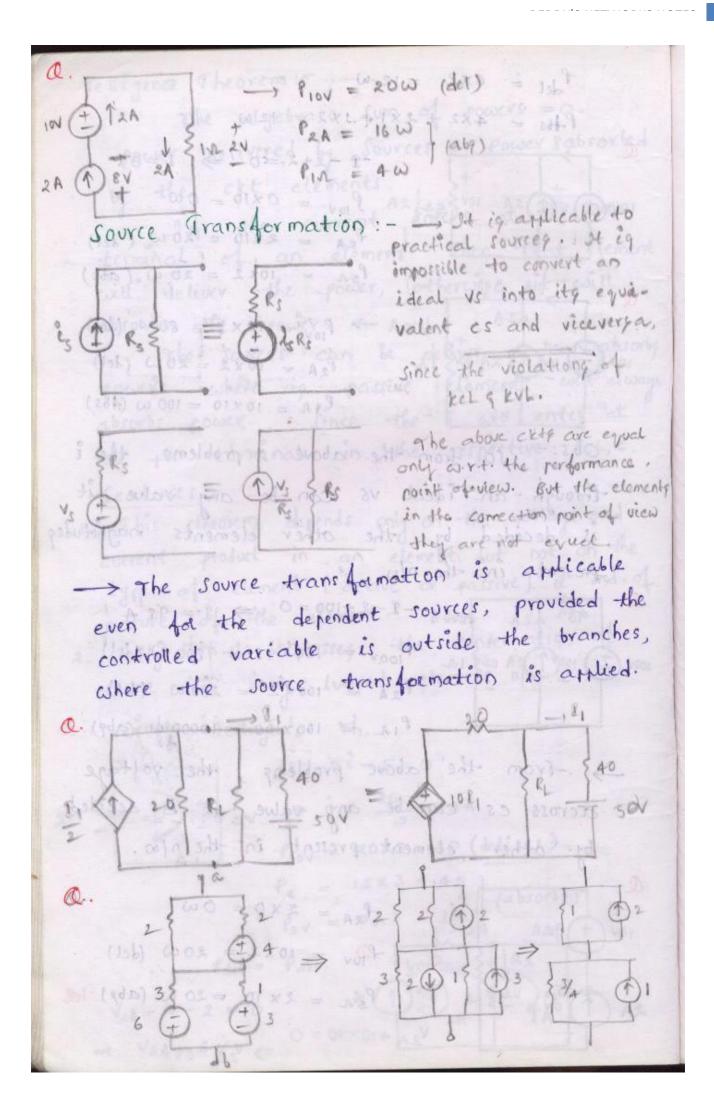
$$P_{R} = 15\times3 = 45 \text{ (absorbp)}$$

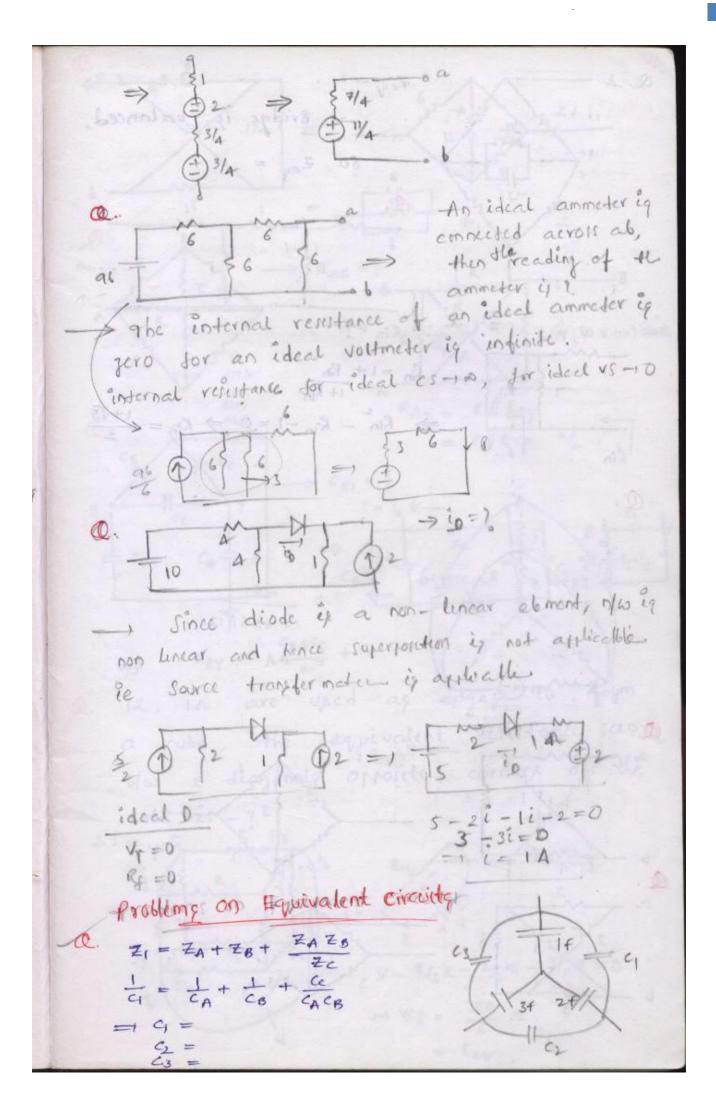
$$P_{SV} = 5\times3 = 15 \text{ (absorbp)}$$

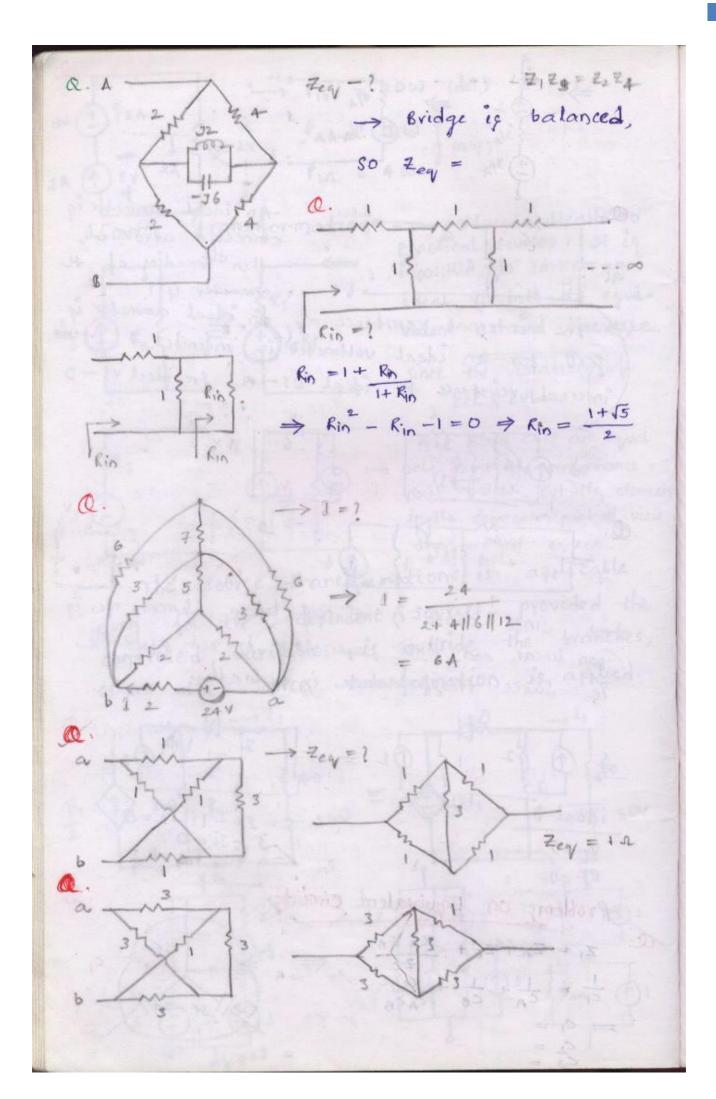
Sol: Van - 4 - 2 = 0

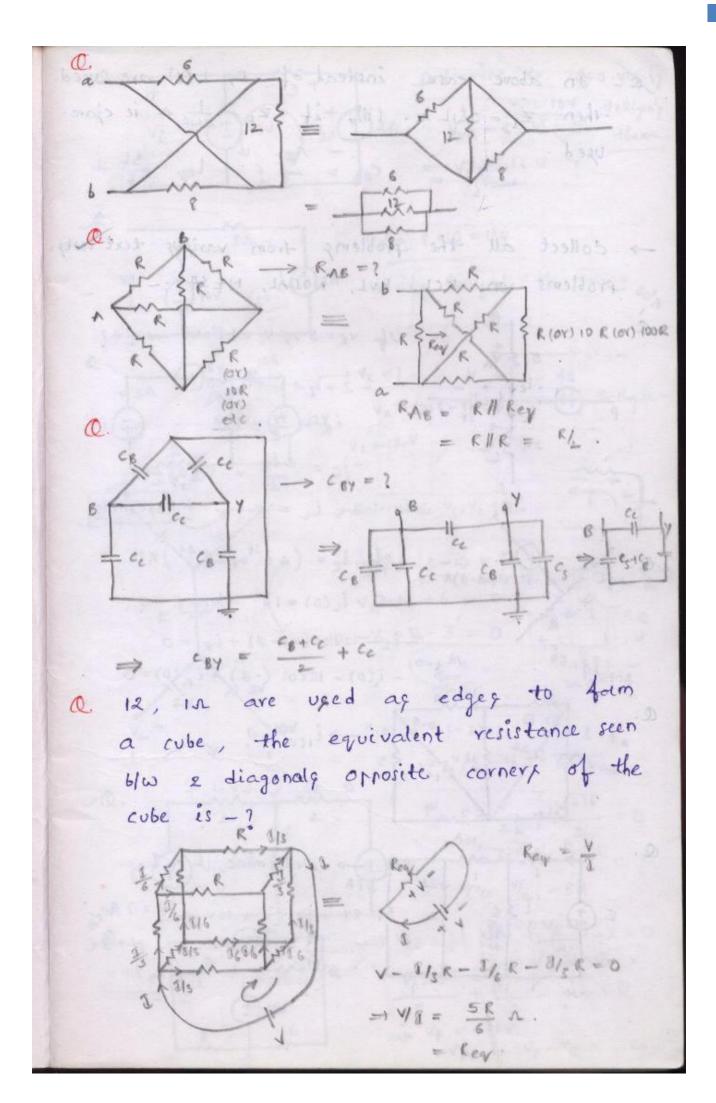
= VRA = 6 V

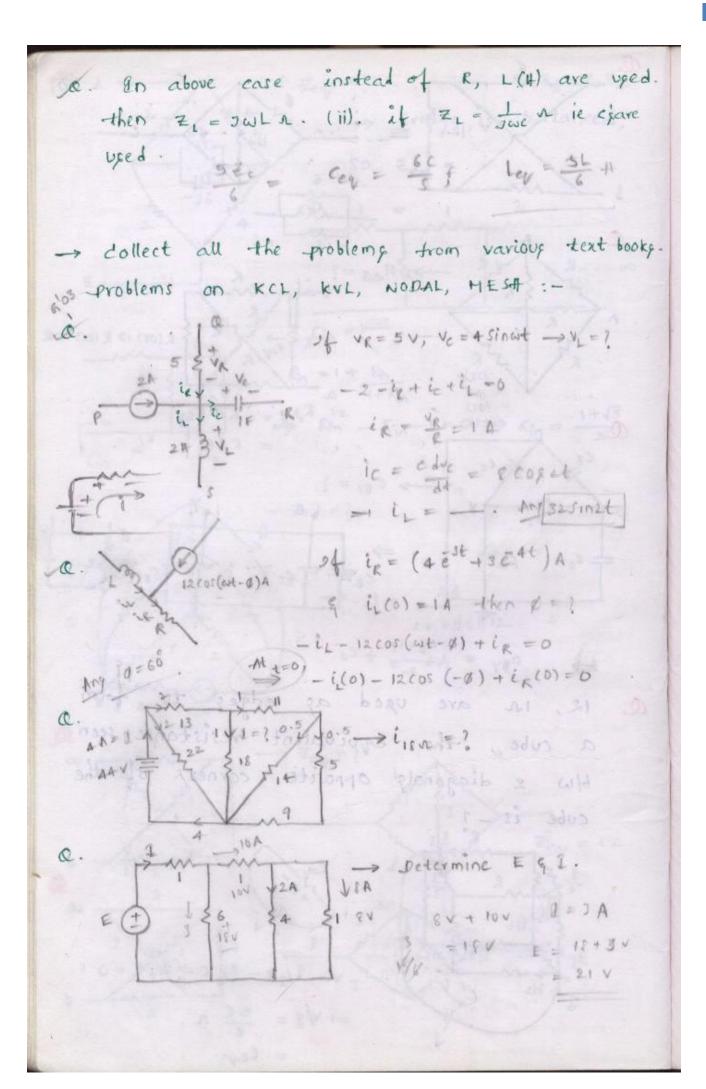


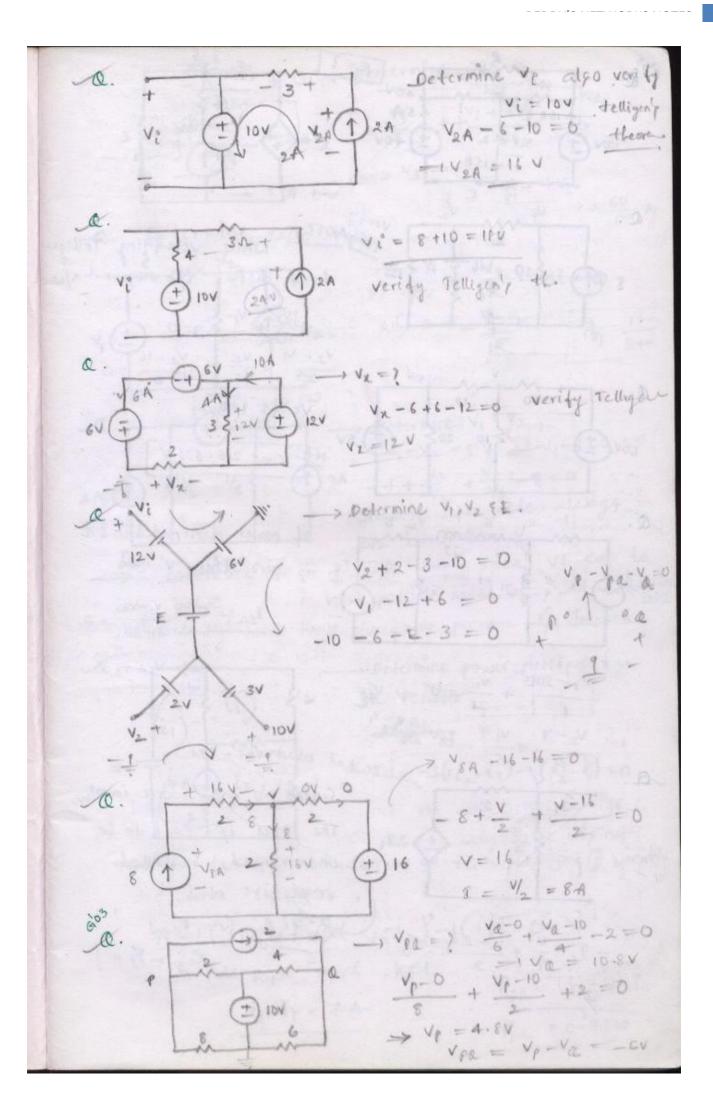


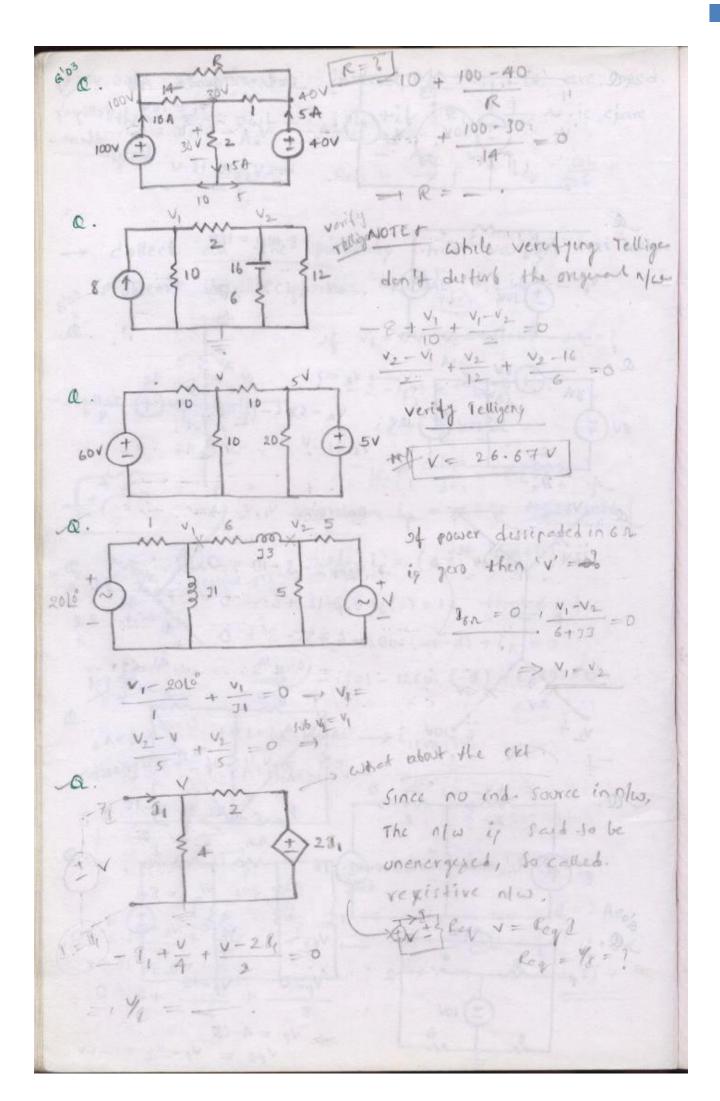


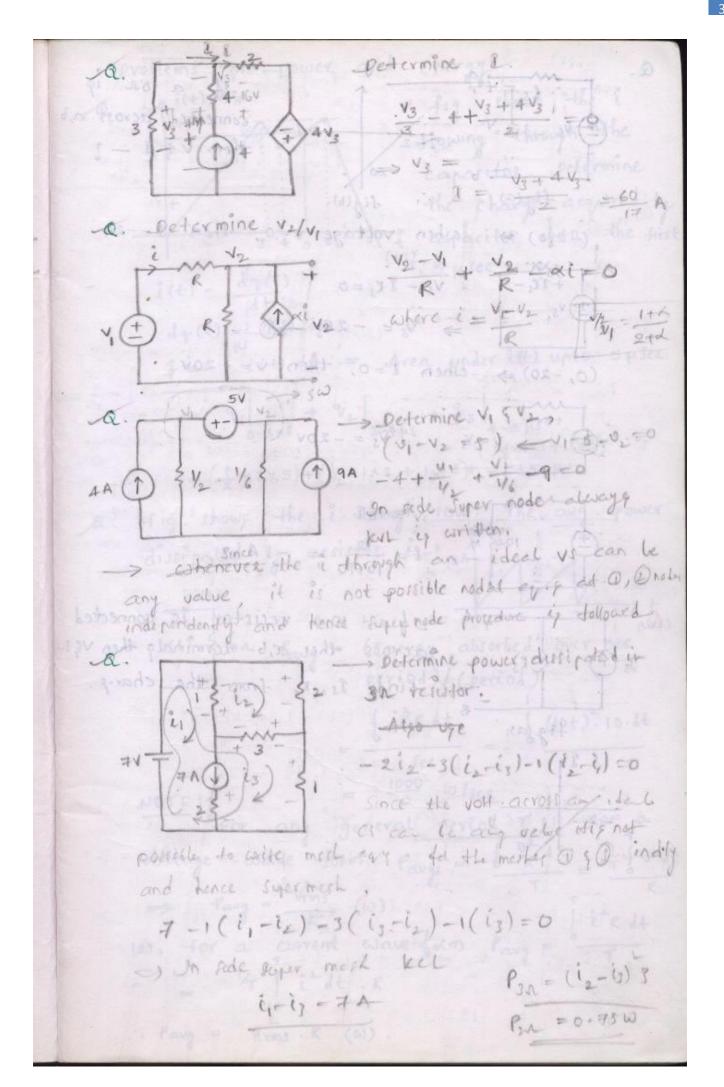


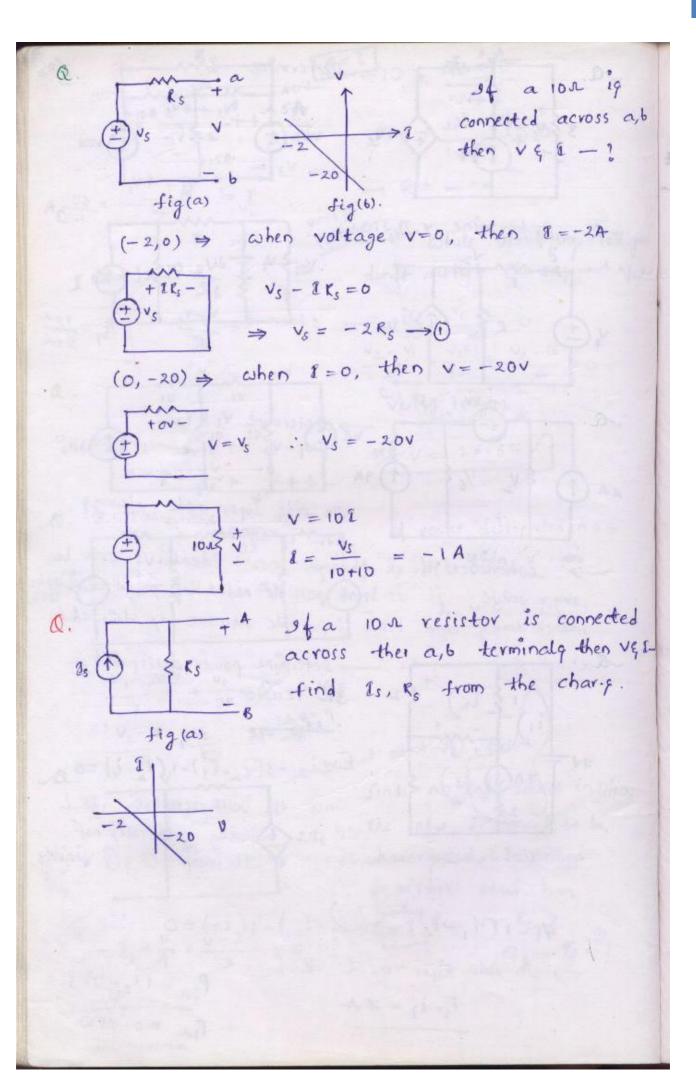


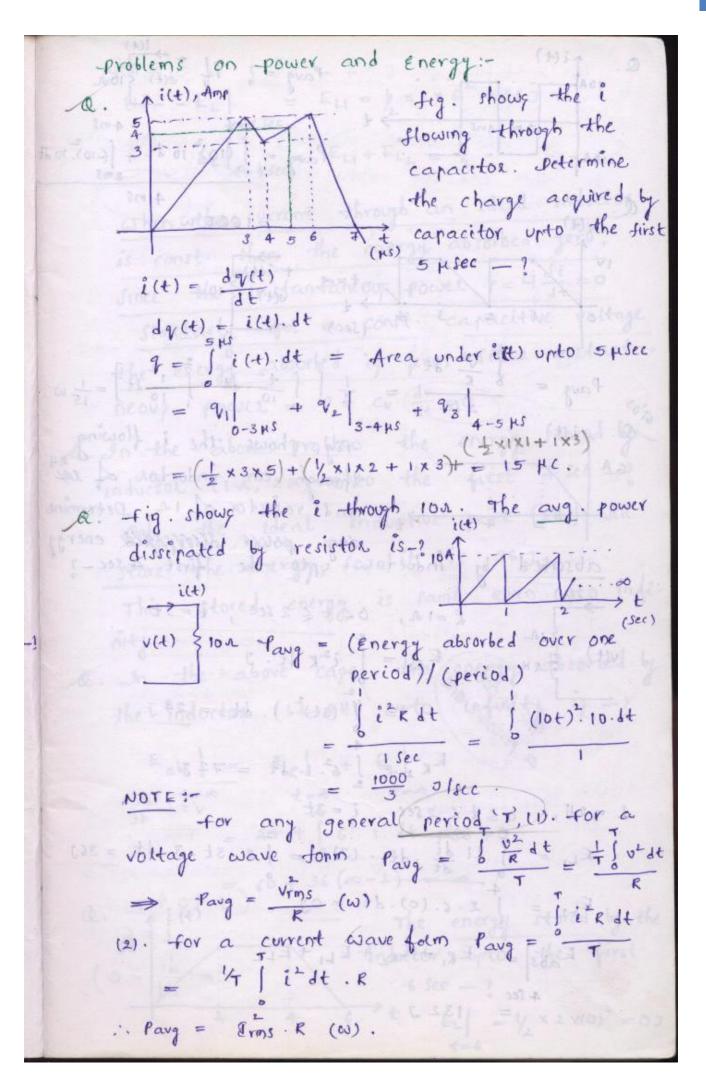


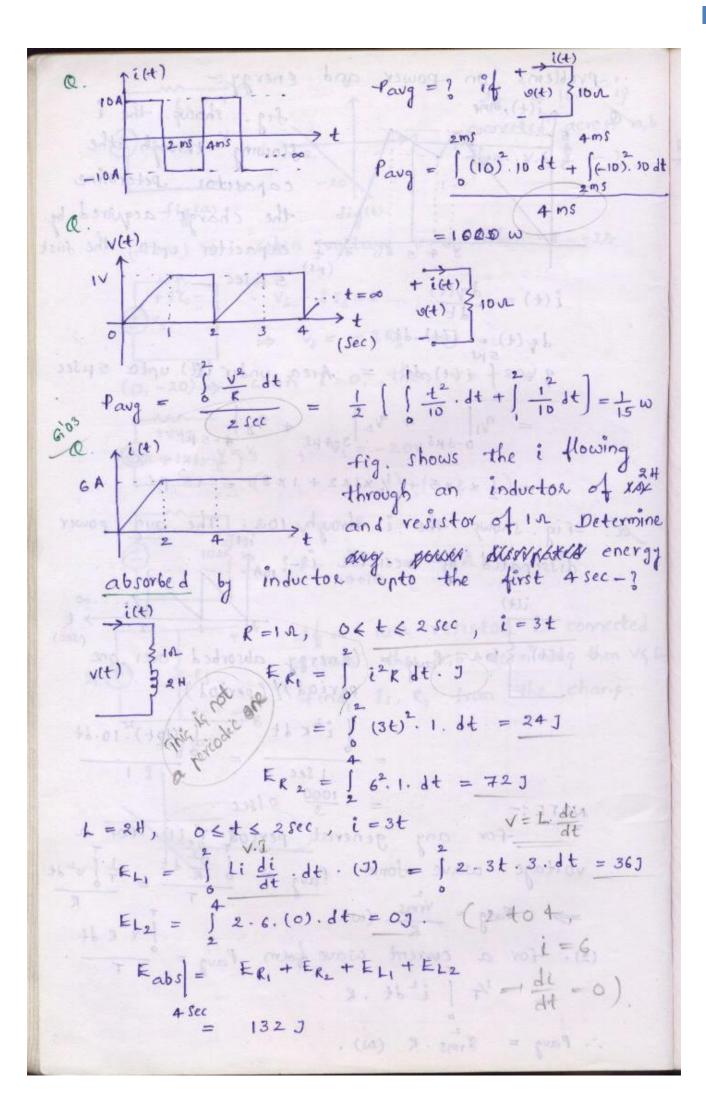












```
NOTE:-

(1) \cdot E_{L} = E_{H} = \frac{1}{2} \times 2 \times 6^{2} = 36

+=2 \sec c
EL | t=4sec = EL1 + EL2 = 1/2
when the current through an ideal inductor
is const. then the energy absorbed zero,
 Since the instantaneous power P = Li di =0
```

Similarly for a const. capacitive voltage the energy absorbed in zero, since instantaneoug power = $P = cv \cdot \frac{dv}{dt} = 0$.

a. In the above problem the energy stored by inductor (11, 24) upto the first 4 sec -? Only the ideal inductive part [24] will store the energy, so it is 36J.

This stored energy is same even upto infinity.

a. In the above cage the energy absorbed by the inductor (12,24) upto infinity is -?

$$|E_{abs}| = |E_{R}| + |E_{L}|$$

 $t = \infty$ $t = \infty$
 $= 24 + \int_{2}^{\infty} 6^{2} \cdot 1 \cdot dt + 36 + 0$
 $= 60 + 36 (\infty - 2) = \infty$

Q. 1 (t) 6-A

The energy stored by the inductor upto the first ·6 Sec - 7 6 t EL = 1/2 x 2 x(0) = 07

(OY)
$$E_{L}|_{J} = E_{L_1} + E_{L_2} + E_{L_3} = 36 + 0 - 36$$

stored $= 0$ J.

a. In the above problem, the energy absorbed by the inductor upto the first asec -?

$$|E_{abs}| = |E_{R_1} + |E_{R_2} + |E_{R_3} + |E_{L_1} + |E_{L_2} + |E_{L_3}|$$

 $|E_{abs}| = |E_{R_1} + |E_{R_2} + |E_{R_3} + |E_{L_1} + |E_{L_2} + |E_{L_3}|$
 $|E_{abs}| = |24 + |72 + |24 + |36 + 0| - |36|$

$$E_{g_3} = \int_{4}^{6} i^2 R dt = \int_{4}^{6} [-3(t-6)]^2 \cdot 1 dt = 24 J.$$

v(t) {11 = 2f

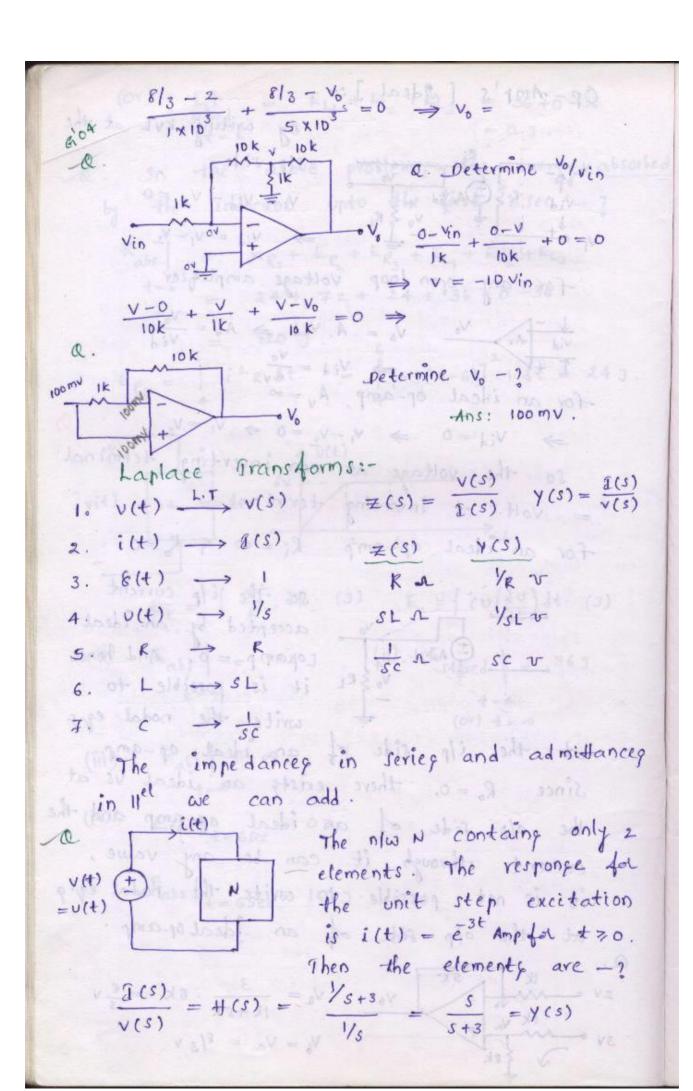
$$E_{R} = \int \frac{v^{2}}{R} dt \cdot (3) \qquad E_{c} = \int cv \left(\frac{dv}{dt}\right) dt \cdot (3)$$

(i).
$$E_{abs} = 132 J$$
 (ii). $E_{stored} = 36 J$
 $t=4$ $t=4$ (or) $t=\infty$

(iii).
$$\exists abs \mid = \infty$$
 7 $t=\infty$

CO- (O) x x y = 132 - 3 + 3 +

Op-Amr's [Ideal] :-By writing KVL at the ilp side, $\frac{V_0}{V_0} = V_1 - V_2 = 0$ $\frac{V_0}{V_0} = V_1 - V_2$ for any open loop voltage amplifier $\frac{1}{v_{id}} \frac{1}{Av} \frac{v_o}{v_i} = A. \quad v_{id} \Rightarrow Av = \frac{v_o}{v_{id}}$ -for an ideal op-amp, $A_v = \infty$ \Rightarrow $V_1 = 0 \Rightarrow V_1 - V_2 = 0 \Rightarrow V_1 = V_2$ so the voltage at non-inverting terminal = volt. at inverting terminal. for an ideal op-amp Ri = 00 q R =0. so the ilp current DAVVID TO accepted by an ideal opamp = 0. And hence vo ski it is possible to write the nodal eggs at the ilp side of an ideal op-amp. Since Ro = 0, there exists an ideal vs at the old side of an ideal op-amp and the current through it can be any value, it is not possible to write the nodal egg at the olp side of an ideal or-amp. $V_0 = \frac{3}{1k+8k} \cdot \delta k = \frac{8}{3} V$ V1 = Va = 8/3 V



a. The driving point impedance fun. of a 1- port n/ω is $\pm (s) = \frac{2s}{s^2+3}$. The realifation is =? $Z(S) = \frac{2S}{S^2 + 3} = \frac{1}{\frac{S}{2} + \frac{3}{2S}} = \frac{1}{y(S)}$ $Y(s) = s \cdot \frac{1}{2} + \frac{1}{5 \cdot 2} = sc + \frac{1}{5L}$ a she circuit (1972) (1972) ₹(5) ½+ 3 2/3 H Q. $y(s) = \frac{2s}{s^2 + 3}$ $\frac{5}{2} + \frac{3}{2}s = \frac{1}{2}s \qquad \text{gamiy} \qquad \frac{1}{3}f$ $Z(S) = S \cdot \frac{1}{2} + \frac{1}{5 \cdot \frac{2}{3}}$ NOTE: = SL + sc 1. For the driving point LC impedance fein., the poles and zeros are alternate, lies only on the Iw axis and both the numerator and denominator polynomial decrease most be default by one. entraliance (or) admid ance No. of inductors = 2, no. of capacitors = 2 Realize the above fun. f1, f2 & c1, 6. for the driving point RL fun. the Pq = are afternate and lies only on the -ve real axis and nearest to the origin is the zero.

[zero can be at the origin]

Eg: Realize the $Z(s) = \frac{(S+1)(S+4)}{(S+2)(S+6)}$ by

Ff 8, Ff-8, C-8, C-8.

are alternate, lies only on -ve real axig and nearest to the origin is the pole.

[pole can be at the origin].

 $eg:= Z(S) = \frac{(S+2)(S+6)}{(S+1)(S+4)}$

a. Realize the above fun.

no. of resistors = 3.

for the driving point RLC impedance fun.

the Pqz's are complex conjugate and they

are symmetric w.r.t. the -ve real axig.

NOTE:- In the above cases instead of impedance dun. of impedance dun. are given, then they are converted into impedance fun. of and above test can be performed.

- -> All RL imp. fun = RC adm. fun. and viceversa.
- -> Immittance = impedance (or) admittance

Realize the above that the first averfor the driving point st fund. the (c) spec are
afternote and lies only on the -ve real axis

No. of inductors = 1, 10, of repositors = 1

and neavest to the origin is the pero-

Filters:-

$$Z_L = J\omega L \quad \Delta = 0, \Rightarrow Z_L = 0 \Rightarrow L \rightarrow 8C$$
 $Z_C = 0 \Rightarrow C \rightarrow 0C$
 $Z_C = 0 \Rightarrow C$

APF > December of the control of several is +

Q. The max. phase shift added by Arf to the ilp signal is -?

(a)
$$0^{\circ}$$
 (b) 40° (c) -40° (d) $\pm 180^{\circ}$

H (s) = $\frac{1-s}{1+s}$

H (3ω) = $\frac{1-3\omega}{1+3\omega}$

$$|\#(\varpi)| = 1$$

$$L_{+}(\sigma\omega) = \phi = -\tan^{2}\omega - \tan^{2}\omega$$

$$= -2 \tan^{2}\omega$$

$$\omega = 0 \implies \phi = 0 = \phi \sin \theta = 0$$

$$\omega = \infty \Rightarrow \phi = -180 = 180 = \pm 180 = \phi_{\text{max}}$$

a. The max. ph. shift added by the 8 order LPF to the il signal is _?

$$+ \frac{V_0(s)}{R} + \frac{V_0(s)}{V_1(s)} = \frac{1}{1 + s c R}$$

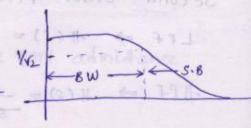
$$V_0(s) = \frac{1}{1 + 3 \omega R C}$$

$$4 (3\omega) = \frac{1}{1+3} \frac{1}{$$

$$|+(\omega)| = \frac{1}{\sqrt{1+(f/f_L)^2}}$$

$$|+(\omega)| = \phi = -\tan^{-1}f/f_L$$

$$|+(\omega)| = \phi = -\tan^{-1}f/f_L$$



Q. The max. ph. shift added by 2 order HPF to the isp signal is -?

$$\frac{V_0(s)}{V_1(s)} = H(s) = \frac{SCR}{1 + SCR}$$

$$H(D\omega) = \frac{1}{1 + \frac{1}{J\omega CR}}$$

$$H(J\omega) = \frac{1}{1-J+1/4}$$
 where $f_H = \frac{1}{2\pi RC}$

$$\frac{1}{\int 1+(f_{1})^{2}}; \quad \frac{1}{\int 1+(f_{1})^{2}}; \quad \frac{1}{\int 1+(f_{1})^{2}} = 0 = 1$$

$$f = f_{1} \implies 0 = 45^{\circ} = 4 \text{ max}$$

Transients:



presence of the energy storing elements called inductor and the capacitor. Since the energy stored in a memory element cannot change instantaneously (within zero time], the Lic elements will oppose the sudden changes in the system, which results the unstability in the Nw due to the oscillations.

If the next now consists of only resistors then no transients will results

in the system at the time of switching, the resistor can accommodate any amount of V & 1.

The transcent effects are more seviere in DC ag compare with AC and the transient free time is possible only for AC.

1. The behaviour of LEC at t=0+ and ag + + -> 00 :- 11

 $Z_L = SLA$, $t = 0 \Rightarrow S = \infty \Rightarrow Z_L = \infty \Rightarrow L \rightarrow 0.C$.

 $Z_c = 0 \Rightarrow c \rightarrow s.c$

1→0 →5 →0 → ZL=0 → L→S.C

Zc=x=) C-O.C.

-> A long time after the switching is nothing but the ss. on ss, the inductor behaviour ig s.c. be haviour and the capacitor be haviour is o.c.

Steady state: whenever the ind. source is connected to the n/w tota long time ideally infinite amount of time, practically upto 5 time constants] then the now is said to be in the ss. In ss the energy stored in memory elements is max and constant. ie 1/2 Li' = max & const.

=> iL = max & const.

since $V_L = L \cdot \frac{di_L}{dt} \Rightarrow V_L = 0 \Rightarrow L \rightarrow S.c.$ Similarly 1/2 cy2 = max & const

```
→ Vc = max & const.
      Since i_c = c \cdot \frac{dv_c}{14} \Rightarrow i_c = 0 \Rightarrow c \rightarrow o.c.
      The inductor i and capacitor volt at t=0
and at t=0^+ instants.

L:- i_L(t) = \frac{1}{L} \int v_L(t) dt
                = + \int_{-\infty}^{-\infty} v_{L}(t) dt + \int_{-\infty}^{+\infty} \frac{1}{t} v_{L} dt
                = iL(0) +// VL(t) dt.
         :. i(0^{+}) = i(5) + \frac{1}{5} \int_{0}^{0^{+}} v_{1}(t) dt
          \Rightarrow i_L(0^+) = i_L(5)
        = \sum_{k} (o^{\dagger}) = E_{k}(\delta)
      -> so, the inductor i cannot change instantaneously ie for all the practical
      existing ilps. similarly the energy.
94 VL(t) = 8(t) then ...
     i_L(0^+) = i_L(0) + \frac{1}{L} \int_{-8}^{0} 8(+).4+
         \hat{\iota}_{L}(o^{\dagger}) = \hat{\iota}_{L}(\delta) + \gamma_{L}
        \Rightarrow E_{L}(o^{\dagger}) \neq E_{L}(o^{\dagger})
\forall_{L}(t) = e(t) = 0 \text{ for } -\infty \leq t < \overline{0} \qquad -\infty \qquad \delta
     So i_L(\delta) = \frac{1}{L} \int_{-\infty}^{\delta} V_L(t) dt = 0.4
         \Rightarrow i_{\perp}(0^{+}) = \frac{1}{2}
             SO EL (0) = 07
   EL (ot) = 1/2 L (1/2) = - (1)
     C:= V_c(t) = \frac{1}{c} \int_{-c}^{\infty} V_c(t) dt
                       = V_c(\delta) + \frac{1}{c} \int_{-\infty}^{\infty} i_c(t) dt
```

At
$$t = 0^{t}$$
 $v_{c}(0^{t}) = v_{c}(0) + \frac{1}{c} \int_{0}^{t} i_{c}(dt) dt$
 $\Rightarrow v_{c}(0^{t}) = v_{c}(0)$
 $\Rightarrow v_{c}(0^{t}) = v_{c}(0) + \frac{1}{c} \int_{0}^{0} \delta(t)$
 $\Rightarrow v_{c}(0^{t}) = v_{c}(0)$
 $\Rightarrow v_{c}(0^{t}) = v_{c}(0^{t}) = v_{c}(0)$
 $\Rightarrow v_{c}(0^{t}) = v_{c}(0^{t}) = v_{c}(0^{t})$
 $\Rightarrow v_{c}(0^{t}) = v_{c}(0^{t}) =$

In all the Source free ckts, the Land c will looses their energies to resistors as a feen of time, hence the energy in the ss is always =0.

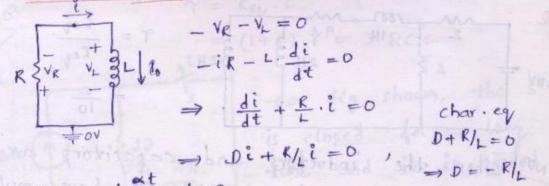
2. With sources initial [t=ot] and final [t+0]

Enstants conditions :-At these 2 instants, Land e elements will looses their regneticance and hence the nature of the ckt ig resistive.

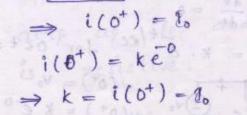
3. with sources the laplace transform approch of solving the transient problems for t>0, t≤0.

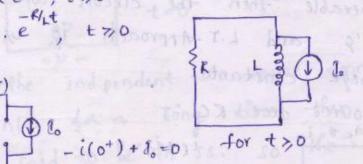
Source free circuits:-

1. Source free KL circuit :-

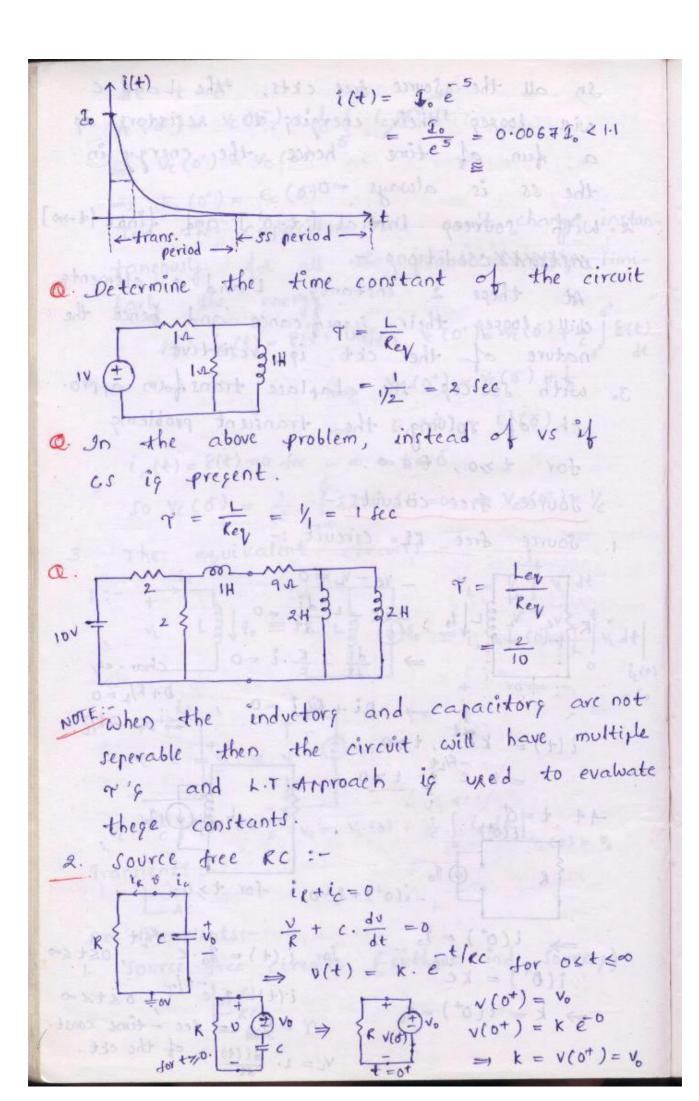


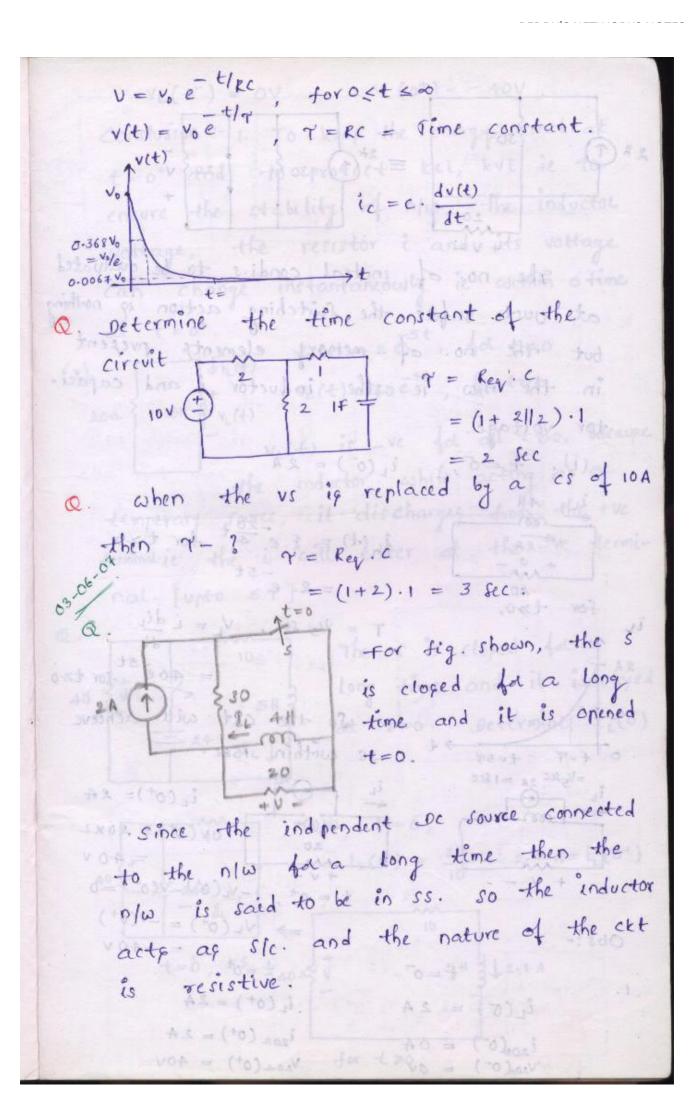
i(t) = tet, t>0 stanlars of = k, e , t > 0 or 1

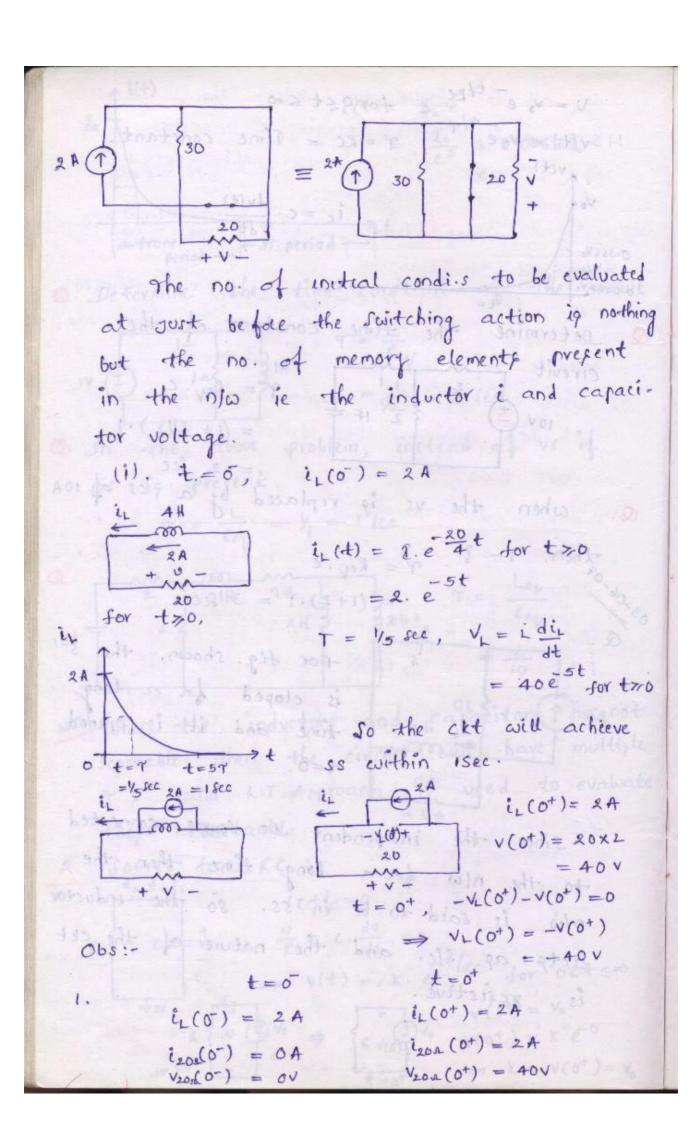




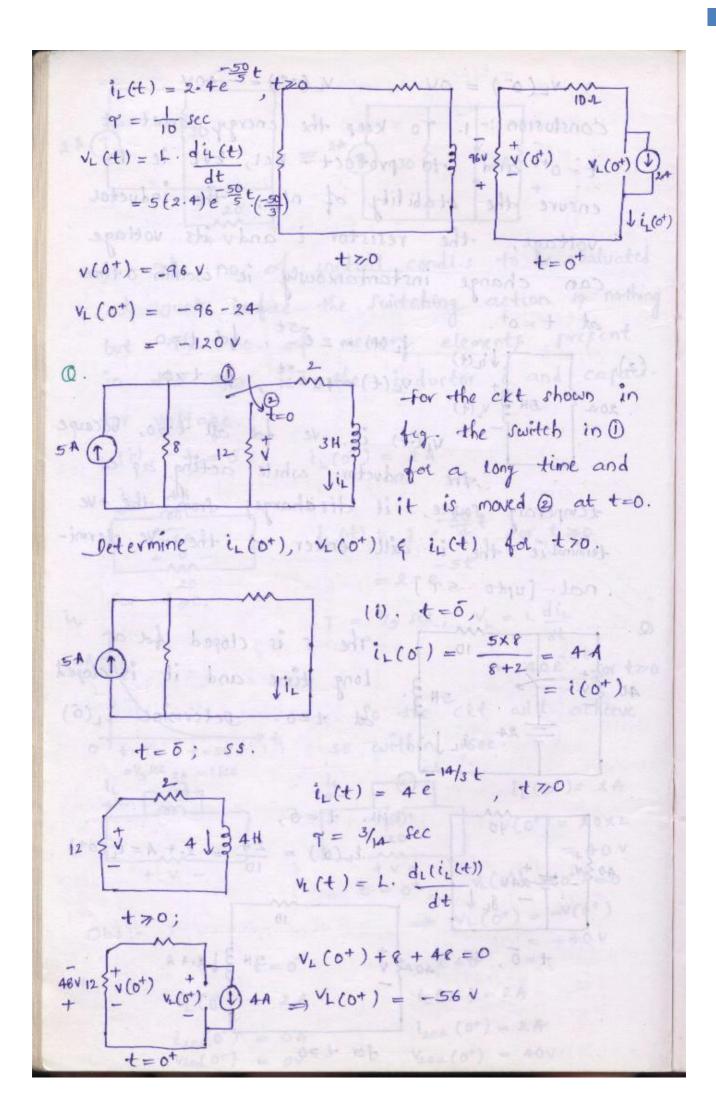
So
$$i(t) = g_0 \cdot e^{-R/Lt}$$
, $0 \le t \le \infty$
 $i(t) = g_0 \stackrel{-}{e}^{-t/T}$, $0 \le t \le \infty$
 $\gamma = \frac{1}{R} = sec = time const.$
 $V_L = L. \frac{di(t)}{dt}$ of the ckt.

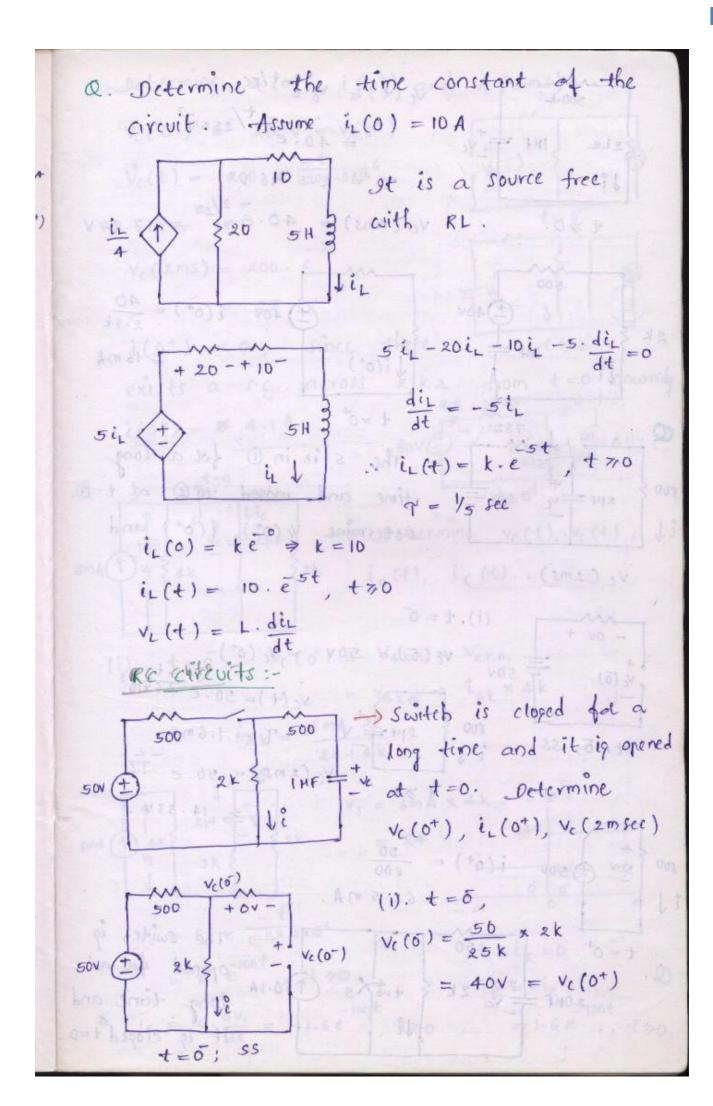


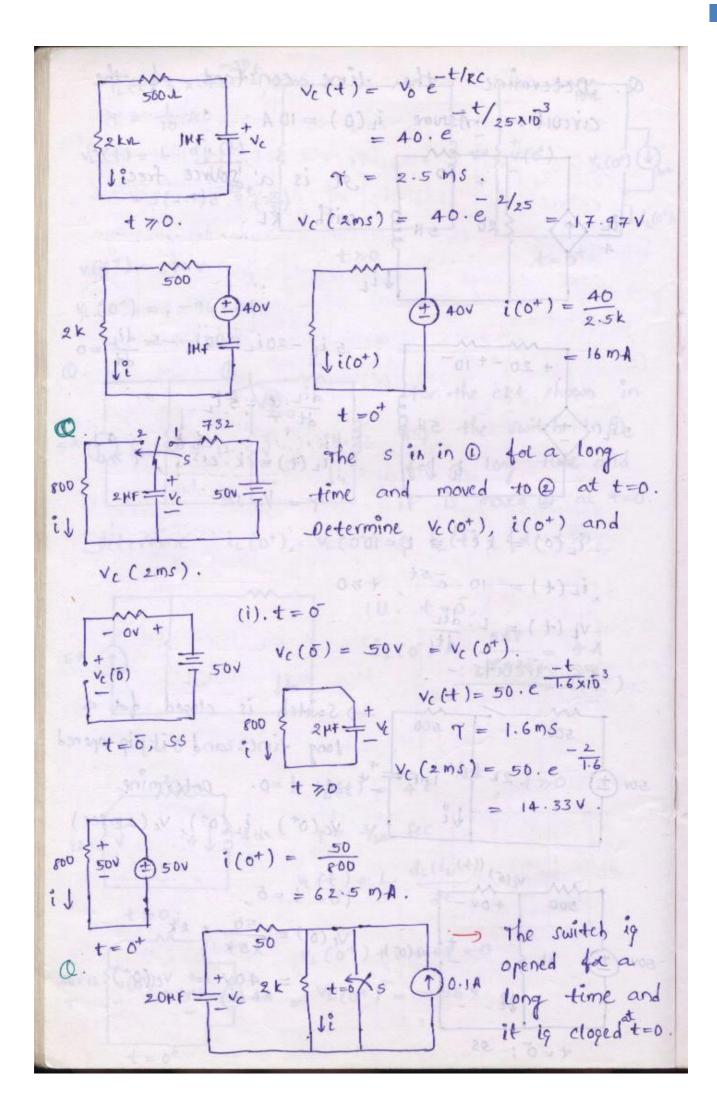


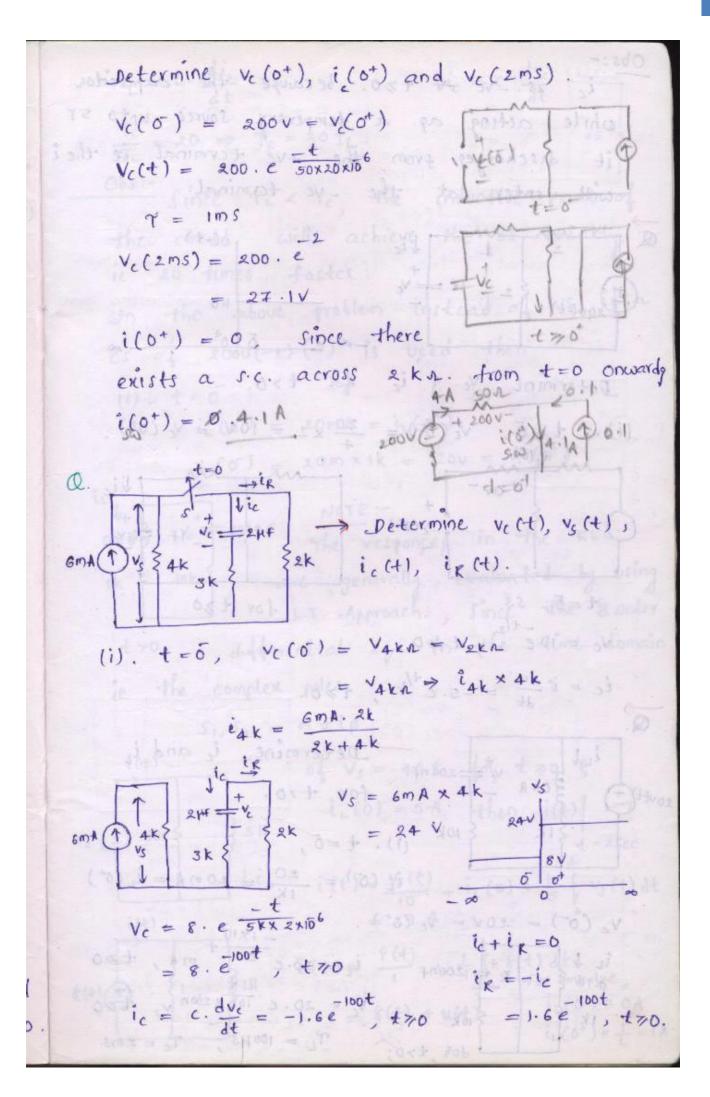


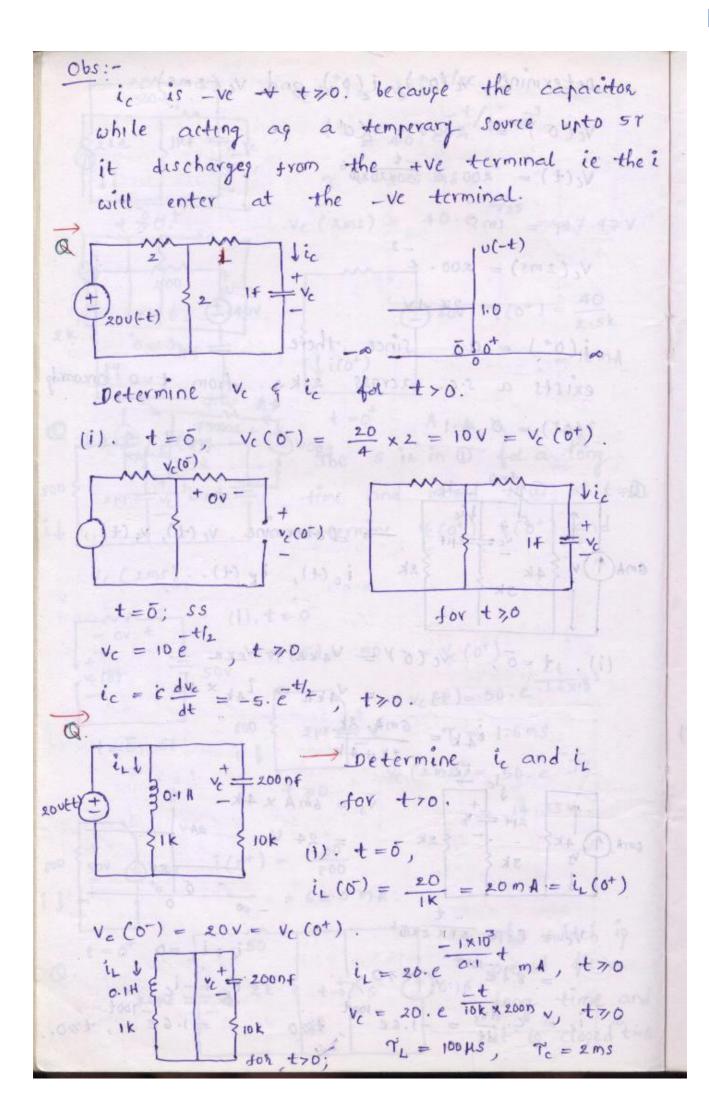
 $V_{L}(0^{-}) = 0V$ $V_{L}(0^{+}) = -40V$ Conslusion: - 1. To keep the energy const at t=o+ and to protect kcl, kvl ie to ensure the stability of nlw, the inductor voltage, the resistor i and its voltage can change instantaneously ie within o time JiL(+) iL(+) = 2 e + , fol + 70 at $t = 0^{\dagger}$. 5H 3 VL(t) =40 = 5t, for the Vi(+) is -ve for all +70, because the inductor while acting as a temperary source, it discharges from the +ve terminatie the i will enter at the -ve terminal. [upto 57] 10 The s is cloped tota 5H3. long time and it is closed at t=0. Determine $i_{L}(\bar{0})$ 50 (1) ON 1. 3 W(5) () 4A () ((6)) for t 70









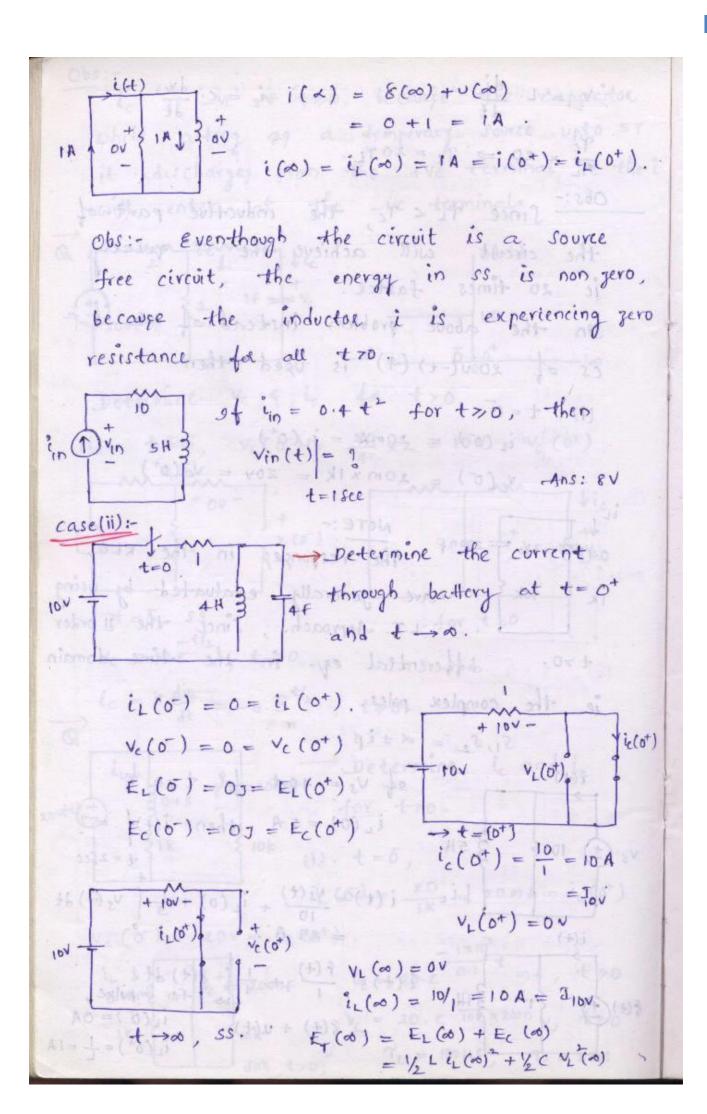


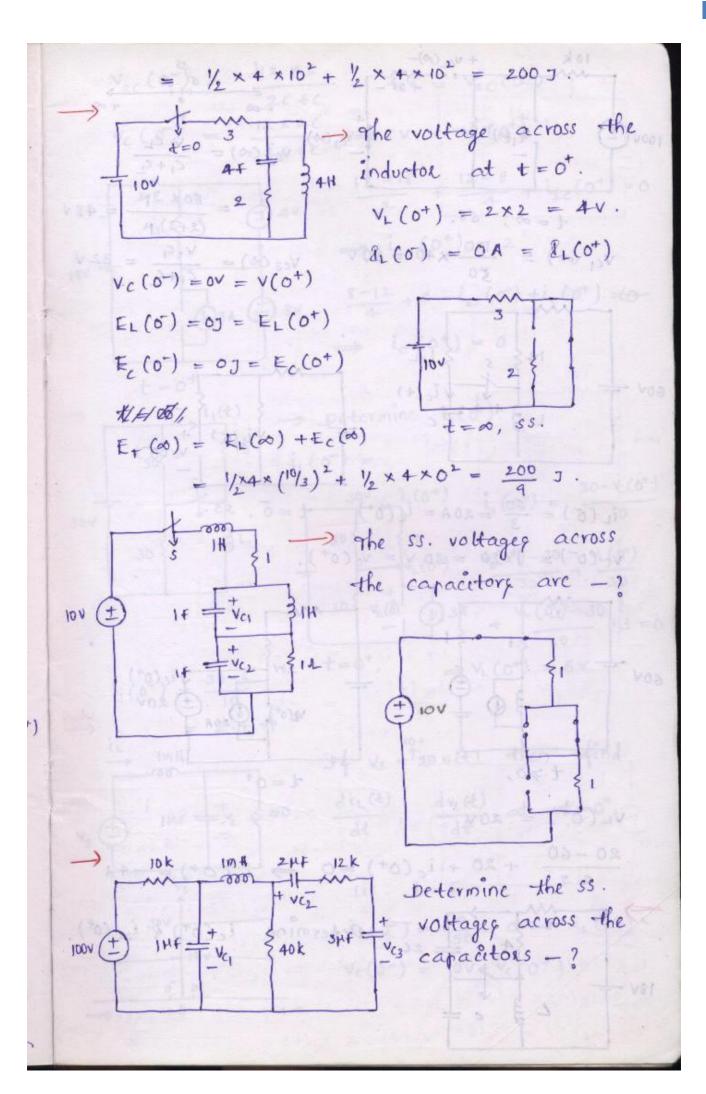
$$V_{L} = L \cdot \frac{di_{L}}{dt}$$

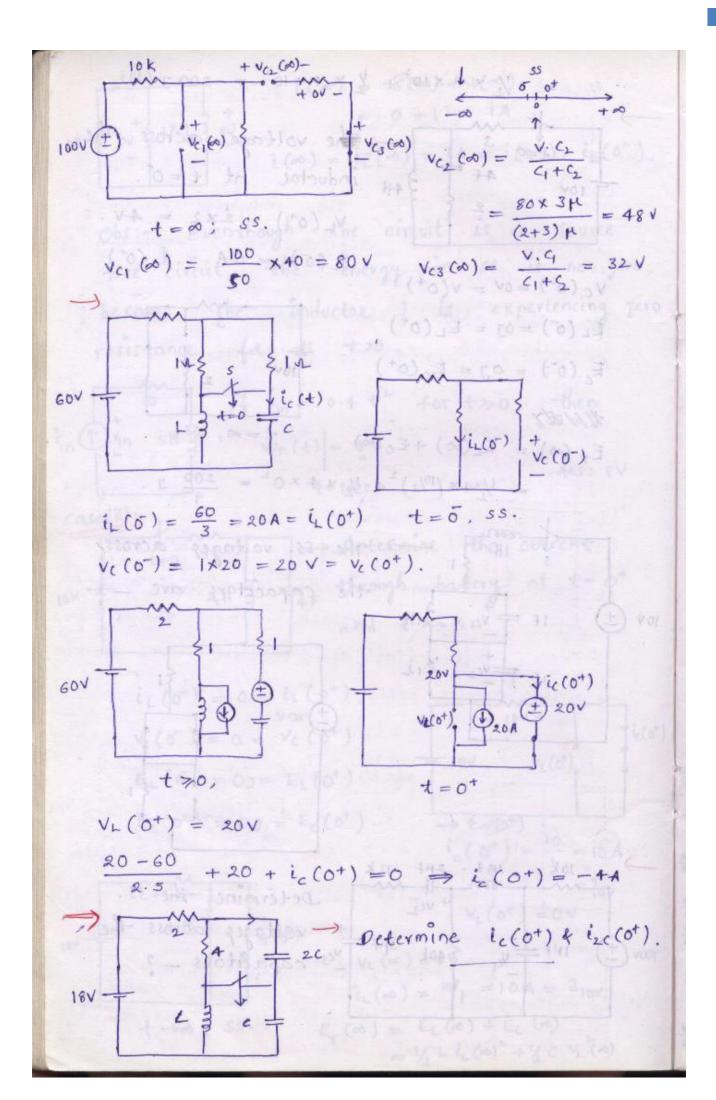
$$\frac{\gamma_{C}}{\eta_{L}} = 20 \Rightarrow \gamma_{C} = 20 \gamma_{L}.$$

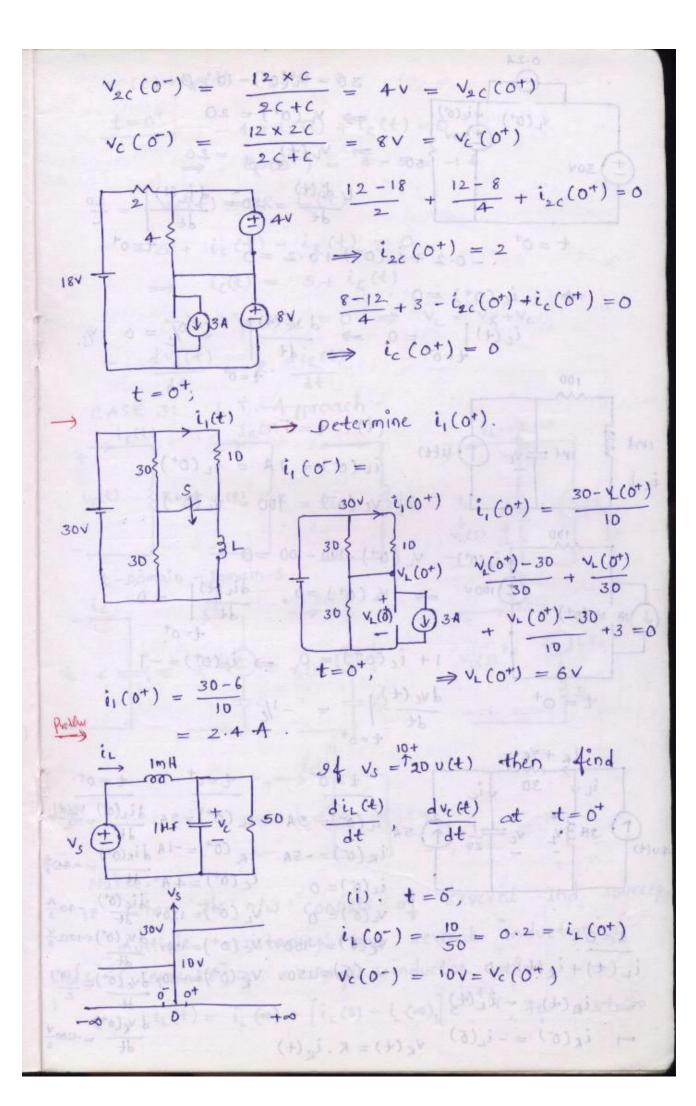
$$\frac{\gamma_{C}}{\eta_{C}} = 20 \Rightarrow \gamma_{C} = 20 \gamma_{C}.$$

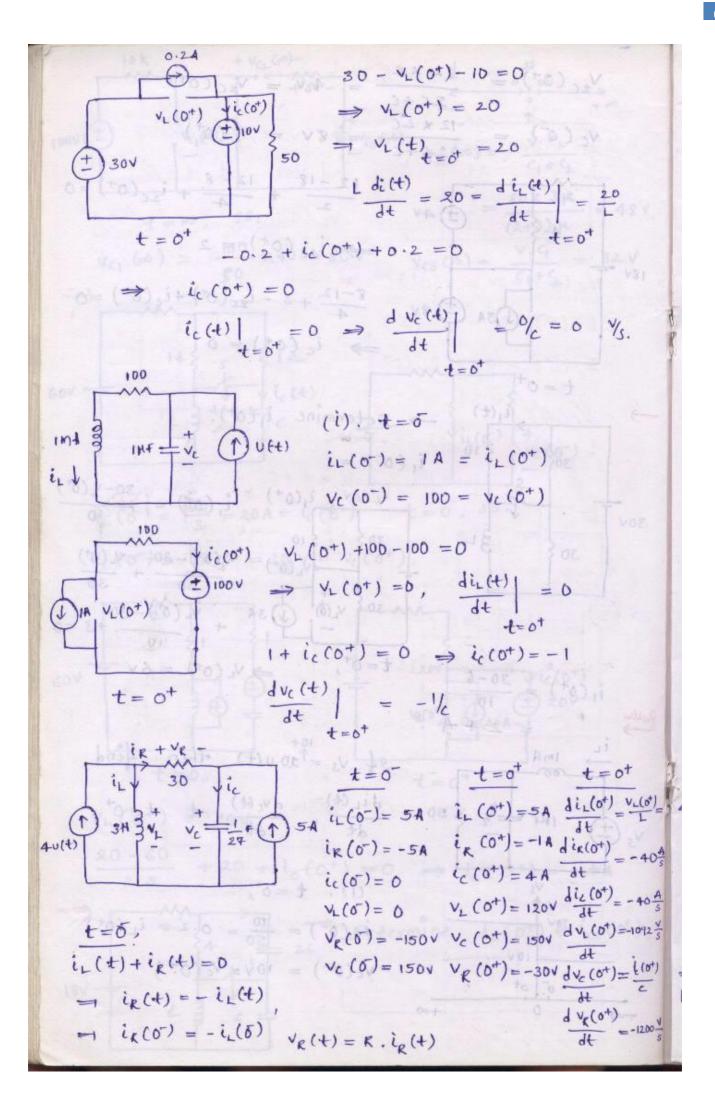
$$\frac{\gamma_{C}}{\eta_{C}} = 20 \Rightarrow \gamma_{C} = 20$$

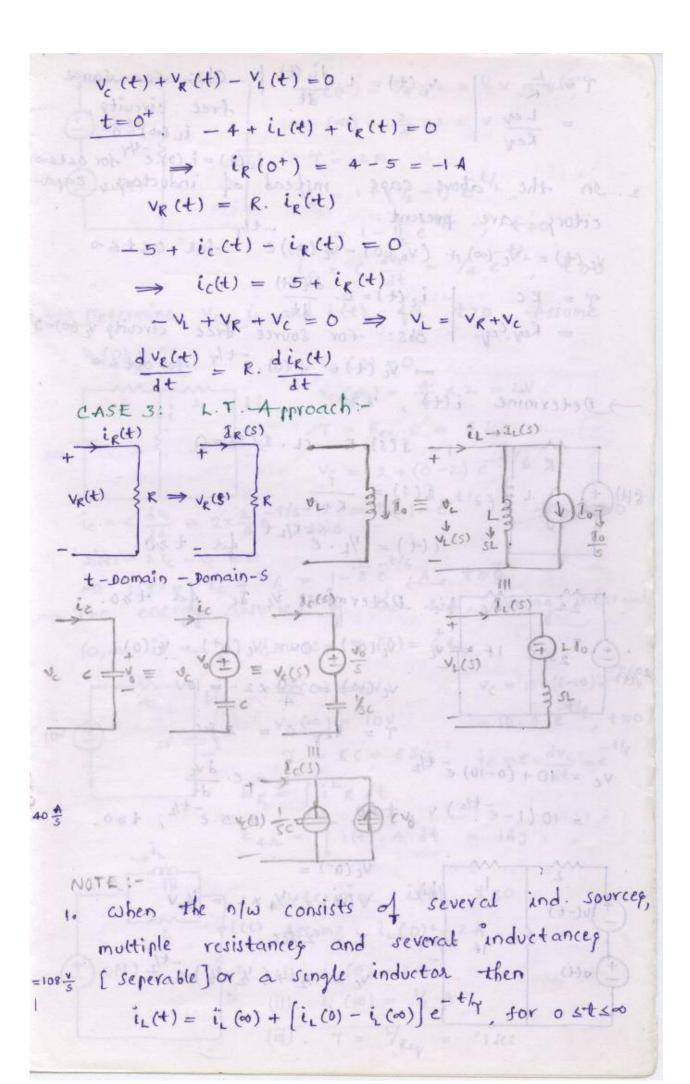












$$T = \frac{L}{R}$$

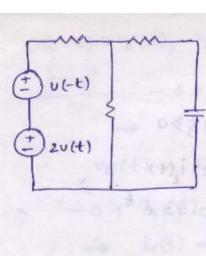
$$= \frac{L \cdot \omega_{1}}{R \cdot \omega_{2}}$$

$$= \frac{L \cdot \omega_{2}}{R \cdot \omega_{2}}$$

$$= \frac{L \cdot \omega_{1}}{R \cdot \omega_{2}}$$

$$= \frac{L \cdot \omega_{2}}{R \cdot \omega_{2}}$$

$$= \frac{L \cdot \omega_{2}}$$



$$v_{c}(0^{-}) = \frac{1}{4} \times 2 = \frac{1}{2} \vee =$$

-) Determine Ve, ic and i(t) for tro. Assume

$$V_{c}(0) = 0V$$

$$V_{c}(0) = V_{c}(0)$$

$$V_{c}(0) = 0$$

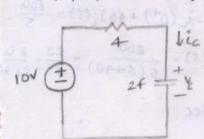
$$V_{c}(0) = 0$$

$$V_{c}(\infty) = \frac{4}{4} \times 2 = 2V$$

 $i_c = c \frac{dv_c}{dt} = 2x \frac{z}{6} e^{-t/6} = 2(1 - e^{-t/6}) v$ for $t \approx 0$

 $2i(t) - 2i_c - v_c = 0$ $\Rightarrow i(t) = i_c + v_c/2 = 1 - 3e^{-t/6} A, t = 0$

> The energy absorbed by the 41, during interval The encilly $(0,\infty)$ is -? Assume $V_{c}(0) = 6V$. $V_{c} = 10 + (6-10)e^{-t/8}$



$$V_{c}(0) = 6V \qquad V_{c} = 10 + (6-10)e^{-t/8}$$

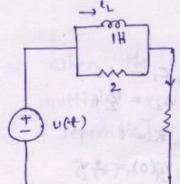
$$V_{c}(\infty) = 10V \qquad = 10-4 \cdot e^{-t/8}, \ t \neq 0$$

$$V_{c}(\infty) = 10V \qquad i_{c} = c \cdot \frac{dV_{c}}{dt} = e^{-t/8}$$

$$V_{c}(\infty) = 10V \qquad i_{c} = c \cdot \frac{dV_{c}}{dt} = e^{-t/8}$$

$$V_{c}(\infty) = 10V \qquad i_{c} = c \cdot \frac{dV_{c}}{dt} = e^{-t/8}$$

 $E_{4A} = \int_{0}^{\infty} i(t) \cdot 4 \cdot dt = 16j$.



Determine i(t), tzo.

filt) Assume in(0) = 2A.

$$\frac{2}{2}$$
 (i). $i_{\perp}(0) = 2A$

(ii).
$$i_{\perp}(\infty) = \frac{1}{2} A$$

(iii).
$$\gamma = \frac{1}{k_{eq}} = 1sec$$

$$i_{L}(t) = V_{L} + (2 - \frac{1}{2}) e^{-t/2}$$

$$= 0.5 + 1.5 e^{-t}, t 70$$

$$V_{L}(t) = L. \frac{di_{L}(t)}{dt} = -1.5 e^{-t}, t 70$$

$$V_{L}(t) = V_{R}(t) \Rightarrow V_{L}(t) = 2 \cdot i_{R}(t)$$

$$= i_{R}(t) = -0.75 e^{-t}, t 70$$

$$\downarrow i_{R}(t) = 0.75 e^{-t}, t 70$$

$$\downarrow i_{R}(t) = 0.1 \frac{di_{L}}{dt}$$

$$\downarrow i_{L}(t) = \frac{1000(t) - V_{L}}{dt} = \frac{1000(t) - V_{L}}{dt}$$

$$= \frac{1000(t) - V_{L}}{dt} = \frac{1000(t) - V_{L}}{dt} = 0$$

$$\Rightarrow \frac{1}{200} \frac{di_{L}}{dt} + i_{L} = 2i_{L}$$

$$\frac{5}{200} \frac{di_{L}}{dt} + i_{L} = 200(t)$$

$$\Rightarrow \frac{1}{dt} + 40 i_{L} = \frac{9000(t)}{200(t)}$$

$$i_{L}(0) = 0 = i_{L}(0^{t})$$

$$5 \cdot 2_{L}(s) - i_{L}(0^{t}) + +10 \cdot 1_{L}(s) = \frac{800}{5}$$

$$\Rightarrow I_{L}(s) = \frac{800}{5(s + 40)} - \frac{20}{5} - \frac{20}{5 + 4}$$

$$i_{L}(t) = 100(t) = \frac{1}{100} (20 \times 40 e^{-40t}) v(t)$$

$$= (10 - 8 e^{-40t}) v(t)$$

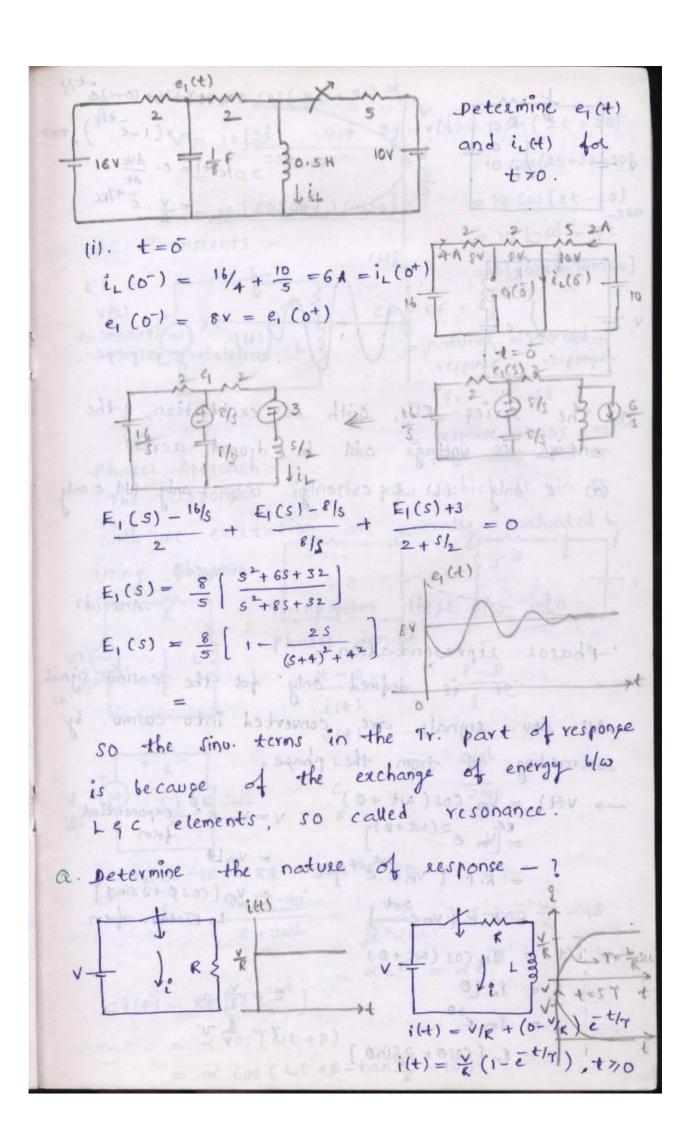
$$= (10 - 8 e^{-40t}) v(t)$$

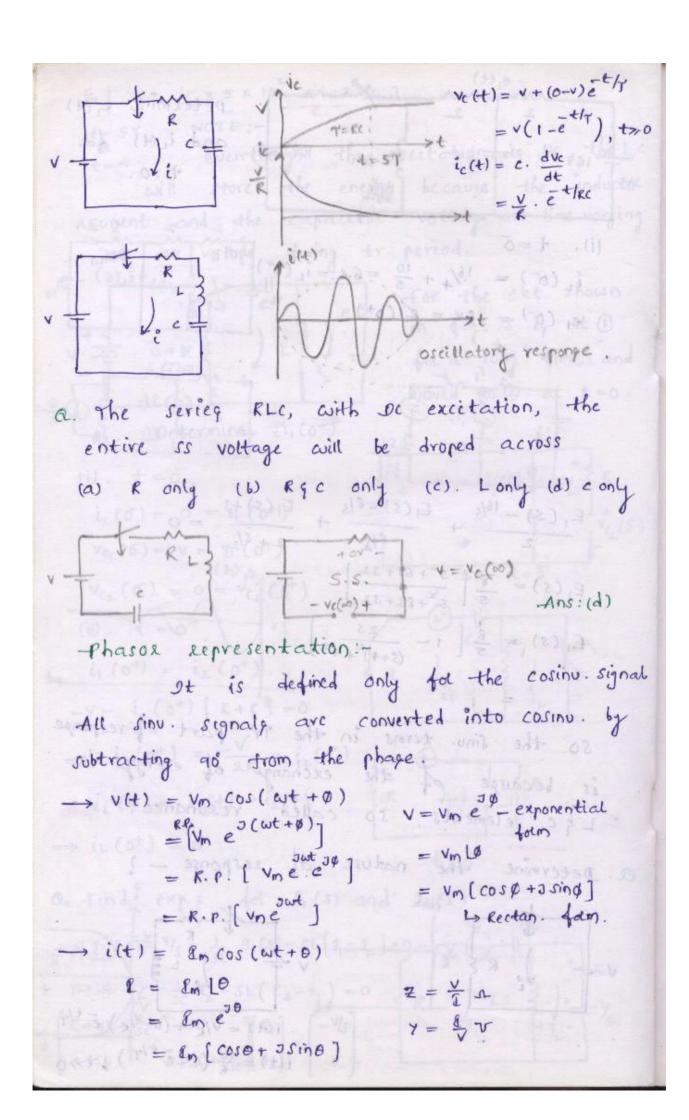
$$= (10 - 8 e^{-40t}) v(t)$$

```
Determine the ss voltages across the
            capacitoes.
                  V_1(\infty) = V_2(\infty) = (V_1 c_1 + V_2 c_2)/(c_1 + c_2) = \frac{5}{3} \sqrt{\frac{5}{3}}
         i(t) = e^{3t}, t > 0, r = \frac{1}{3}
   i(0+) = 101 0 b
   v_1(s) - \frac{2}{s} + \frac{1}{s} 2(s) = 0
                  V_1(s) = \frac{2}{s} - \frac{1}{s} \cdot \frac{1}{s+3} = 0 \cdot \frac{5/3}{s} + \frac{1/3}{s+3} = 0
         v_1(t) = \frac{5}{3} + \frac{1}{3} \cdot e^{-3t}, t > 0
  v_1(\infty) = 5/3v
              v_2(s) - \frac{1}{s} - \frac{2}{s} \cdot 2(s) = 0 (78) v = v = (3) sv
                v_2(s) = \frac{1}{s} + \frac{2}{s} \cdot \frac{1}{s+3} = \frac{5/3}{s} - \frac{2/3}{s+3}
                 V_2(t) = \frac{5}{3} - \frac{2}{3} \cdot e^{-3t}, t = 0
602 V2 (00) = 56 V
                                                                                                                         petermine the inductor
                       $10 5H3 / t=0 current fol too.
                                                                                                                             what is the energy
                                                                                                                          stored by an inductor
            after a long time after the switch is opened
                 (i). i_L(0) = 0 = i_L(0+)^{10A}
                                i_(0) = 10 A 0= (100) (-10) (5)
                          \gamma = \frac{1}{2} \sec \frac{1}{2} \sec \frac{1}{2} \sec \frac{1}{2} \sec \frac{1}{2} = \frac{1}{2} \sec \frac{1}{2} = \frac{1}{2} + \frac{1}{2} = 
                                                     = 10-10e , t >0 = 100e , t >0
```

EL = 1/2 x 5 x 10 = 250 J 3 1 12 200 00 50 t=57 NOTE; even-though the excitation ig Dc, the L,c will store the energy because the inductor current and the capacitor voltage are time varying with the slope during tr. percod. for the ckt shown in fig. s is at ()

Red a long time and moved to (2) at t=0. moved to 2 at t=0. a. Determine 1, (0+) (i). t=0, $i_L(\sigma) = 0 = i_L(o^+)$ νe, (δ) = v = 4, (0+) V(2 (0) = 0 = V(2 (0+) (ii) $t = 0^+$ i, (0+) = i2 (0+) $-v - i_1(0^+)(R+R) = 0$ $\Rightarrow i_1(0^+) = \frac{-\sqrt{2}}{2R} = i_2(0^+)$ $i_{L}(t) = i_{1}(t) \sim i_{2}(t)$ \Rightarrow il (0+) = 0 a pair total walds Oz. Find exp. q fol & (s) and \$2(s) - R 1, (s) - 1/5 - 1 Sc . S, (s) - SL [1, - 1,] =0 $-R\cdot I_2 - \frac{1}{SC}I_2 - SL(\ell_2 - \delta_1) = 0$ $\begin{bmatrix} R + SL + \frac{1}{SC} & -SL \\ -SL & R + SL + \frac{1}{SC} \end{bmatrix} \begin{bmatrix} Q_1 \\ Q_2 \end{bmatrix} = \begin{bmatrix} -V/S \\ 0 \end{bmatrix}$





Eq:
$$V(t) = 10 \cos(2t + 30)$$
 $V = 10 \frac{130}{50}$
 $V = 10 \frac{130}{50}$

is
$$(t) = \frac{Vm}{\sqrt{R^2 + (\omega L)^2}}$$
. Sin [$\omega t + \beta - t$ and $\frac{\omega L}{R}$]

(2). LTA:-

 $V(t) = V_0 \sin(\omega t + \theta)$
 $V(t) = V_0 \sin(\omega t + \theta)$
 $V(t) = V_0 \sin(\omega t + \theta)$
 $V_0 = V_0 \cos(\omega t + \theta)$
 $V_0 = V_0 \cos$

at
$$t = t_0$$
 is $\omega t_0 + \beta = t_0 + \frac{\omega t}{R}$

The excitation is $v(t) = v_m \cos(\omega t + \beta)$

then $i(t) = i_{tr} + i_{ss}$
 $= k \cdot e^{-\frac{t}{L} \cdot t} + i_{ss}$
 $= k \cdot e^{-\frac{t}{L} \cdot t} + i_{ss}$

where $k = \frac{-v_m}{R^2 + (\omega t)^2}$ $\cos(\beta - t_0 - t_0 - t_0)$

Suppose $e - t_0 - t_0 - t_0$
 $e - t_0$

The value of to = 0 Re . 245 + VA = tan ozer

```
Vc(t) = Vetr + Vess
 = k. e t/Re + vm . sin (wt+p - tan wcr)
      V_{c}(\delta) = 0 = V_{c}(0^{+}) = V_{c}(0)
 where k = \frac{-V_m}{\int 1 + (\omega c R)^2} \sin(\rho - \tan^2 \omega c R) <<1
         i(t) = c. dv.(t)
      Suppose p - tant wer = 0 > k = 0 > ve (+) = vess(+)
     et is tr. free response
        p = tant were at t=0.
        wto + 0 = tan wer , t= to
  It the excitation is v(t) = vmcos (wt+0)
      Ve (+) = Vetr (+) + Vess (+)
           = K. e t/RC + Vm cos (wt+ & -tan wcr)
     Vc(0) = 0 = Vc(0+) = Vc(0)
     where k = \frac{-v_m}{1+(\omega c_R)^2} \cos(\phi - \tan^2 \omega c_R) < 1
 i(t) = cdvc(t), surpose w-tantwcr = 1/2
   \Rightarrow k=0 \Rightarrow V_{c+r}(t)=0. \Rightarrow V_{c+r}(t)=V_{ss}(t)
    A tr. free response,
    Ø = tantwert 1/2 at t= Q & wt. + Ø = tantwer + 1/2 at
     )cos(24+1/4)
   The value of to for the tr. free response,
      2 to + 11/4 = tan wer + 11/2
If In the above case excitation is sin(2++11/4)
. The value of to = 0 RC. 2to + 1/4 = tan wer
```

The tr. tree condities not possible for the now's with both energy storing elements in for RLC. Since the complex poles $S_1, S_2 = 4 \pm JB$

i(t) = ext (k, cospt + kz sin pt) + iss(t)

Here k, and kz are functions of sin q

cosine res. hence no time satisfieq k, and

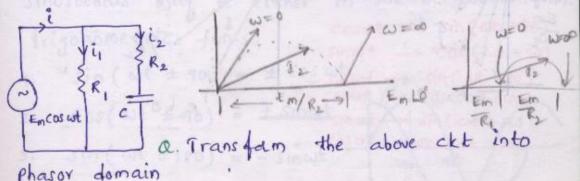
kz fimultaneously zero to tr. term is always

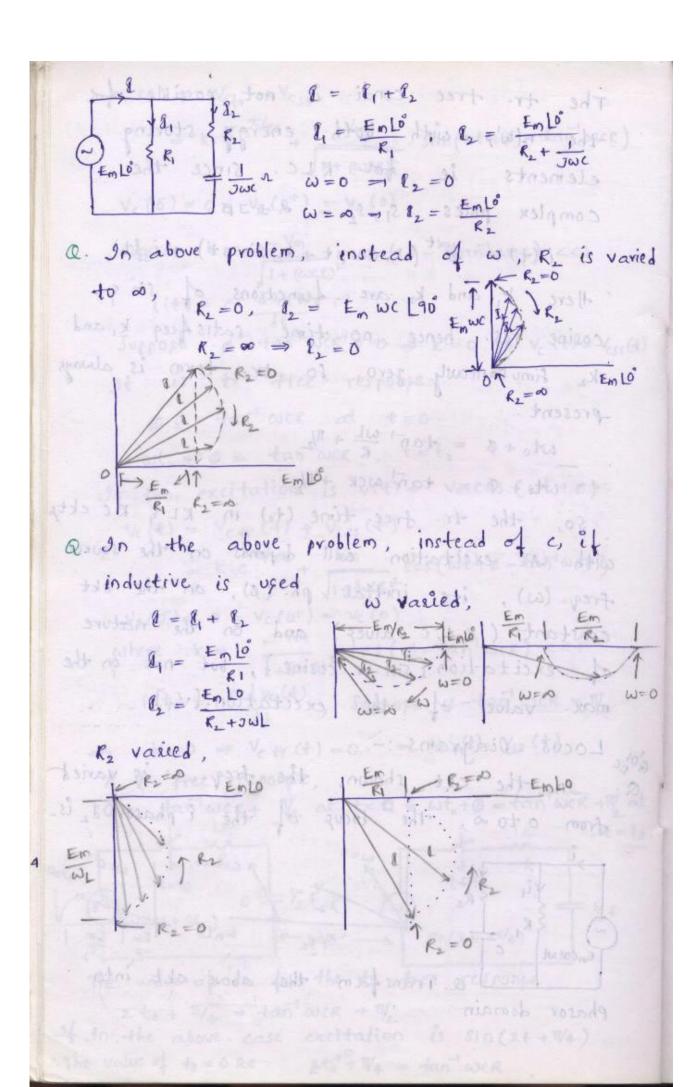
present.

 $\omega t_0 + \phi = \tan^{-1} \frac{\omega L}{R} + \frac{\pi}{2}$ $\omega t_0 + \phi = \tan^{-1} \omega c R + \frac{\pi}{2}$

so, the tr. free time (to) in RLE RC ckts with Ac excitation will depends on the source freq. (w), its initial ph. (p), on the ckt constants (R, L, c values) and on the nature of excitation [sin or cosine], but not on the move. value of the excitation. [vn]

from 0 to 0, the locus of the i phasor I, is-





```
AC fundamentals
  (sinu) = sinu =0 1-10 0 = 0 + 10) Fire 5
                     u(t) = Vmsino = Vmsinat = Vmsin(=)+
  d (sinu.) = sinu
     The indi- 4 was 5 - - is them a a
 trequency = No. of eyeles per second.
        Tsec - diayele (331+ tw) 200 3 = 3
    ( or + lace 100 ) all a - ( 001+ 718) 200 0 =
      Tree xicycle = No. of cycle in one fee
   のはチェーキ、人心をなれる中は、3万大の(atto)
 => vo(t) = Vn sincet = Vn sincens) to all a
Lead, Lag and inphase quantitives:
                         (O'Un white must - v
                    1-16031+00/p. 12/m Stout = 0
                 (0+ + 031+ 00 +3 Fro you sin (w+ +36)
                            ( 1 Lang 40 ( Sin ( Wd - 41°)
                      1 of ( Darry) v3 = Vm, snowt
1. ph. difference can be ( " V, = Vm, sin (wt/30)
 obtained for the sinusoidals vi was an (wt 30)
                                V4 - 4m4 sm ( w+ = +50)
with same frequency
2. While defining the ph. difference, all the
   sinusoidals may be either in sine of cosine form.
   Trigonometric fun.s: cos (wt-90)
                            cosut -> sin(wt +90)
     sin ( wt ± 90) = ± cos wt wt -> sin ( wt +180)
   2. Cos(wt ± 90) = Fsinwtsinut > sin(wt + sed)
  3. sin (wt #180) = - sinut cos ( wt #360)
  4. cos(wt ± 180) = - coswt
```

```
a. i = 5 sin wt, i = 6 cos wt then i leads ity 90
      i, = 6 sin (wt +90)
 Q. i, = 5 sinut, i2 = -6 coswt then i2 logs iby 98
      i, = 6 cos (wt +186)
        = 6 cos (wt +180) = 6 sin (wt +180 +98)
   = 6 \sin(\omega t + 270)
     = 6 sin (wt + 360 - 96)
      = 6 \sin(\omega t - 96)
Q. V1 = -10 cos(wt + 50), sandy on box god, box
   V2 = 12 sin (wt-10). V2 leads v, by (40-10)=30
   ν, = 10 cos (ωt +50+180) VI lags V2 by +6. (20+10) (40~10)
 = 10 Sin (wt + 50 + 180 + 90)
  = 10 sin (wt + 360 - 40)
  = 10 sin ( wt - 40 )
a. (1 = 3 sin (714t-20)
                         the disterence com b
82 = - 5 (os (714 t + 30) then is lage i, by 48
 a the ph. angle of current i w.r.t voltage of
  Up with the ckt shown is _
(a) 0 (b) 45° (c) -+5° (d) -98.
              twing the state for the state
 V_1 = 100(1+3)
  102 to 200 in contract to 200 to 3 oins ...
 V2 = 100 (1-3) +was = - (0) + 10 3 310
 Total voltage = v1+v2 - = (08 = 100 ora) .
               = 200 + 70 = (091 ± 10) 203 + A
```

$$l_{R} = \frac{V}{R} = \frac{200}{10} = 20 L^{6}$$

$$l_{L} = \frac{V}{V_{L}} = 20 L^{6}$$

$$l_{L} = \frac{V}{V_{L}} = 20 L^{2}$$

$$l_{L} = \frac{V}{V_{L}} = 20 V_{L} L^{4}$$

$$l_{L} = \frac{V}{V_{L}} = \frac{V}{V_{L}} = \frac{V}{V_{L}}$$

$$l_{L} = \frac{V}{V_{L}} = \frac{V}{$$

10)

currents &1, &2 and &3 are met at a sonction. All currents are marked as entering

a node. if
$$l_1 = -6 \sin \omega t$$
, $l_2 = 8 \cos \omega t$,

then $l_3 = \omega ill be - .$
 $l_1 + l_2 + l_3 = 0$
 $l_3 = -8_1 - l_2$
 $= 6 L^6 - 8 L 9^6$

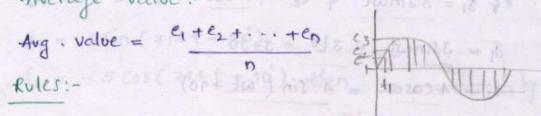
Average and RMS value:-

 $l(t) = l(t + t)$
Ly periodic wave form.

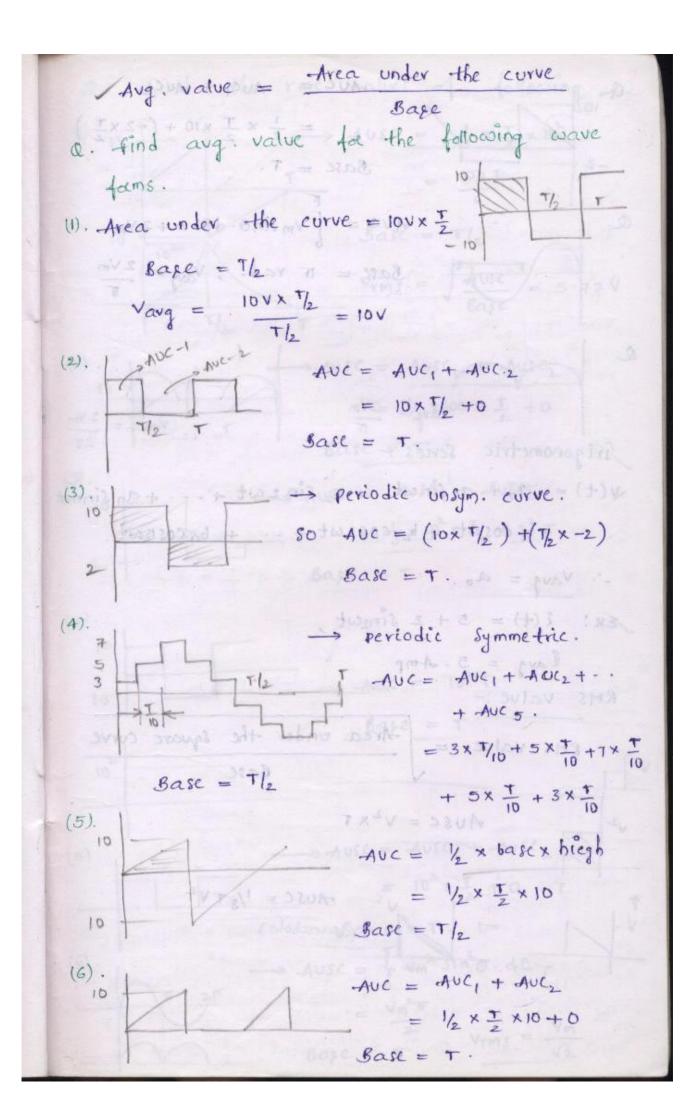
 $l(t) = l(t + t)$

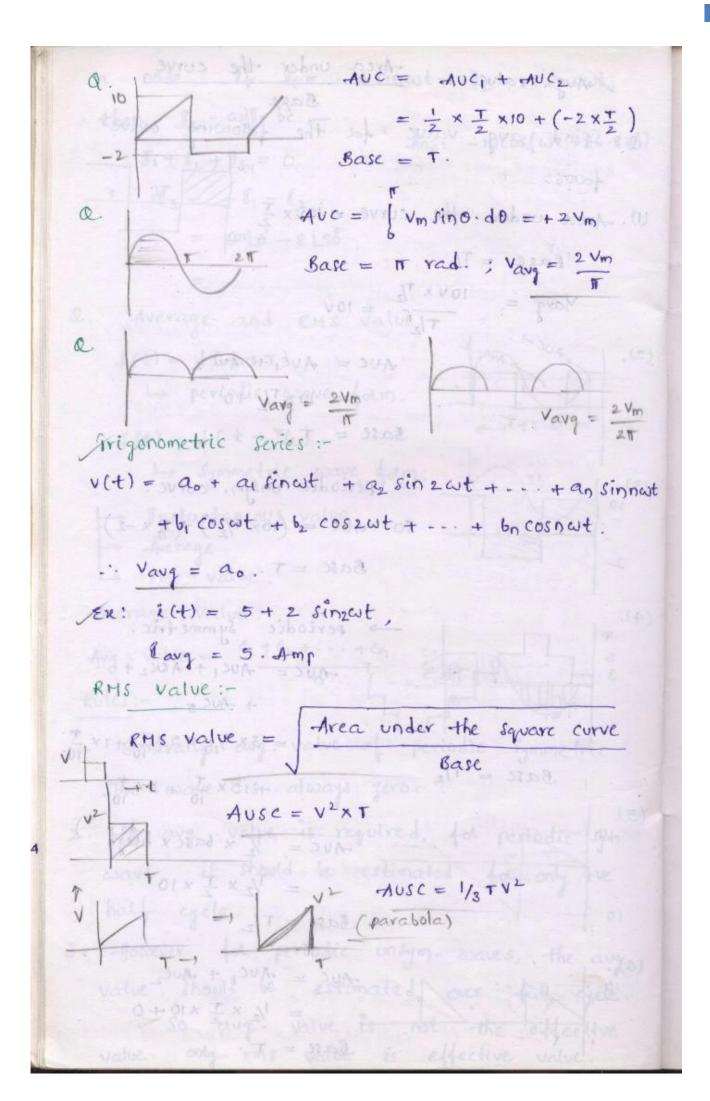
-> symmetric wave form. -> 8nstantaneous value -> Average

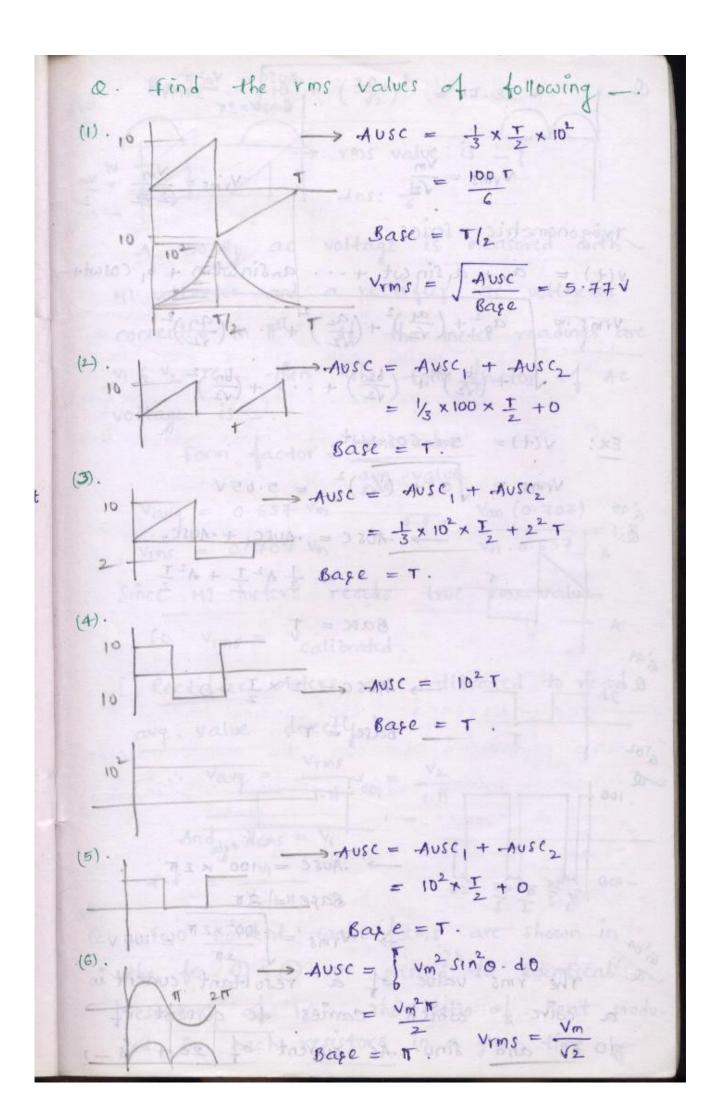
> rms value. 360 - 40) (at tw) niz lu : Average Value: -2014) = 3 } Junio = 12 18 10 Aug value = e1+e2+...+en (3)

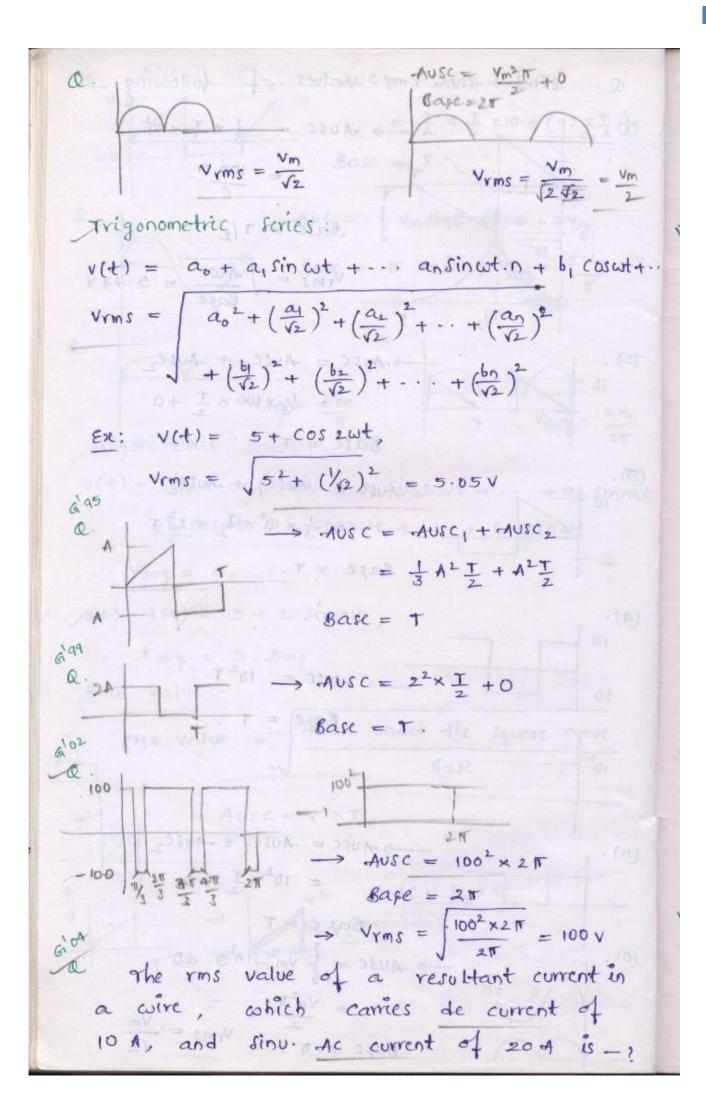


- 1. Generally ang. value of periodic symmetric Sine wave is always zero.
- 2. If any value is required, for periodic sym. wave, it should be estimated for only the half eyele + or + or) are
- 3. However for periodic unsym. waves, the aug. value should be estimated over full cycle. So ang. value is not the effective only rms value is effective value. value.









Erms =
$$\int 10^2 + \left(\frac{20}{V_2}\right)^2 = 17.32 \text{ A}$$
.

If $\int 10^2 + \left(\frac{20}{V_2}\right)^2 = 17.32 \text{ A}$.

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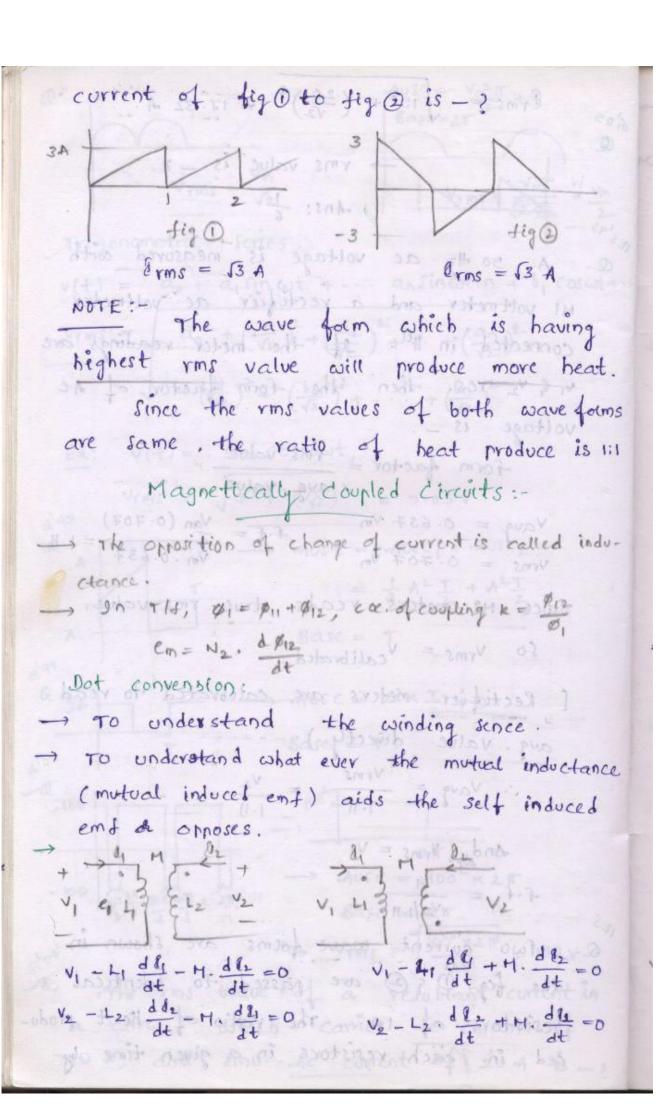
If $\int 10^2 + \left(\frac{20}{V_2}\right)^2 = 17.32 \text{ A}$.

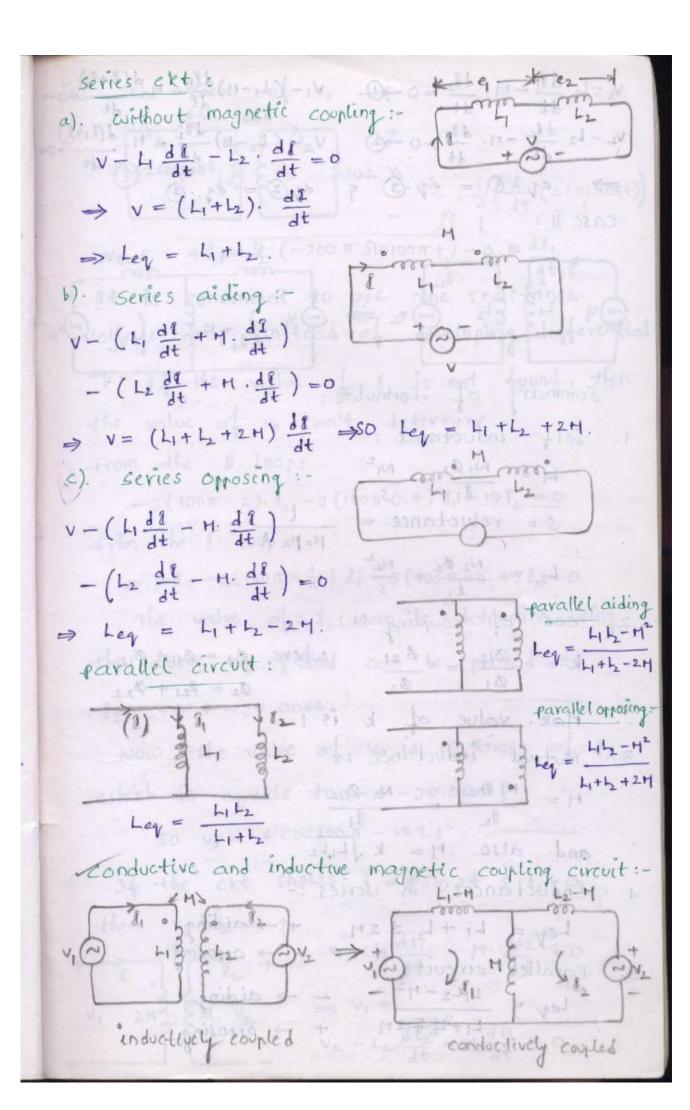
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If $\int 10^2 + \left(\frac{20}{$



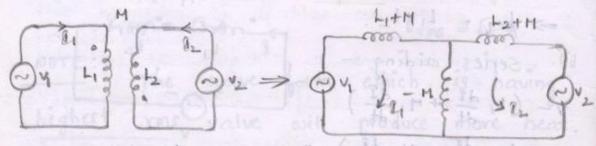


$$V_{1}-L_{1}\frac{dU_{1}}{dt}-H \cdot \frac{dU_{2}}{dt}=0 - 0 \qquad V_{1}-(L_{1}-H)\frac{dU_{1}}{dt}-H \frac{d(U_{1}+U_{2})}{dt}=0 - 0$$

$$V_{2}-L_{2}\frac{dU_{2}}{dt}-H \cdot \frac{dU_{1}}{dt}=0 - 2 \qquad V_{2}-(L_{2}-H)\frac{dU_{2}}{dt}-H \cdot \frac{d(U_{1}+U_{2})}{dt}=0$$

$$\Rightarrow eq \cdot 0 = eq \cdot 3 \quad q \quad eq \cdot 2 = eq \cdot 4$$

case 11:



Summary of formulae? (12 11 11 11)

1. Seif inductance: (1)

$$h_1 = \frac{N_1 \emptyset_1}{\emptyset_1} = \frac{N_1^2}{S}$$

$$S = \text{reluctance} = \frac{1}{\text{Ho Mr. A}}$$

$$L_2 = \frac{N_2 \emptyset_2}{\emptyset_2} = \frac{N_2^2}{S}$$

2. coe. of coupling (k):

$$k = \frac{\varphi_{12}}{\varphi_{1}} = \frac{\varphi_{21}}{\varphi_{2}} \quad \text{where } \varphi_{1} = \varphi_{11} + \varphi_{12}$$

$$\varphi_{2} = \varphi_{21} + \varphi_{22}$$

Max. value of k is 1.

3. Mutual inductance:-

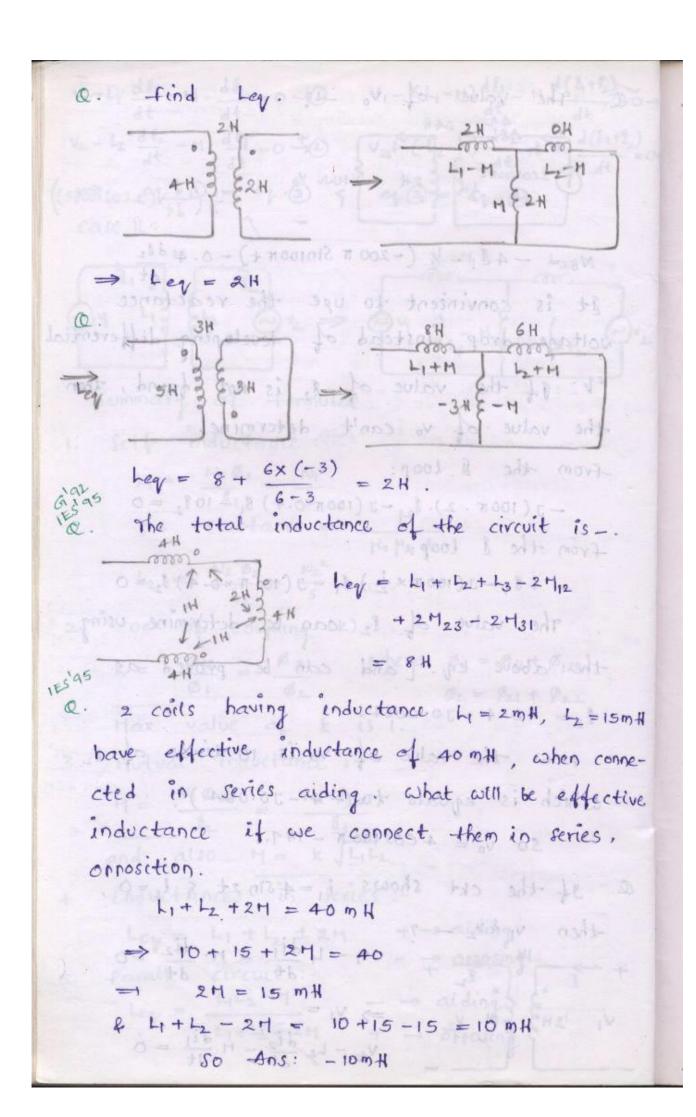
$$M = \frac{N_1 \otimes 21}{\theta_2} = \frac{N_2 \otimes n_2}{\theta_1}$$
and also $M = K \sqrt{L_1 L_2}$

+. Enductances in series:

Ley =
$$L_1 + L_2 \pm 2H$$
 $+ \rightarrow aiding$
5. Parallel circuit:- - \rightarrow opposing

Leq =
$$\frac{L_1L_2-H^2}{L_1+L_2\mp 2H}$$
 - \rightarrow aiding + \rightarrow ortosing

Q. The value of vo -? Ar ath 1 2 cosmont 1 & 24 From Vo (d (2 cos (00 1+)) Vo = -481-1/2 (-200 1 Sinjoon+)-0.4 dl2 It is convincent to use the reactance voltage drop instead of developing differential er. If the value of 12 is not found, then the value of vo can't determine. from the & loop: $-J(100\pi \cdot 2) \cdot \ell_2 - J(100\pi \cdot 0.4) \ell_1 - 10\ell_2 = 0$ from the & loop: $-48,-J(100 \pi \times \frac{1}{2})8,-J(100 \pi \times 0.4)8_2=0$ The value of 82 can be determine using the above eq. [and can be proved as Now the value of vois 10 times of 12 which is equals to (-4-10.064). SO Vo = 4 COS 100 N - 179.1 Q. 9f the ckt shows i,=4sin 2t & iz=0, then v1 & v2 - 7 of 12 + 01 - 4 din = H. diz =0 $V_2 - L_2 \frac{di_2}{dt} - H \frac{di_1}{dt} = 0$



a Two identical coils of negligible resistance when connected in series with a current of 10 A. when the terminals of one of the coil is reversed, the current drawn is 8A, then the coe of coupling - ? wood was all

June Lu = be to L. (OP H has) ald - my PI = 10 A = J[WL+WL2-2WH]

82 = 8 A = 0 sty stast sest J[WL, +WL_ +2WH]

 $\Rightarrow \frac{L+H}{L-H} = \frac{10}{8} \Rightarrow L=9H$

Also $H = k\sqrt{L_1L_2}$ $= k\sqrt{L_1L} = kL$

 $\Rightarrow k = \frac{H}{L} = \frac{1}{4}$ Q. Two inductive coils $h_1 + h_2$ are magnetically coupled in series orrosing & in parallel aiding res. The mutual inductance blow the coil is H. The equivalent inductances in the two wills

cases will be —? L1+L2-24 & L1+L2-24

My some solar of Acrocificuits thing & momen

Ac through pure resistance :-

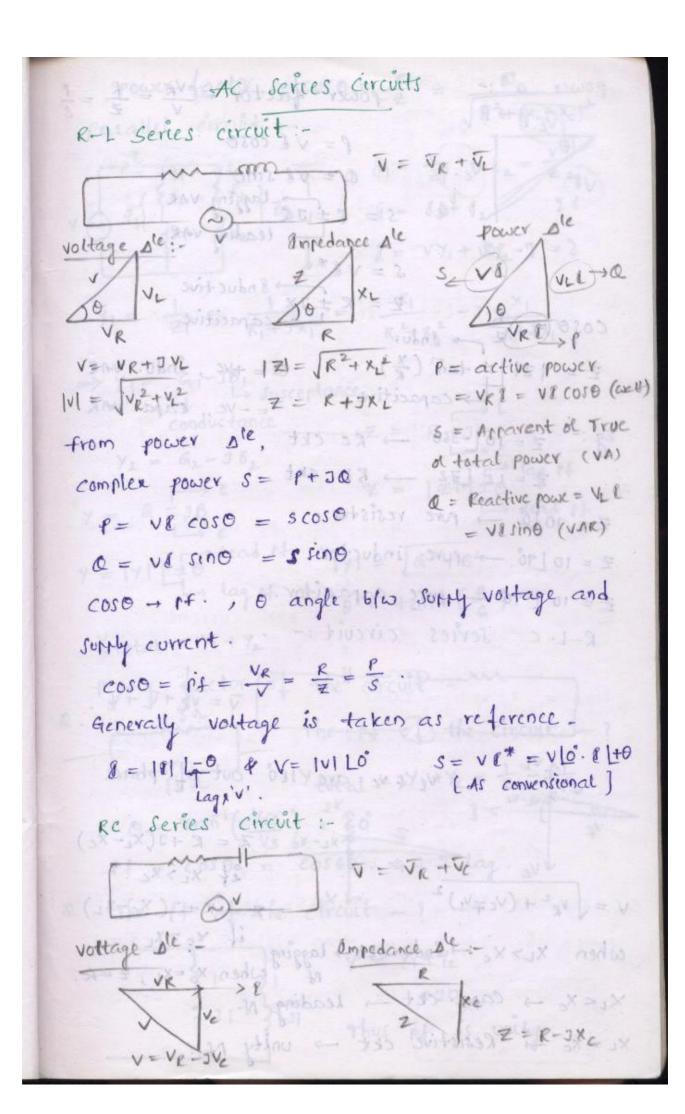
The current i(t) in phase with voltage v(t)

The active power 100%, reactive power ox

-> power is double freq. transient. (freq. of power = 100 Hz) - power is unidirectional. Ac through pure inductance: $V_L(t) = L \cdot \frac{di(t)}{dt} = L \cdot \frac{d}{dt} \left[8m sin \omega t \right]$ = 2m L. w coswt - pailyuns to son site = vm. sin (w+ +90), where vm= 8mwL. Anductive reactance XL = WL = 28+1 -> voltage leads the correct by 98. , power is double freq. transient (" f of v & - power is bidirectional. -> active power = 0% (There is no any power utilized to but it is transferred from land to source, source to load alternatively. Reactive power a = 100% Ac through pure capacitor: i(t) = c. dv(t) $\frac{1}{x_c} \cdot \sin(\omega t + 90) , \quad x_c = \frac{1}{\omega c} = \frac{1}{2\pi f c}$ JOTE V & leads v by 98. remain 3 points are similar to inductance.

In agent do their state of the Francis of the

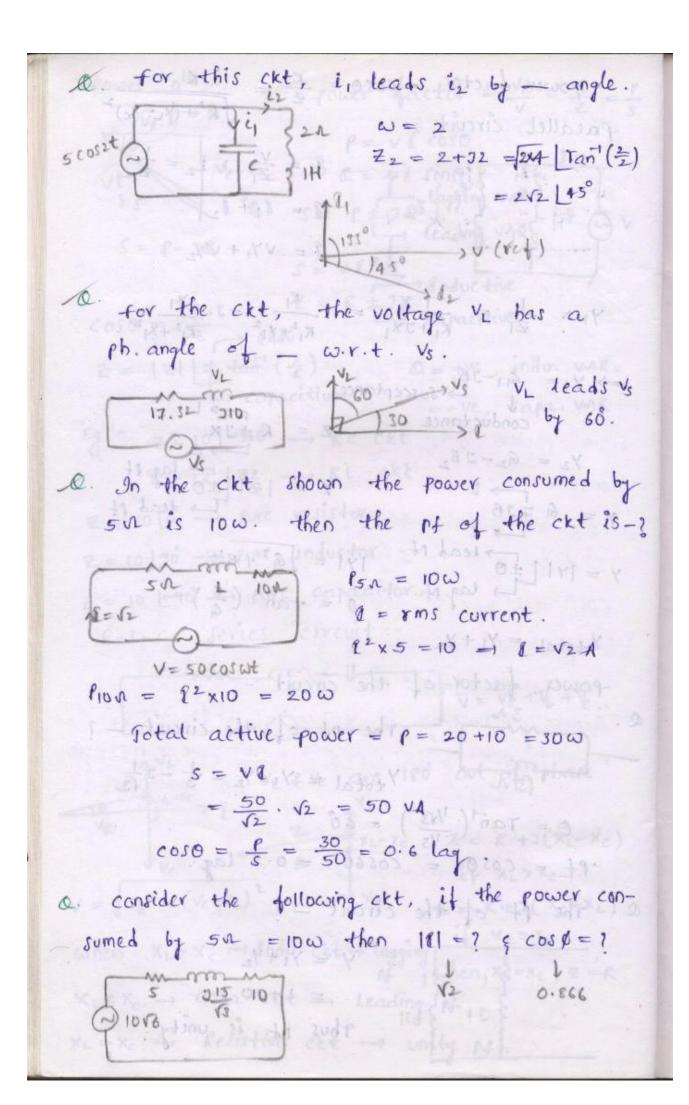
The earliest power took, reporting power or



```
power ple:- power factor = \frac{VR}{V} = \frac{R}{Z} = \frac{P}{S}
                                                                                                                                                                   P = V & coso
                                                                                                                                                         a = ve sino
                                                                                                                                                                       P = J@ lagging VAR leading VAR
             S = P - JQ
S = V E^*
Z = R \pm JX
Coso = \frac{R}{Z} \rightarrow Indu.
                   Z = |Z| | \pm \tan^2(\frac{x}{R})  Q = +vc, indu. VAR
                                                                                     L→ capacitive =-ve, capa. VAR
           Eq: = Z=10[-360 -> RC CKt 3 a volony movi
                                            Z = 12 L72 -> RL ckt 2 racing salgmos
         Z = 10 Lo -> pure resistor
           Z = 10 L90 -> pure inductor 2 - one 10 de
           Z = 10 1-90 - pure capacitor.
                R-L-c. series circuit:-
                                                                             m and It
                                                                                        VL & vc are 180 out of phase
                                                                                                  \frac{2}{R} \times \frac{1}{2} \times \frac{1}
when XL>Xc -> Endu-ckt -> lagging up no no. Z=R.
     X1< Xc -> capa. ckt -> leading of
    XL=Xc - Resistive ckt -> unity of.
```

power factor =
$$\cos \theta = \frac{R}{Z} = \frac{R}{R^2 + (R_L - X_C)^2}$$

Parallel circuit: - $\frac{R_1}{R_1} = \frac{V}{R_1}$; $\frac{1}{L_2} = \frac{V}{Z_2}$
 $\frac{V_1}{R_1} = \frac{1}{R_1}$; $\frac{1}{R_1} = \frac{V}{R_1}$; $\frac{V_1}{R_1} = \frac{V}{R_1}$; $\frac{V_2}{R_1} = \frac{V}{R_1}$; $\frac{V_1}{R_1} = \frac{V}{R_1}$; $\frac{V_1}{R_1} = \frac{V}{R_1}$; $\frac{V_2}{R_1} = \frac{V}{R_1}$; $\frac{V_1}{R_1} = \frac{V_1}{R_1}$; $\frac{V_1}$



Model - 6: power calculations:

a the complex power drawn by the circuit is -?

Thus $P = 3307 \omega$ = 3307 - J461.53. $Q = 461.53 \omega$ leading

nf = coso = cos [Tañ (a)] = 0.99 lead.

d The voltage of a ckt is 10 15±° 4 current is 21-45°. The active & reactive powers -?

$$V = 10 L15^{\circ}$$
 $0 = 60^{\circ} (lag)$ (lags $v by 60^{\circ}$.
 $0 = 2 L - 45^{\circ}$ $S = V0^{*}$
 $0 = 10 \times 2 L60^{\circ}$

Horsy this parks in several . It gripped to

Active power = 20 cos60 + 20 sin 60

o. The current through the current coil of a watter $R = 1 + 2 \sin \omega t$, it the voltage across the pressure coil $v = 2 + 5 \sin 3\omega t$. Then the wattmeter reading is -2

wattreter reading = 1x2 = 2w.

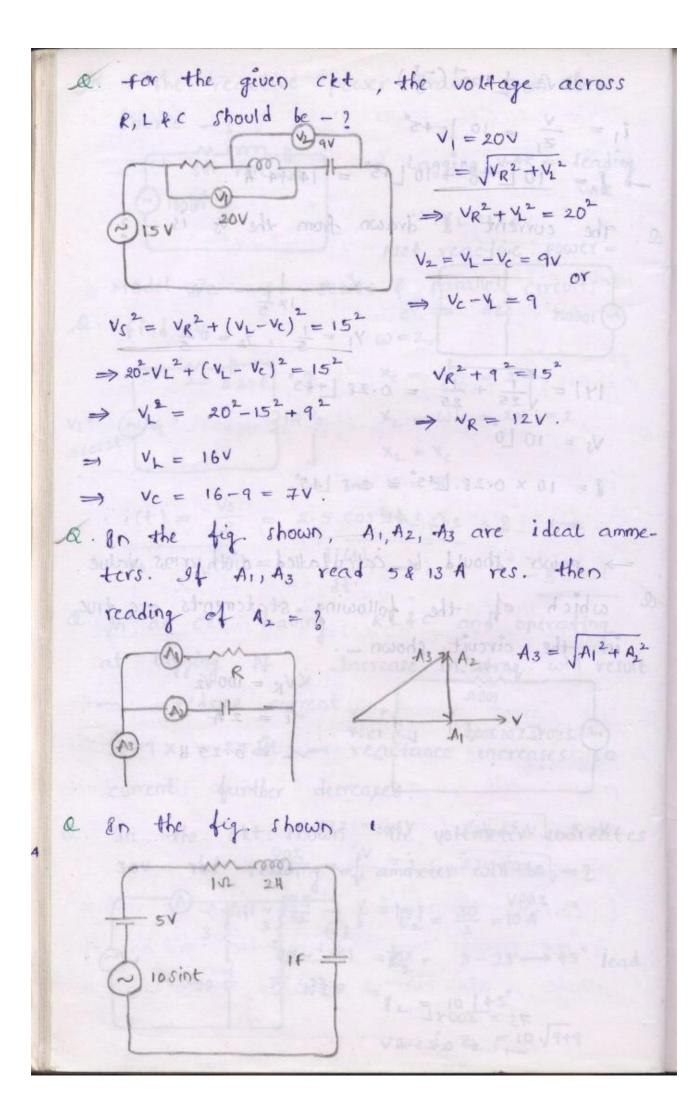
[correct to the funda. of current, the voltage is not present and correct the 3rd har of voltage, the current is not present.]

A. The reactive power drawn from the source - 1 to make most salama and a 30 +310 -310 - Lagging V-AR = leading @ 10000 + V = 2 .: XL = XC. Net reactive power = Model - 7: Ac series & parallel circuits: Q. find vo: $\omega = 2$, $2 \Lambda 0.25 F$ $1 \times c = \frac{1}{\omega c} = 2 \Lambda$ Z = R.Per. Carry good 21 by $i(t) = \frac{vs}{R} = 2.5 \cos 2t$ $V_0 = V_L(t) = L \cdot \frac{di(t)}{dt} = 200 -5 sinet$ a In ac ckt having RLAC and operating at lagging of . Increase in freq. will result +- reduce current it devoids torros air .a TXL = 21 AL = reactance encreases so current further decreages. a. In the ckt. shown, the voltmeter indicates 30v. The reading of ammeter will be - ? (10 03 13 to -13 to 2000 10 1+5 agailler V = i2 Z2 = 10 \q+9

$$i_{1} = \frac{V}{Z_{1}} = 10 \left[-45^{\circ} + 10 \right]$$

$$i_{1} = \frac{V}{Z_{1}} = 10 \left[-45^{\circ} + 10 \right]$$

$$= 10 \left[-45^{\circ}$$



case I serbel appeared when new and the then aloud is max; it aboth the sourced and good impedance i are pure resisting is R. - K. want of and St. Thorn 1 2 8 = 11.13 85 = 625 W case 2 .. The source is "Somplex finger dance. dondi. . when was any posser a transfor = full- I all of a la Network Theorems and Metwork Theorems super position theorem: - sampling xsignes -> Applied for linear, bilateral n/w. only. -> Atteast 2 ind. sources are required. -> can be applied for v or 8 but not for the power. YEAR-lance Xet - 1 10 -Homogenity principle: nother to will start a start of the The venin's:

Applicable for unilateral, bilateral, active & passive and it can't be attlied for

non-linear n/w.

- Thevenin's & Noeton's eq. ckts are applicable only for practical voltage & corrent sources res. and not too whater ideal sources.

a Maximum power transfer theorem: case 1: The power transfered to the load is max, it both the source and load impedance are pure resistive => R_ = R_s. condi-for max.p. transfer $P_{\text{max}} = \frac{V^2}{4R}$ casez: The source is complex impedance, but the load is pure resistive, dondi. for max. power transfer = R_=1Zs1 $\Rightarrow R_L = \sqrt{R_5^2 + X_5^2}$ case 3:- Both the source and load has complex impedance - months nothing vagor condi. for more p transfer: ZL= Zs* of Zs = ZL* case 4: source has complex impedance, but load has variable resistance RL, but fixed reactance XL. & The dondi. for max. p. transfer = RL = Rs2 + (XL + Xs)2 -> HPT is more applicable for communication and electronic ckts. and is never preferred in power systems owing to so! voltage drop and 50% losses in the source impedance. a petermine max power dissipated through RL. 3 6+ J8 24 5 RL 6+ J8 130 3 2 (0103 4) 200 @ 110L8 100 \$ 90L8 100 Who for make, ideal sooveds.

$$V_{Th} = 100V$$
 $Z_{Th} = 5 [53.13^{\circ}]$

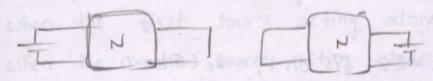
dondi. fol MPT $\rightarrow R_{L} = |Z_{Th}| = 5$

$$1 = \frac{100 [0^{\circ}]}{5 + 3 + 14} = 11.13 [-26.5^{\circ}]$$

$$\Rightarrow$$
 Pmax = $\ell^2 R = 11.13^2 \times 5 = 625 W$.

Reciprocity Theorem:

- The is known as reciprocal nlw.
- -> The NIW N should not contain any active elements of control sources.



$$\Rightarrow$$
 $V_1:V_2 = 1:4$ then $V_1 = V \times \frac{1}{5}$

$$R_1: R_2 = 10:1$$

$$V_2 = 10 \times \frac{1}{11}$$

$$R_1 : R_2 = 3:2$$

 $V_1 : V_2 = 3:2$

$$\Rightarrow V_1 = 10 \times \frac{3}{5}$$
; $V_2 = 10 \times \frac{2}{5}$

Gransients

charging function $f(t)^{+} = Ae^{-t/7} + B$ Discharging function $f(t)^{-} = A.e^{-t/7}$ Where $A = f(t=0^{+}) - f(t=\infty)$ and $B = f(t=\infty)$

The switch s is on vect) time. At t=0, s is thrown onto pos. 2 find vect), for too. At $t=\bar{0}$, s is on 1, \Rightarrow $v_c(t=\bar{0})=100$ V At $t=0^{+}$, s is 00^{2} , $\Rightarrow v_{c}(t=0^{+})=100^{\circ}$. (since the voltage across the capacitor can't change instantaneously. At $t=\infty$, S is on $2 \Rightarrow V_c(t=\infty) = -50V$ (9t discharges 100v and charges upto -50 V) At t=0, sis on 1, ic(0)=0A = 100 - (-50) = 150ION B = 1 - 50 V LAWE MADE CHARLE BY MILL CH $Vc(t) = Ae^{t/\tau} + B = 1sec$ At $t=\delta$, s is open i(t)=0At $t=0^{\dagger}$, s closed i(t)=0(Since inductor will not allow the current to change). At $t=\infty$, s closed \Rightarrow i(t)=100 A.. A = 0-100 = -100 no dample priprods B = 100 1(+)= 100-1000 =+11-(+0++)+ = A - 373/63

and selfted)

```
At t=\bar{0}, (sopened) v(t)=0 voltage

At t=\omega^{+}, (scloped) v(t)=100 v

At t=\omega, (scloped) v(t)=0 v

for inductor: charging dun: current

when inductor: charging dun: voltage

discharging dun: voltage

discharging dun: eurrent
```

A. The new consists of 2 ideal sources and several resistances, one of which is R. The power consumed by the resistor is P, walls when the first source acting alone & P2 w, when the second source acting alone. If both the sources are acting 2 gether then the power dissipated by R is -.

current through R for 1st source acting alone = $8_1^2 R = P_1 \implies 8_1 = \sqrt{\frac{P_1}{R}}$ 111^{14} $5^{11}^2 R = 9^{11} \implies 8^{11} = \sqrt{\frac{P_2}{R}}$

when both are acting together, $\ell = 1. + \ell''$ Notal power dissipated = $\ell^2 R$

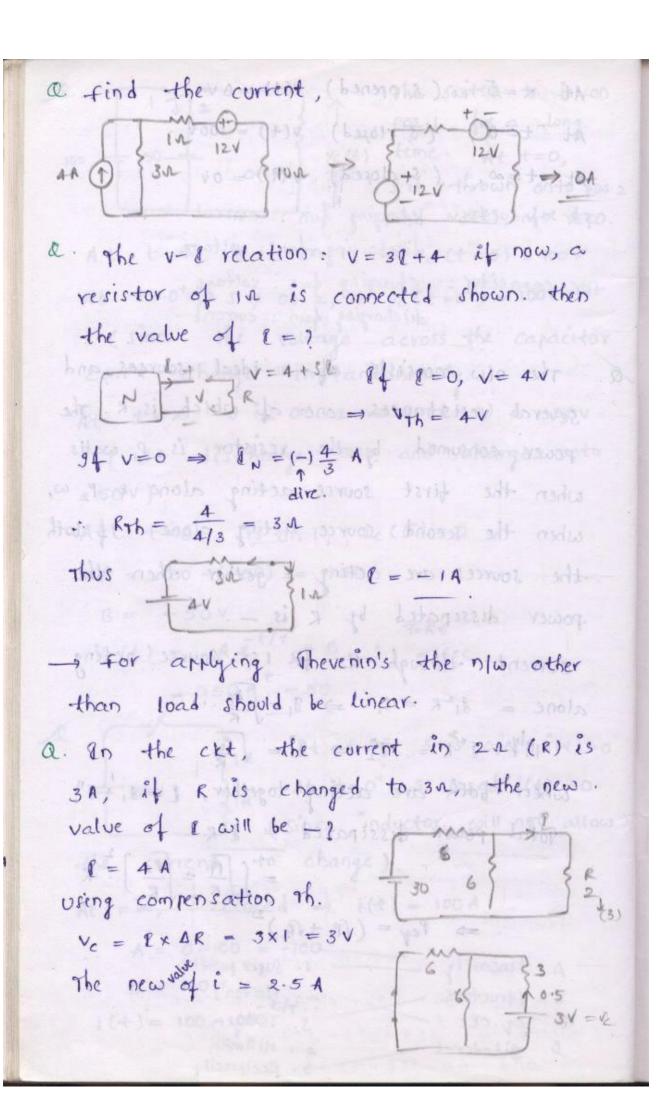
$$= \left(\sqrt{\frac{P_1}{R}} \pm \sqrt{\frac{P_2}{R}} \right)^{\frac{1}{2}} R$$

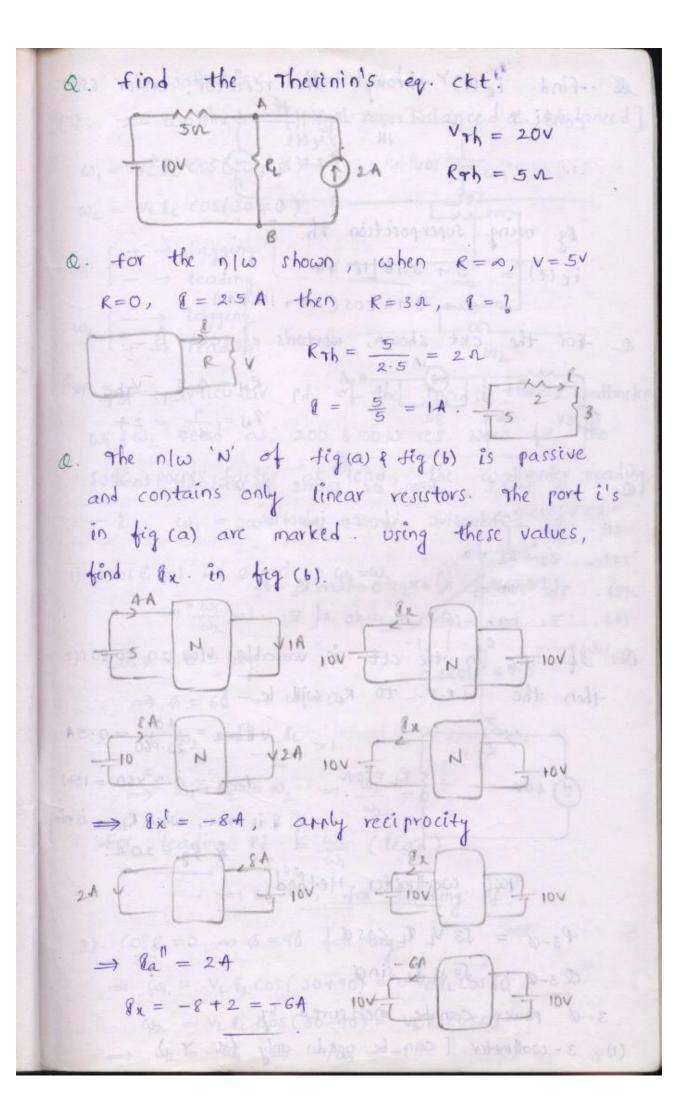
=> Pey = (SP1 ± SP2)2

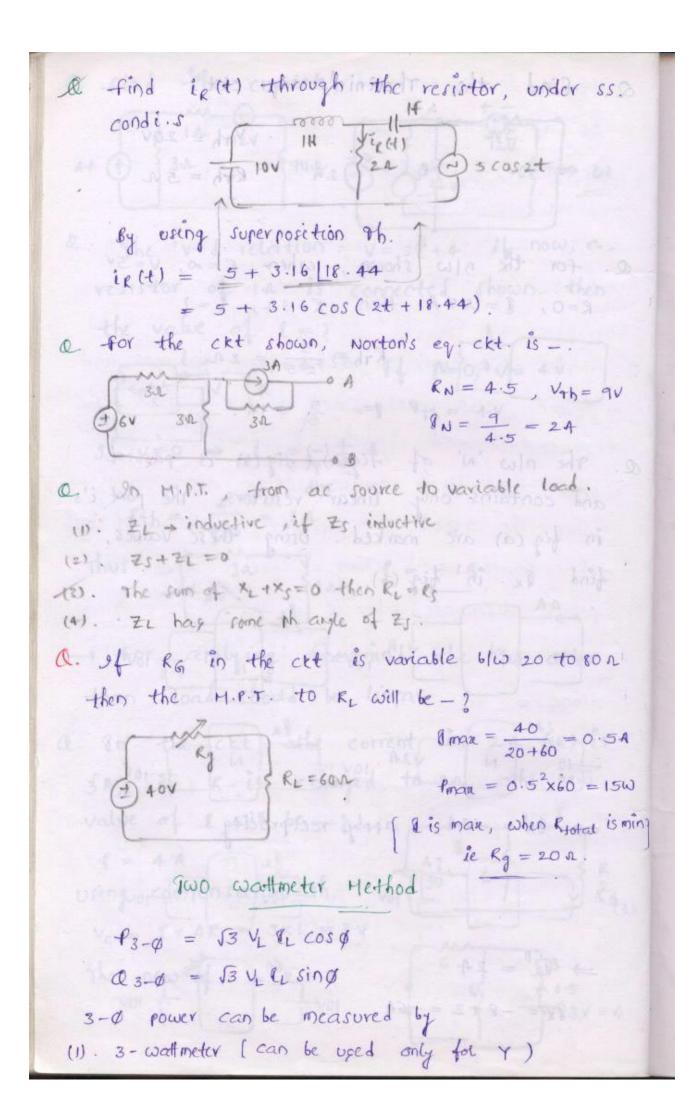
B structure 2. Norton's to coon out

e eq. cet 3. Telligen

D silederet 4. Hillman 5. Reciprocity

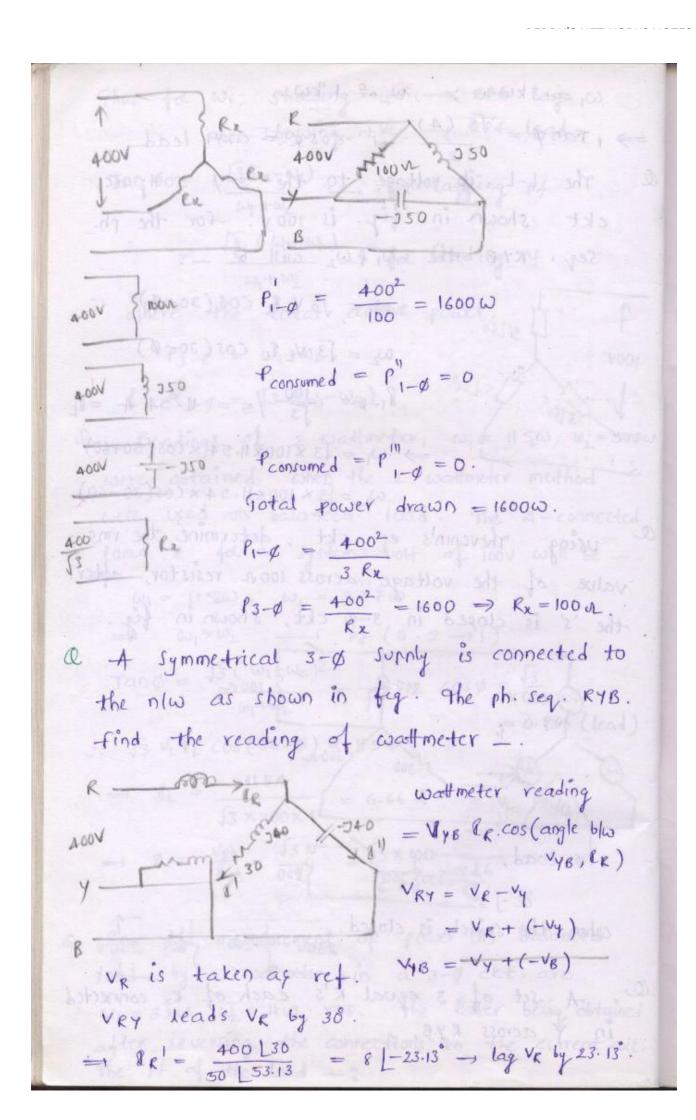


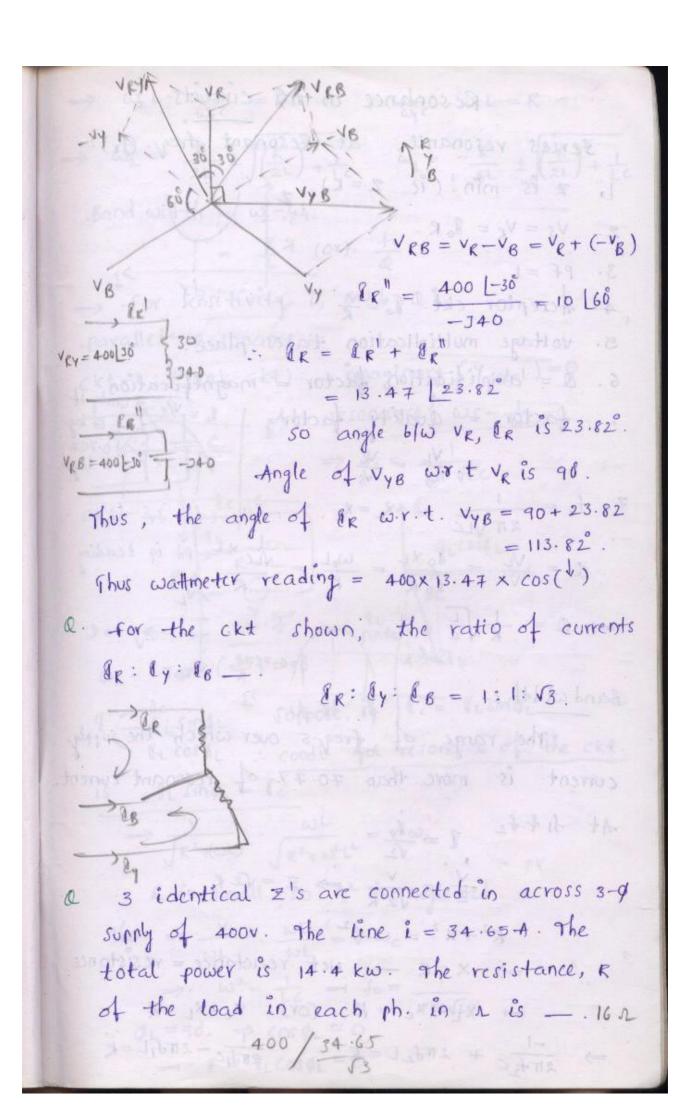




```
(2). 1- wattneter [ balanced Y]
(3). 2- wattreter [ Yol A, balanced of unbalanced]
  ω, = VL & L COS (30 ± Ø)
 \omega_2 = V_L \ell_L \cos(30 \mp 0) R - L_{Mag}
\omega_1 \left\{ \begin{array}{l} + \rightarrow lagging \\ - \rightarrow leading \end{array} \right\}
\omega_2 \left\{ \begin{array}{l} - \rightarrow lagging \\ + \rightarrow leading \end{array} \right\}
\omega_2 \left\{ \begin{array}{l} - \rightarrow lagging \\ \end{array} \right\}
\omega_2 \left\{ \begin{array}{l} - \rightarrow lagging \\ \end{array} \right\}
\omega_2 \left\{ \begin{array}{l} - \rightarrow lagging \\ \end{array} \right\}
e for particular of the load, the 2 wattmeter
    wife, read as, 200 $ 100 w res. Now for the
    same power, factor at lead, the watmeter reading
   -2 \omega_1 = 200 \omega \omega_2 = 100 \omega
 1). \cos \phi = 1 \rightarrow \phi = 0 \Rightarrow \omega_1 = \omega_2 of (0,0.5)
  \frac{\omega_1}{\omega_2} = 1
2). \cos \phi = 0.5 \log \phi
\Rightarrow \phi = 6\delta \Rightarrow \omega_1 = 0.
            & W2 = 53 VLBL - 1 = (0-08) 200 gly 81
        \Rightarrow \omega_1 + \omega_2 = \omega_2 \Rightarrow \frac{\omega_1}{\omega_2} = 0.
    for leading Pf = \frac{\omega_2}{\omega_1} (lead)
              = \omega_1 = 0, for leading rf.
   3). cos & =0 = 0 = 98 fol lag
   = = W = VL (LCOS (30+90) = - VL (LCOS 68
 ω2 = VL & COS (30-90) = VL & COS60
       \rightarrow \omega_2 = -\omega_1 \Rightarrow \omega_1/\omega_2 = -1
```

The Pt of the load -2





Resonance in AC circuits

series resonance, at Resonant freq. (fr):-

2.
$$V_S = V_R = \ell_0 R$$
.

6.
$$Q = amplification factor = magnification places factor = avality factor = magnification places for the sum of the su$$

7.
$$f_Y = \frac{1}{2\pi\sqrt{LC}}$$
, $X_L = X_C$.

$$Q = \frac{VL}{V} = \frac{80 \times L}{80 R} = \frac{W_0 L}{R} = \frac{1}{VLC} \times L \text{ pd iq leading}$$

Bandwidth: - It to the it

the range of freq.s over which the supply current is more than 70.7% of resonant current.

At
$$J_1 + J_2$$

$$Q = \frac{q_0}{\sqrt{2}}$$

$$\frac{V}{Z} = \frac{V}{\sqrt{2}R} \implies Z = \sqrt{2}R$$

$$\Rightarrow X_L - X_C = R \quad (or) \quad X_C - X_L = R$$

$$\Rightarrow \frac{-1}{2\pi f_2 C} + 2\pi f_2 L = R \qquad \frac{1}{2\pi f_1 C} - 2\pi f_1 L = R$$

$$\Rightarrow \omega_{L} - \frac{1}{\omega_{L}c} = R$$

$$\Rightarrow \omega_{L} = \frac{R}{2L} \pm \sqrt{\frac{R}{2L}^{2} + \frac{1}{Lc}} \qquad \omega_{1} = -\frac{R}{2L} \pm \sqrt{\frac{R}{2L}^{2} + \frac{1}{Lc}}$$

$$\text{band width } = \omega_{2} - \omega_{1}$$

$$= \frac{R}{L} \quad (\text{or}) \cdot \frac{4}{Q}$$

$$\Rightarrow \text{for sensitivity } \uparrow, \quad \text{Bw } \downarrow, \quad \text{Q} \uparrow$$

$$\text{parallel Resonance :-}$$

$$\text{ckt-1: (Tank ckt): 'ronaginary (Y+otal) = 0}$$

$$\text{At resonance } \downarrow \text{wc-} \downarrow \text{L} = 0$$

$$\Rightarrow f_{0} = \frac{1}{2\pi} \sqrt{Lc}$$

$$\text{ckt-2: } \downarrow \text{left}$$

$$\text{QL} = \frac{1}{2\pi} \sqrt{Lc}$$

$$\text{R's small so } R^{2} \text{ is neglected.}$$

$$\text{Then } \Rightarrow \frac{V}{WL} = \frac{WL}{WL} = V \cdot W_{C}$$

$$\Rightarrow W^{2} = \frac{1}{Lc} \Rightarrow f_{0} = \frac{1}{2\pi} \sqrt{Lc}$$

$$\text{QL} = \frac{1}{2\pi} \sqrt{Lc}$$

$$\text{PL} = \frac{1}{2\pi} \sqrt{Lc}$$

Thus min current drawn by the ckt. → 8 is small so Rejector ckt. - z is very high.

- so current magnification is taking place in the ckt.

ckt -3:

At Resonance,

img (Ytotal) = 0

Y1 =
$$\frac{R}{R^2 + X_L^2} - J\frac{XL}{R^2 + X_L^2}$$

$$Y_{1} = \frac{R}{R^{2} + X_{L}^{2}} - J \frac{X_{L}}{R^{2} + X_{L}^{2}}$$

$$\Rightarrow \frac{X_{C}}{R^{2} + X_{C}^{2}} = \frac{X_{L}}{R^{2} + X_{L}^{2}}$$

$$Y_{2} = \frac{R}{R^{2} + X_{C}^{2}} + \frac{J X_{C}}{R^{2} + X_{C}^{2}}$$

$$\Rightarrow \frac{x_c}{R^2 + x_c^2} = \frac{x_L}{R^2 + x_L^2}$$

$$\Rightarrow (R^2 - \frac{L}{c})(\frac{L}{\omega_0 c} - \omega_0 L) = 0$$

case studies:-

1.
$$R^2 \neq \frac{L}{c} \implies \omega_0 L = \frac{1}{\omega_0 c} \implies f_0 = \frac{1}{\Re r \sqrt{Lc}}$$

$$2 \cdot \frac{1}{\omega_{0}c} - \omega_{0}L \neq 0 \Rightarrow R^{2} = \frac{L}{c}$$

ie img (7 total) = 0 - ckt. resonates

at all the frequencies.

The total admittance of ckt at resonance,

$$= \frac{R}{R^2 + X_L^2} + \frac{R}{R^2 + X_C^2}$$

- ckt resonates at all the freq.s.

$$J + R^2 = \frac{L}{c} \implies YT = 10000$$

If
$$\frac{1}{\omega_0 c} - \omega_0 L = 0 \implies Y_T = \frac{2R}{R^2 + \frac{L}{c}}$$

if $R^2 = \frac{L}{c} + \frac{1}{\omega_0 c} - \omega_0 L = 0 \implies Y_T = \frac{1}{R}$.

-> current at the resonance = v.yr.

case 4: Re xe

At Resonance, img (Y-total) = 0

$$\Rightarrow \frac{Rc}{Rc^2 + Xc^2} = \frac{RL}{RL^2 + XL^2}$$

$$\Rightarrow fo = \frac{1}{2\pi \sqrt{LC}} \left(\frac{RL^2 - L/C}{Rc^2 - L/C} \right)$$

for must be a real no, and should not be a complex no.

⇒ RL- 4c 70 & Rc- 4c 70.

A. an a series RLC, the applied voltage 2000,

R = 10 n, X = Xc = 20 n then Vc = ?

$$Q = \frac{l_0 \times L}{l_0 R} = \frac{20}{10} = 2$$

⇒ |VL| = |Vc| = QVS

= 2 x 200 = 400V

 $V_{c} = 400 L - 90^{\circ}$ $V_{L} = 400 L 90^{\circ}$

TVC VC

Q. In a series RLC, Q=100. If all the compo. s are doubled then Q'-?

$$Q = \frac{1}{R} \int_{C}^{L} dt = \frac{1}{2R} \int_{C}^{2L} = \frac{Q}{2} = 50.$$

Q In series RLC, If at f, 0.707 lead and
at the and at to 1/4/1
Per find d, at resonance $-$. $R^2 = \frac{L}{c}$ $2n$
$R^2 = \frac{L}{C}$ $\Rightarrow C = \frac{2}{4} = 0.5 f$
a find Resonant freq - ? 22 4th
$fo = \frac{1}{2\pi\sqrt{4}} = \frac{1}{4\pi}$
a Determine the current suffied by the source.
If the ckt is at resonance
V=10[26. 6 od 120m of
$V + \text{otal} = \frac{2R}{R^2 + \frac{1}{C}} = \frac{1}{4}$ $V + \text{otal} = \frac{2R}{R^2 + \frac{1}{C}} = \frac{4}{5}$ $V = \frac{1}{5}$
Y-total = 2R 4 7
(VOOR Sportlog 2+4/cm 511-5 200 12502 100 10 2
$\ell = VY = 10 \cdot 20^{6} \cdot X + \frac{4}{5} = 8 \cdot 20^{6}$
a find Resonant freq - as
2H 2H 2F 01 MANAGEMENT OF THE PROPERTY OF THE
H - 1 +19 +2 H 905 X S
Leg = L1+L2+2M 008 x 5
to = 2TT They'C
a. In the ckt shown vfl are in phase (resonance)
The value of k and the polarity of coil pa
ave doubled o the control of the con
are -
$\frac{1}{\sqrt{-J/2}} \frac{(k)p \rightarrow a}{10vL} \frac{x}{J8} \frac{x}{J8} = x_{L} + x_{L2} \pm 2x_{m}$

2).
$$X_L = X_C = |2| = 8 + 8 - 2 \times m$$
 $\Rightarrow X_m = 2 \cdot L$
 $H = K \sqrt{L_1 L_2} \Rightarrow K = \frac{H}{\sqrt{L_1 L_2}} = \frac{WH}{\sqrt{WL_1 \times WL_2}}$

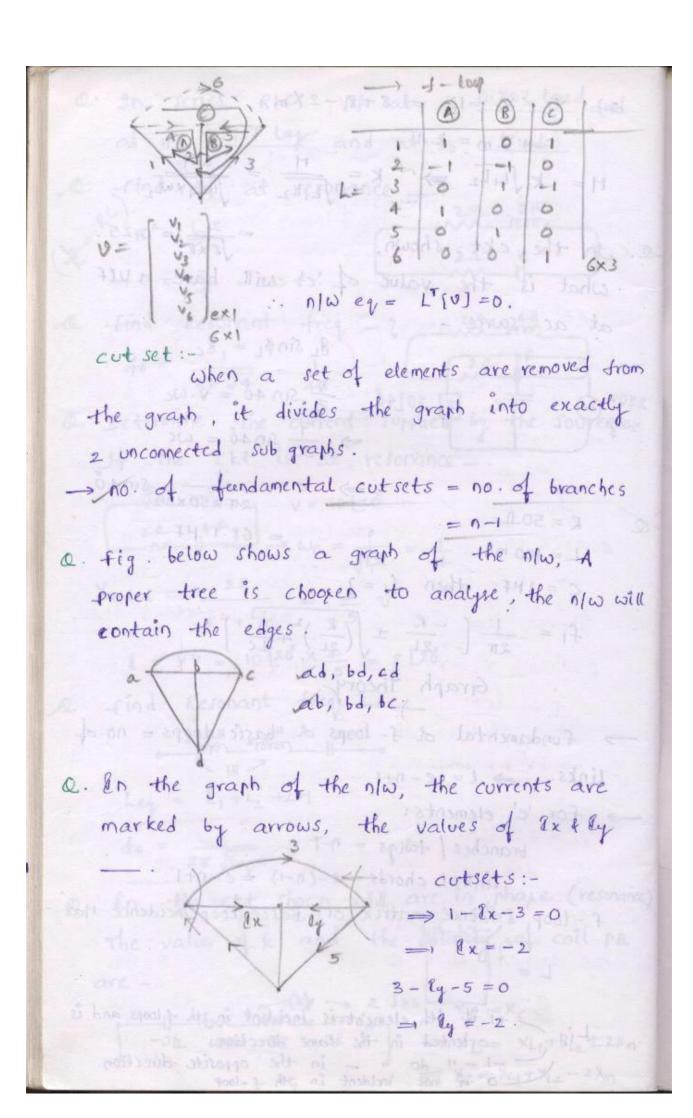
2. In the ckt shown,

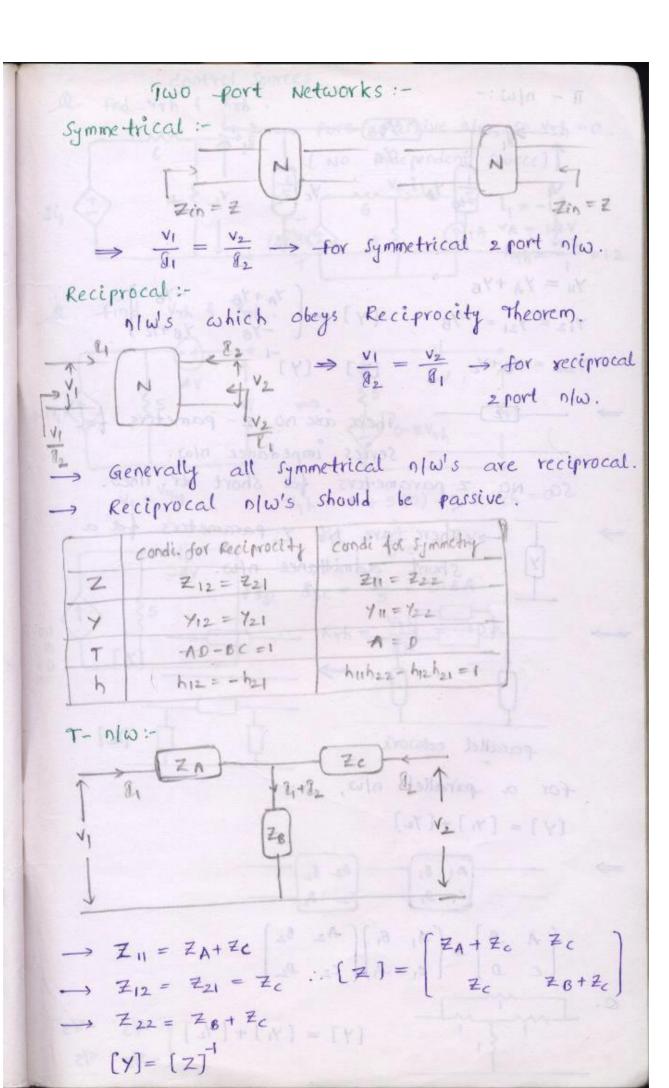
 $\frac{2}{\sqrt{8 \times 8}} = 0.25$.

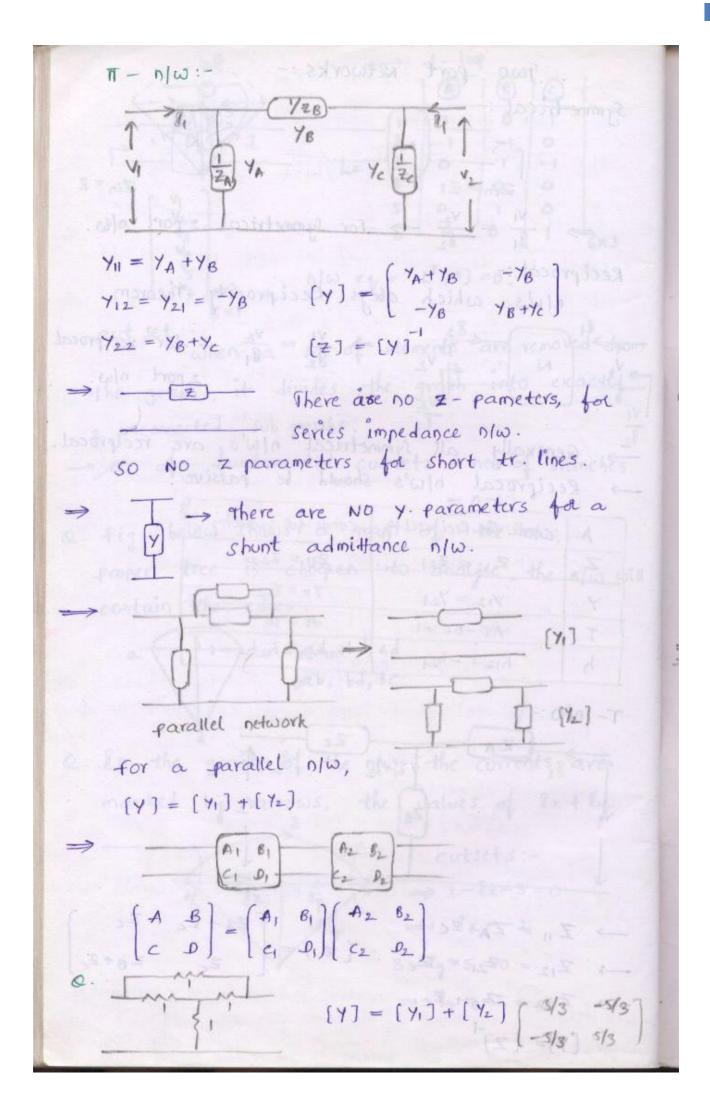
What is the value of 'c' will have a UIF

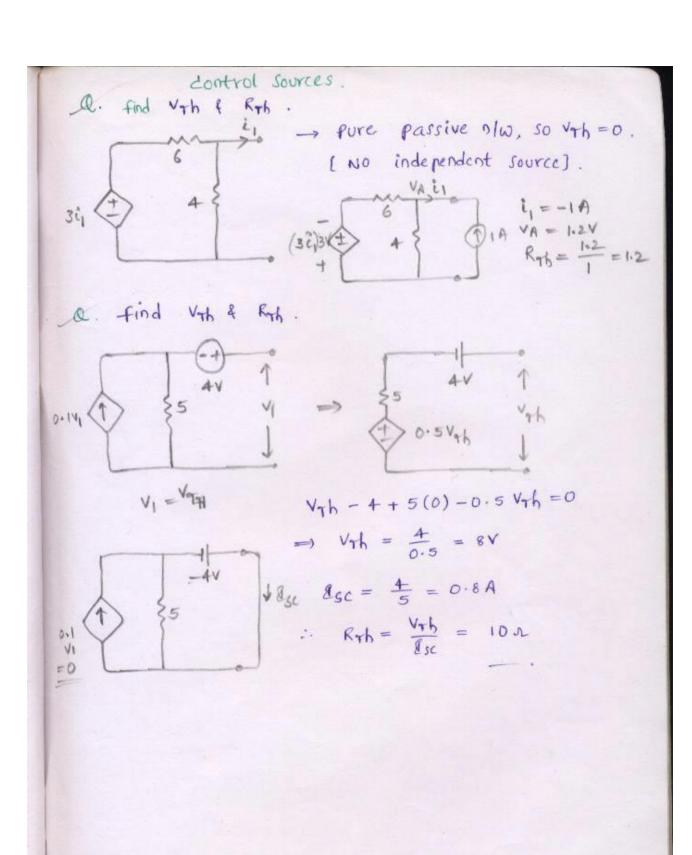
at ac source -

 $\frac{8L \sin \beta_L}{\sin \beta_L} = \frac{8L}{2L}$
 $\frac{230V}{\cos \delta_L} \Rightarrow \frac{1}{30} \sin \delta_L = \frac{8L}{2L}$
 $\frac{1}{30} \sin \delta_L = \frac{8L}{2$









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SET - 1

I B. Tech II Semester Regular Examinations, September- 2021

NETWORK ANALYSIS

(Comm. to ECE, EIE, ECT)

Time: 3 hours Max. Marks: 70

Answer any five Questions one Question from Each Unit All Questions Carry Equal Marks

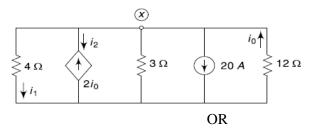
UNIT-I

1 a) Distinguish between Ideal sources and practical sources

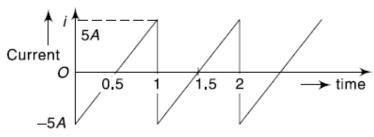
(3M) (4M)

(7M)

- b) Two resistors 2R and 3R are connected in parallel across a 5A DC current source. The voltage that appears across the current source is 30V. Find R and the power dissipated in each resistor.
- c) Find i_0 , i_2 and the value of the dependent source for the following network:

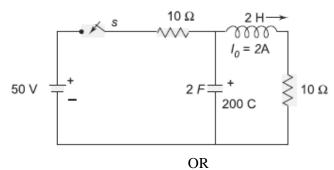


- 2 a) Explain about incidence matrix and its properties and also analyze the relationship (7M) between KCL and incidence matrix.
 - b) Find the average and rms value for the following waveform: (7M)



UNIT-II

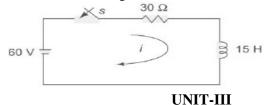
For the circuit shown below, the initial current in the inductance is 2 A and its direction is as shown in the figure. The initial charge on the capacitor is 200 C with polarity as shown when the switch is closed. Determine the current expression for the inductance.



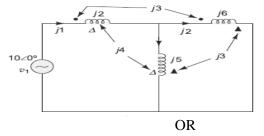
4 a) Analyze the dc response for a series R - L - C circuit.

(7M) (7M)

b) A series RL circuit with $R = 30 \Omega$ and L = 15 H has a constant voltage V = 60 V applied at t = 0 as shown in figure below. Determine the current i, the voltage across resistor and the voltage across the inductor.



- 5 a) Explain the concept of Dot convention in magnetically coupled circuits and derive (7M) the expression for coefficient of coupling in terms of mutual and self-inductances of the coils.
 - b) Find the current passing through all the elements using mesh analysis for the following circuit. (7M)



- 6 a) Explain step by step procedure of phasor analysis for a Series RLC circuit. (7M)
 - b) A series ac circuit has a resistance of 15 Ω and an inductive reactance of 10 Ω . (7M) Calculate the value of a capacitor which is connected across this series combination so that the system has unity power factor. The frequency of ac supply is 50 Hz.

UNIT-IV

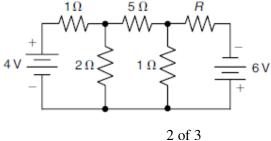
- 7 a) What is resonance in an ac circuit and discuss the effects of resonance in electrical (3M) systems
 - b) Define the terms 'Q factor' and 'band width' w.r.t ac circuits. (4M)
 - c) Voltages across resistance, inductance and capacitance connected in series are 3 V, 4 V and 5 V respectively. If supply voltage has 50-Hz frequency, what is the magnitude of supply voltage? Find the resonant frequency of this series RLC circuit.

OR

8 a) State and explain maximum power transfer theorem.

(4M) (10M)

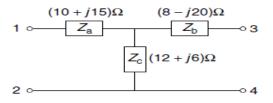
b) Find the value of R in the following circuit, such that maximum power transfer takes place. What is the amount of this power?



SET - 1

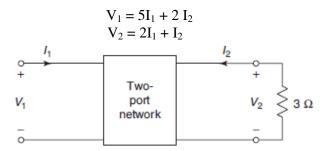
UNIT-V

- 9 a) Derive the h parameters of a two-port network. (7M)
 - b) Find Z parameters for the following network: (7M)



OR

- 10 a) Deduce the relationship between impedance and admittance matrix. (7M)
 - b) The following equations give the voltages V_1 and V_2 at the two ports of a two port network as shown in the following figure: (7M)



A load resistor of 3 Ω is connected across port 2. Calculate the input impedance.